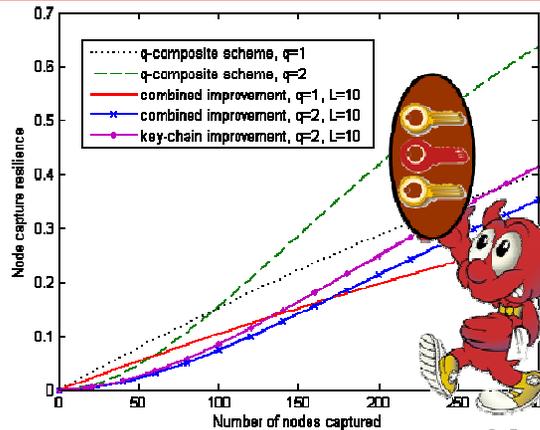


Two Improvements of Random Key Predistribution for Wireless Sensor Networks

Jiří Kůr, Vashek Matyáš, Petr Švenda

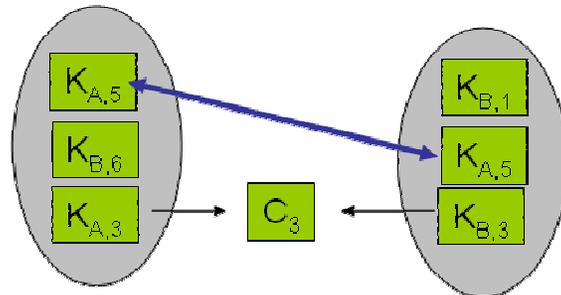
Faculty of Informatics

Masaryk University

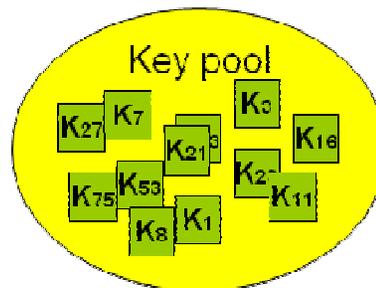
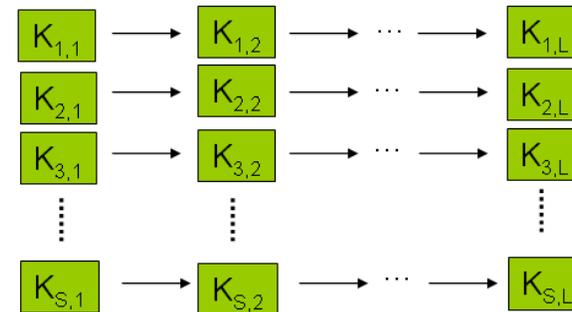


Capture resilience improvements

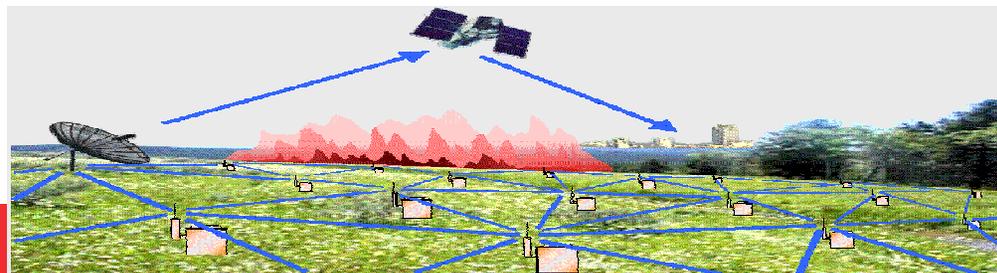
Collision key improvement



Key-chain improvement



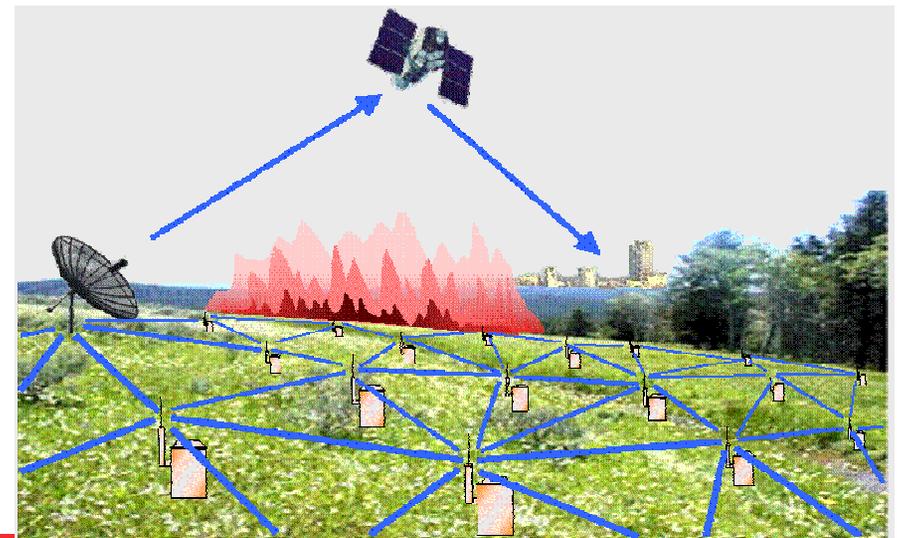
Eschenauer & Gligor 2002
Chen et al. 2003



Wireless Sensor Network (WSN)

- Sensor nodes
 - environmental sensors
 - RF transceiver
 - battery powered
 - low computational and memory resources
 - 8-bit processor, 4KB RAM, < 128KB EEPROM
 - number of nodes: $10 - 10^5$
- Topology
 - self-organized topology
 - ad-hoc position/neighbors – not known in advance
 - multi-hop communication

- Base station(s)
 - lap-top capabilities
 - almost unlimited energy resources



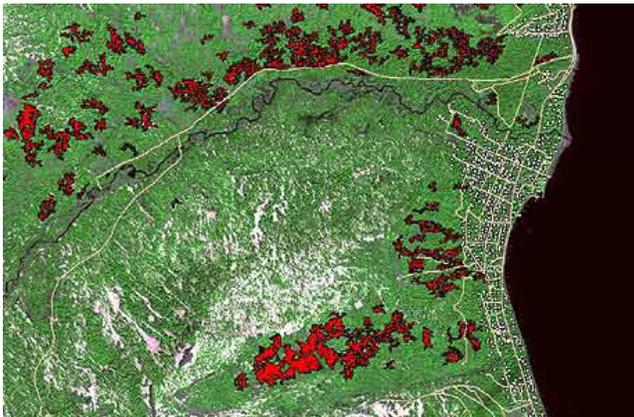
Applications of WSNs



Traffic control



Medical information



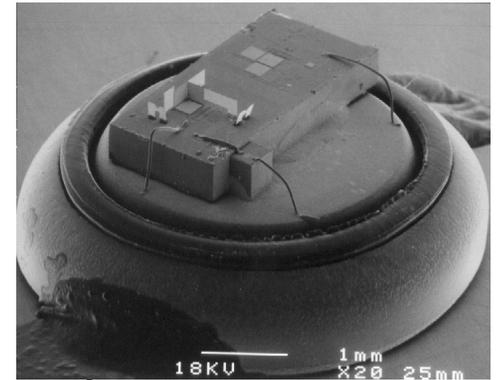
Remote fire detection



Combat field control

Some differences from standard networks

- Running on battery (limited resource)
 - days for personal network
 - years for large scale monitoring network
 - especially communication is energy-expensive
- Relatively limited computation power
 - powerful CPU possible, but energy demanding
- Nodes can be captured by an attacker
 - all secrets can be extracted from unprotected nodes
 - and returned back as malicious node

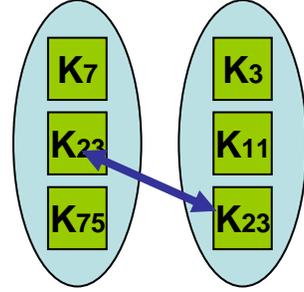


Many ways how to establish keys

Asymmetric
cryptography



Random key
pre-distribution

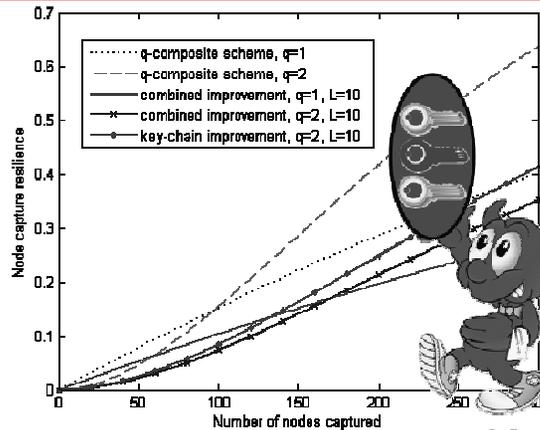


Trusted party



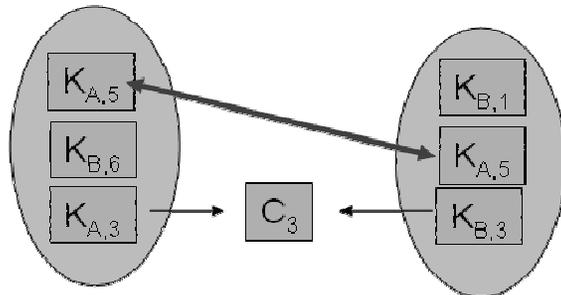
Master key,
pairwise keys



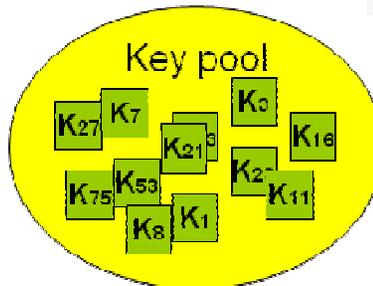
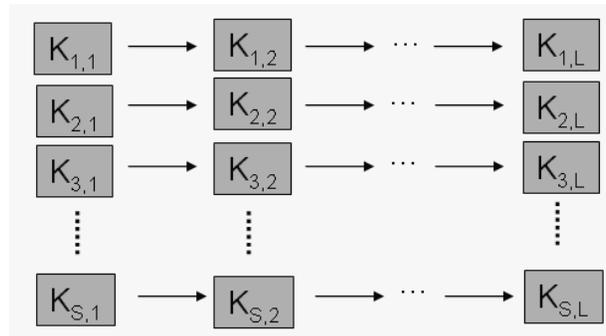


Capture resilience improvements

Collision key improvement

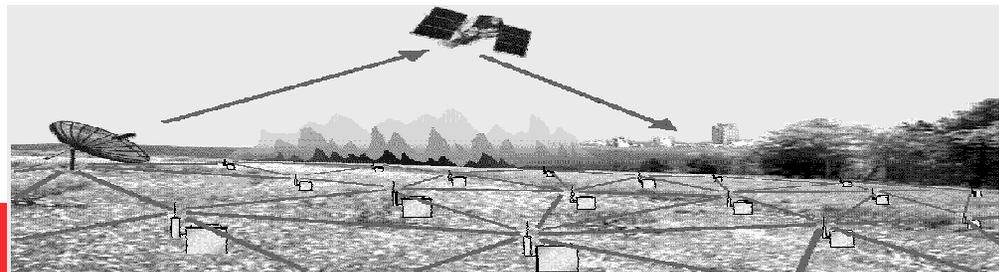


Key-chain improvement



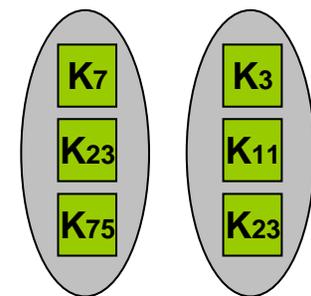
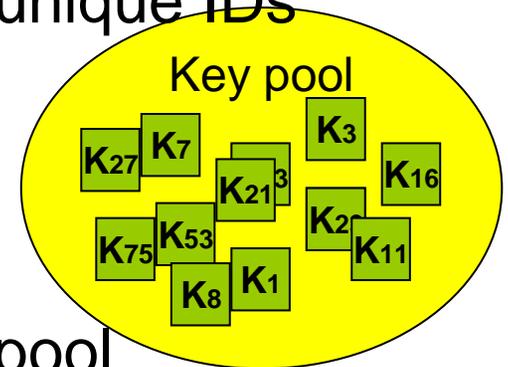
Eschenauer & Gligor 2002

Chen et al. 2003

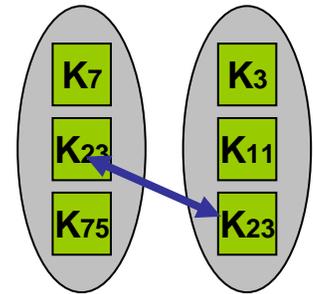


Random key pre-distribution

- *Eschenauer & Gligor 2002, Chen et al. 2003*
- Elegant idea with low memory requirements
 - based on birthday paradox
 - large pool of **S** cryptographic keys with unique IDs used
- For every node prior deployment:
 1. randomly select **m** keys from large key pool
 2. return selected keys back to pool
 3. proceed with next node

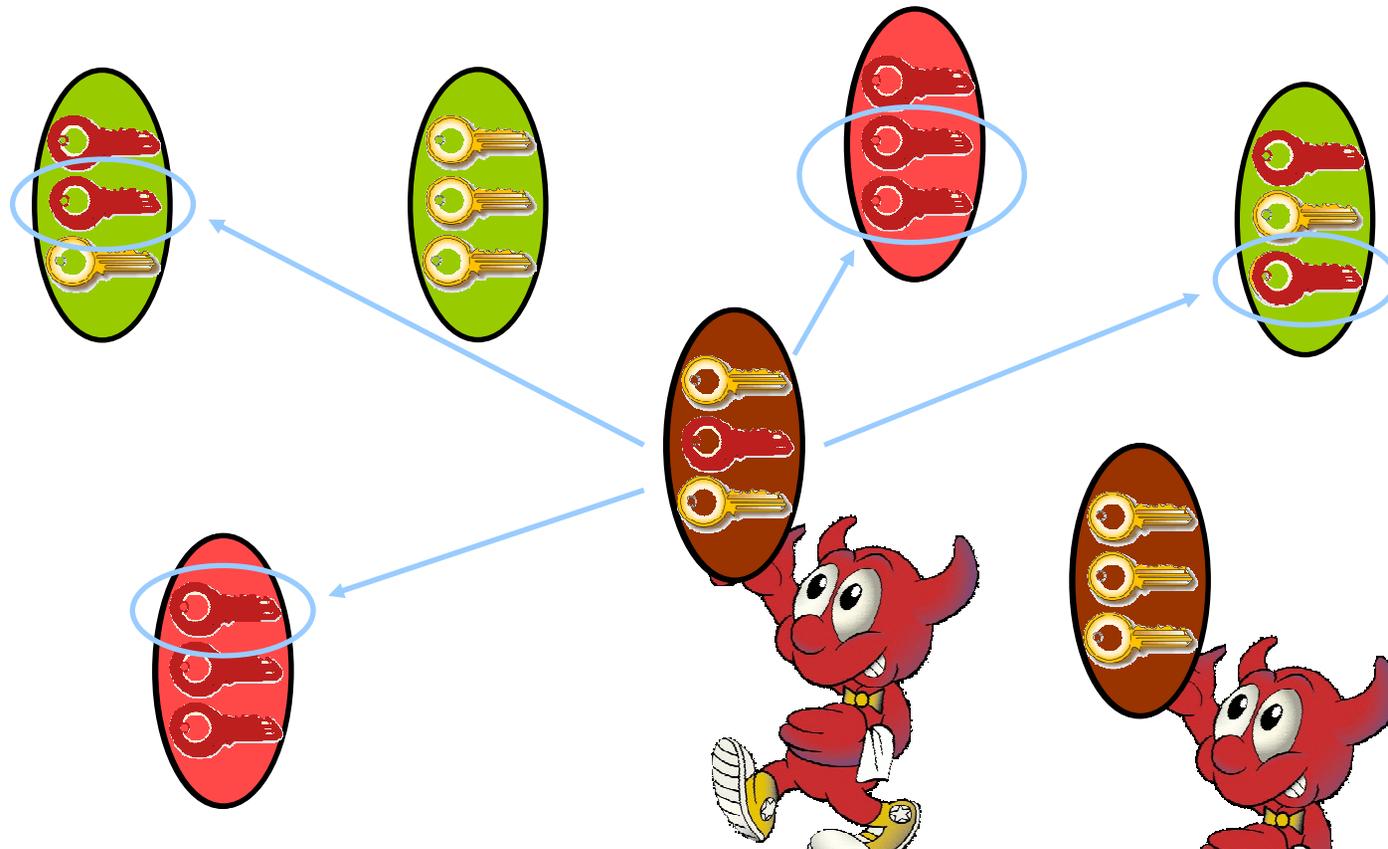


Random key pre-distribution (2)



- During neighbour discovery:
 1. neighbours establish radio communication
 2. nodes iterate over their keyrings for shared key(s)
 3. if shared (by chance) key(s) are found, secure link is established
- What is key sharing probability?
 - e.g., 100 keys from 10000
 - 64% probability at least one key shared
- q -composite scheme – at least q keys shared
- Not all nodes can establish secure link
 - but sufficient connectivity probability can be set

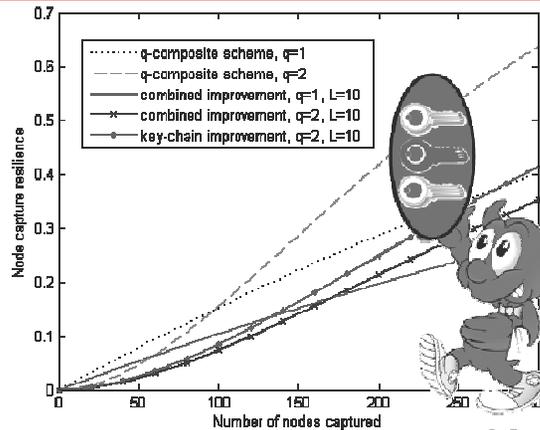
How random key pre-distribution fails



- Keys from uncaptured nodes compromised as well
- Good tradeoff between memory and security

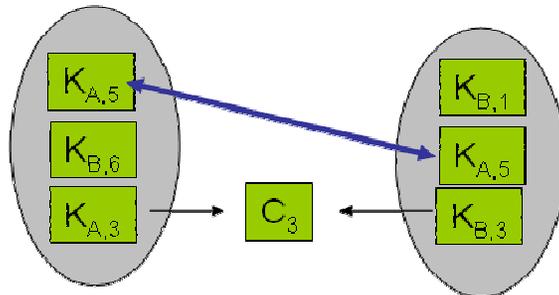
Random key pre-distribution - parameters

- S ... key pool size
- m ... key ring size
 - node memory limitation
- P ... probability that two nodes share at least q keys
 - dependent on m , key pool size S and q
 - we can calculate minimal P required so the network graph remains connected
- ncr ... node capture resilience
 - assume attacker randomly captured n nodes
 - fraction of secured links between uncaptured nodes that are compromised using keys from captured nodes

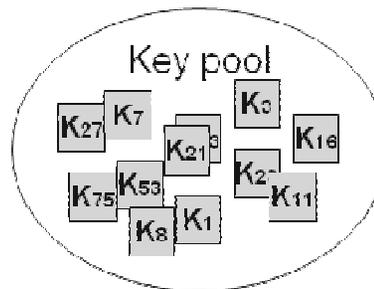
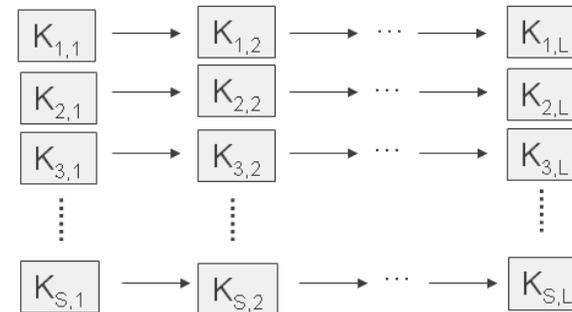


Capture resilience improvements

Collision key improvement

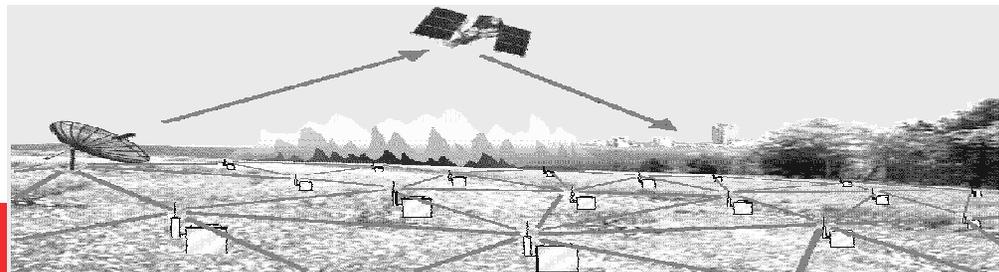


Key-chain improvement



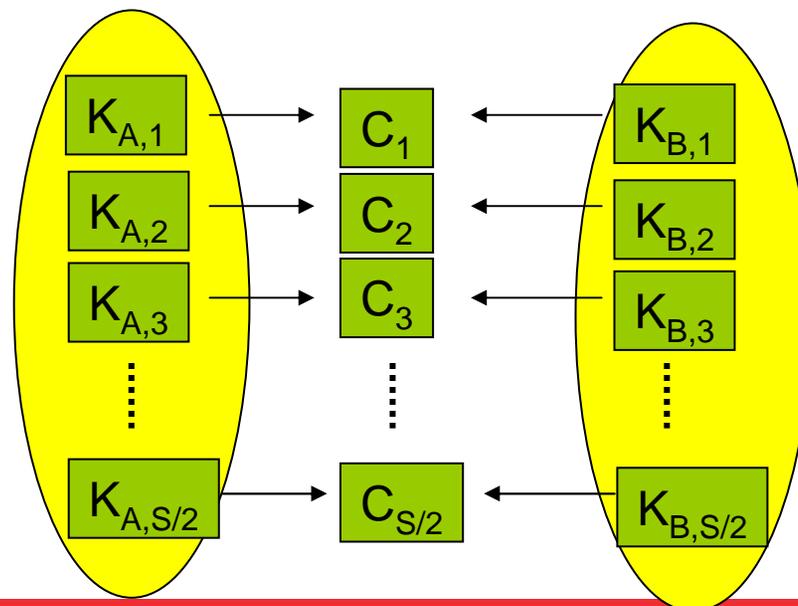
Eschenauer & Gligor 2002

Chen et al. 2003



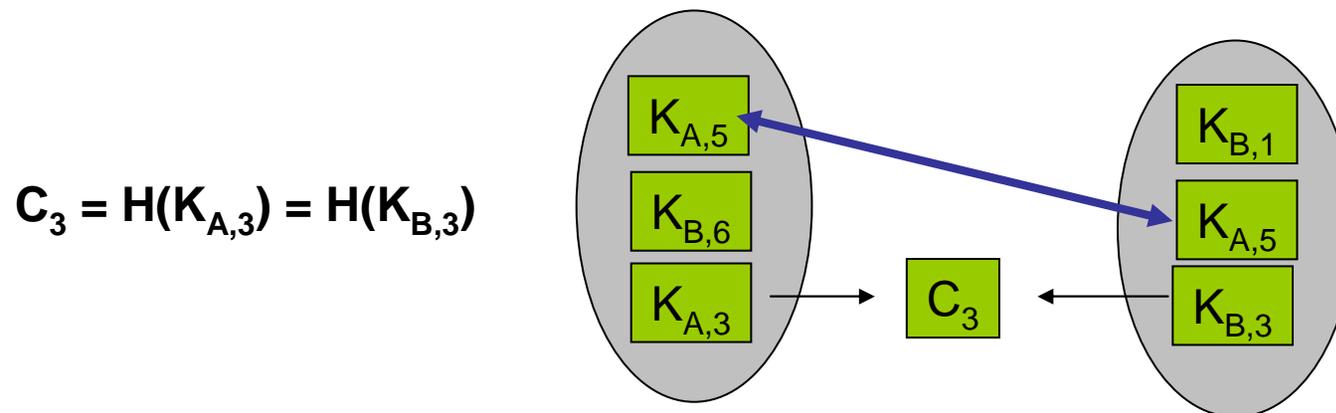
Collision key improvement

- Key pool created using $S/2$ related key pairs K_A, K_B
- $C = H(K_A) = H(K_B)$
- H is cryptographically secure hash function with a limited input/output length, e.g. 80 bits
- Such collisions can be found with moderate computational power



Collision key improvement (2)

- For every node prior deployment:
 1. randomly select m keys (*no related key pair* is allowed)
 2. return selected keys to a key pool
 3. proceed with next node
- During neighbor discovery:
 - beside normal keys, also collision keys can be shared
 - probability of link key establishment is higher

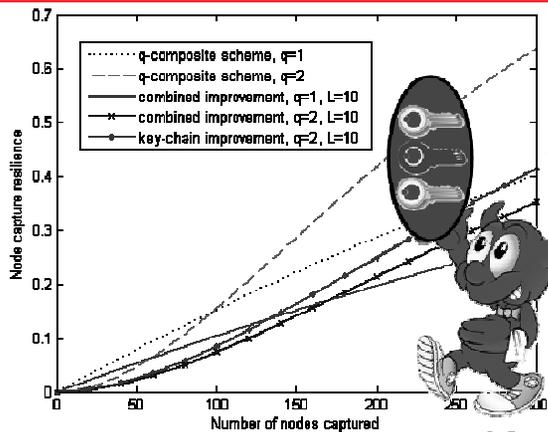


Key pool construction

- To find an n-bit collision approx. $2^{n/2}$ hash operations are needed
- To find c^2 collisions, approx. $c * 2^{n/2}$ hash operations are needed

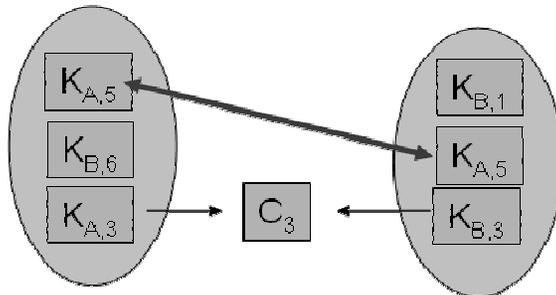
- Goal: to find 80-bit collisions in SHA-2
- Method: Van Oorschot and Wiener's parallel collision search
 - time-memory trade-off approach
- Hash operations computed: approx. 2^{47}
- Over 2^{12} collisions found - enough for key pool

- Aggregate time spent on single 3GHz core: 19 000 hours
- We have used BOINC framework and approx. 1000 cores
 - Final time: approx. 19 hours
 - GPUs could bring significant speed up

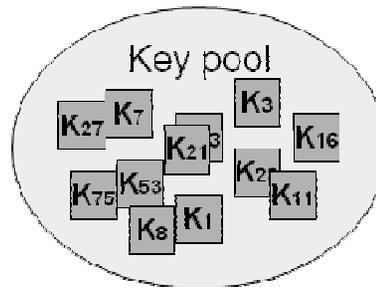
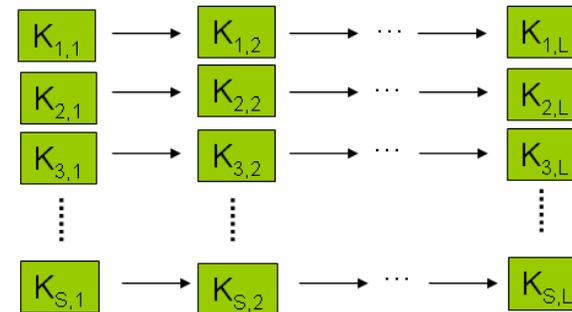


Capture resilience improvements

Collision key improvement

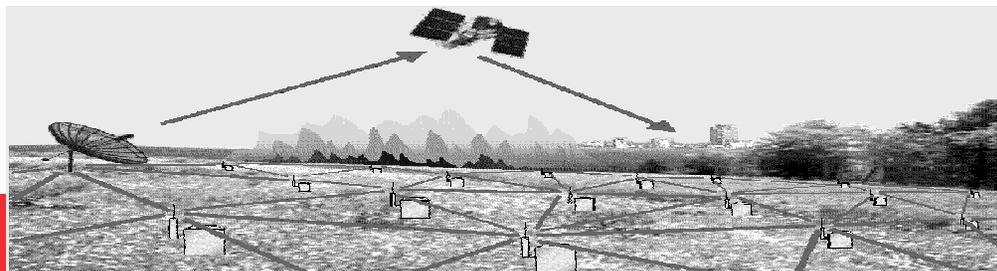


Key-chain improvement



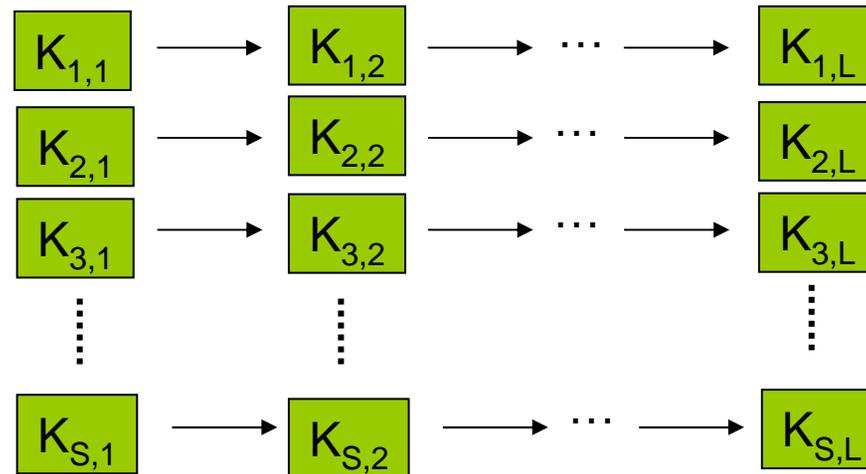
Eschenauer & Gligor 2002

Chen et al. 2003



Key-chain improvement

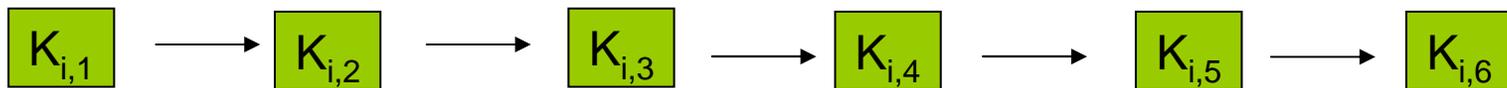
- Key pool created using S hash chains of a length L



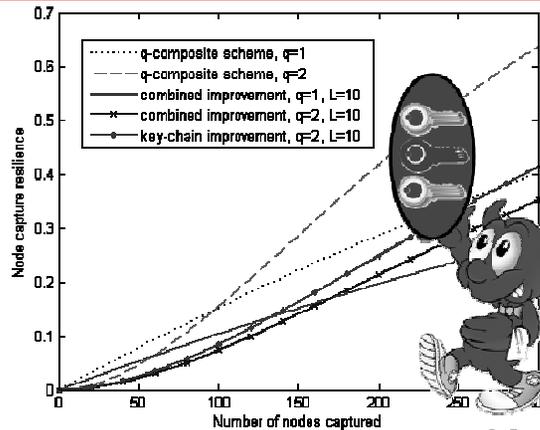
- For every node prior deployment:
 1. randomly select m hash chains
 2. randomly select single key from every selected chain
 3. return selected chains (keys) back to pool
 4. proceed with next node

Key-chain improvement (2)

- During neighbor discovery:
 - two nodes can calculate shared key if they possess keys from the same hash chain (with index i)

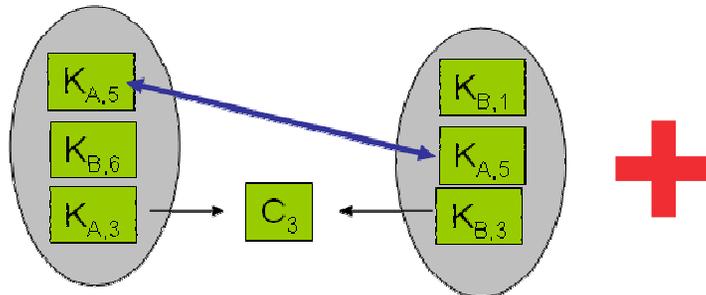


- Probability of key establishment remains as in original design
- Node capture resilience improves
 - attacker may capture keys that are further in the chain
 - slightly better than in collision key improvement
- Hash chains for key predistribution used also in *Ren et al. 2006*
 - different key ring construction, keyed hash function used

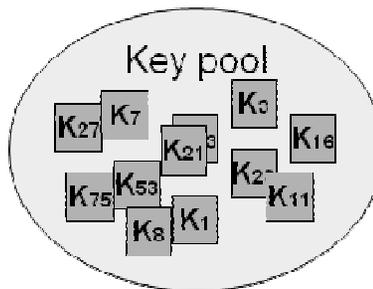
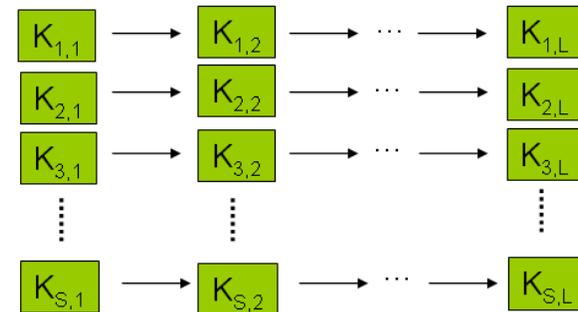


Capture resilience improvements

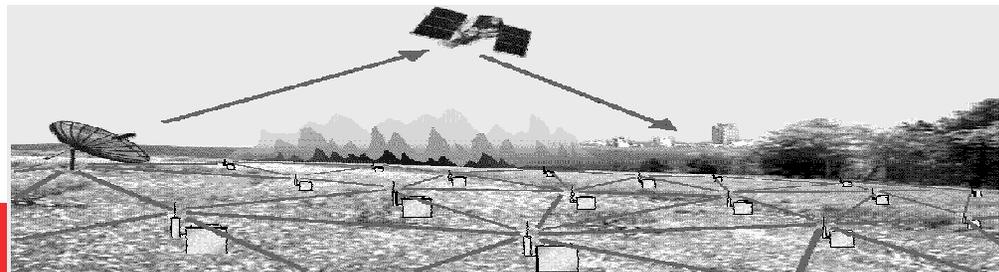
Collision key improvement



Key-chain improvement

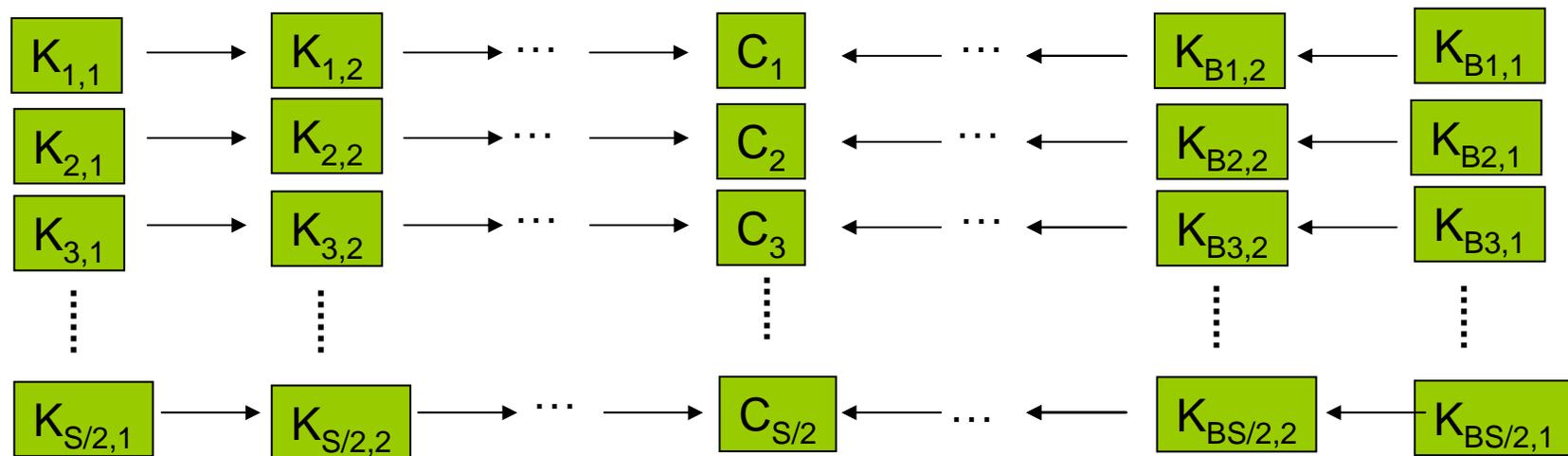


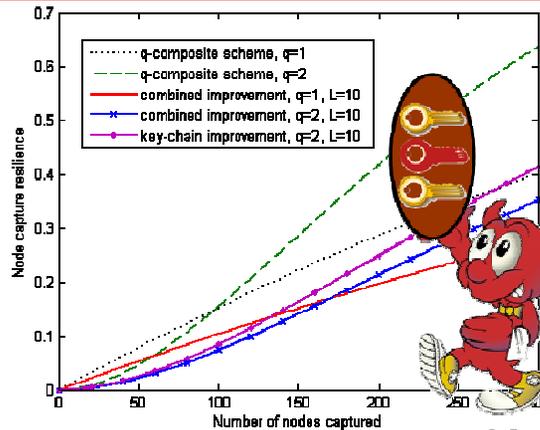
Eschenauer & Gligor 2002
Chen et al. 2003



Combination of improvements

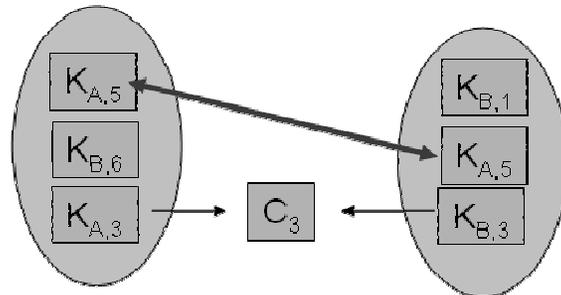
- Both improvements can be easily combined
- Collision search produces colliding hash chains



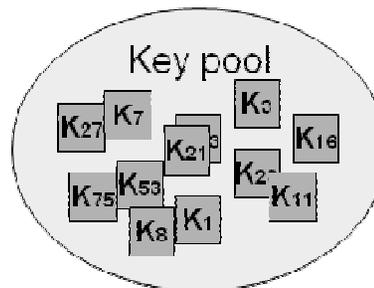
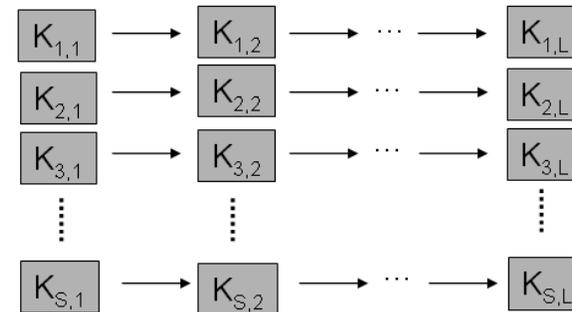


Capture resilience improvements

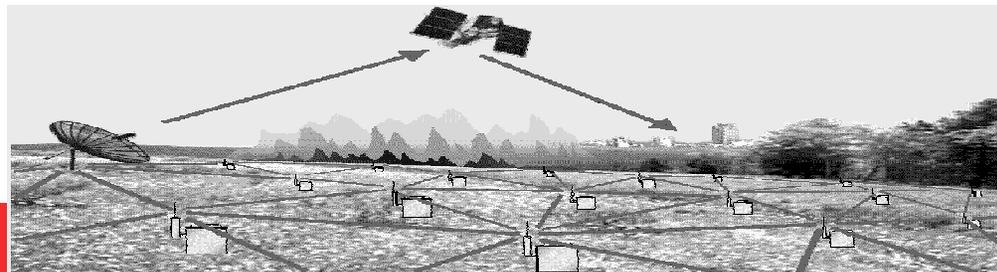
Collision key improvement



Key-chain improvement



Eschenauer & Gligor 2002
Chen et al. 2003



Combination of improvements - evaluation

- $P = 0.33, m = 200$

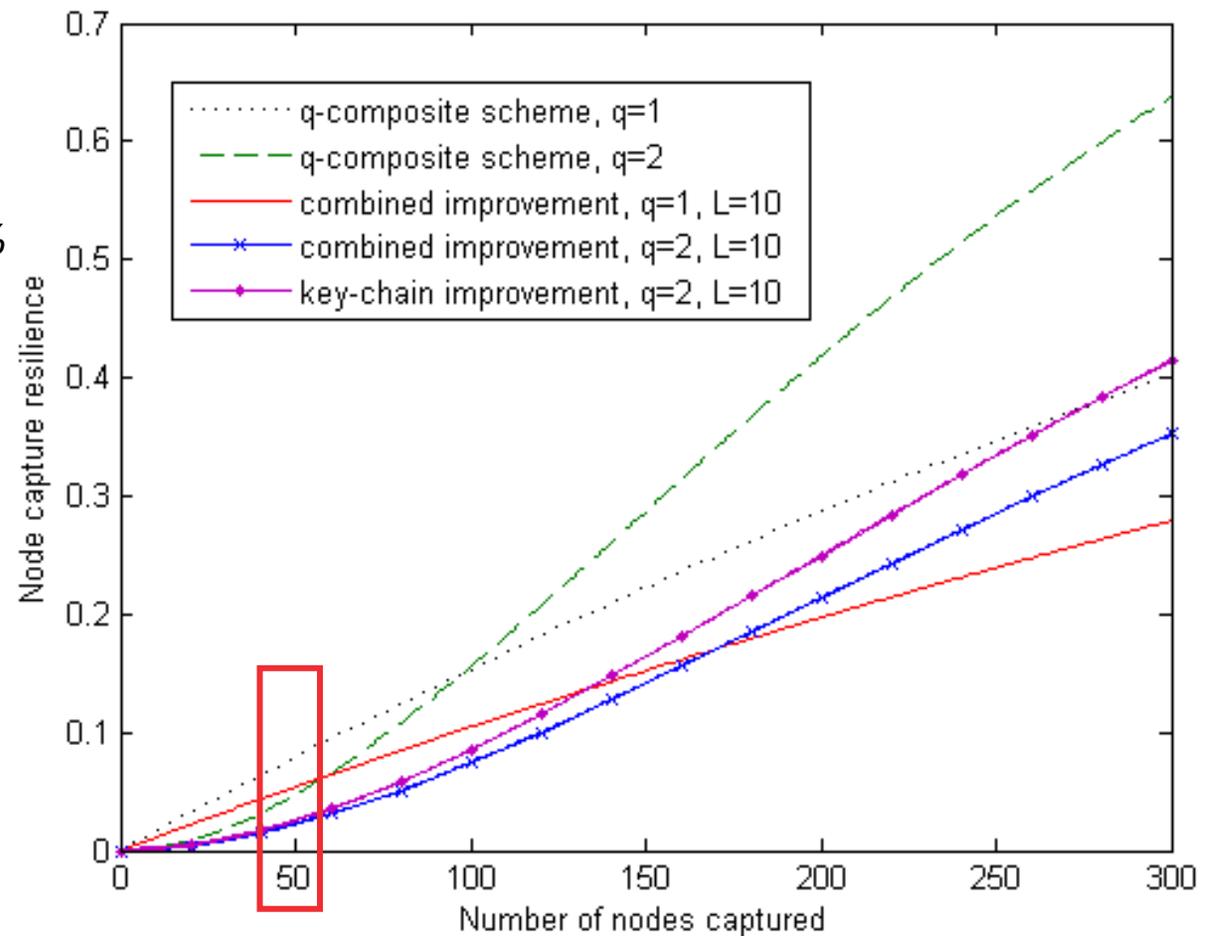
- For $q = 2$ and $n = 50$

- *q*-composite: $ncr = 4.7\%$

- Collision key: $ncr = 2.7\%$

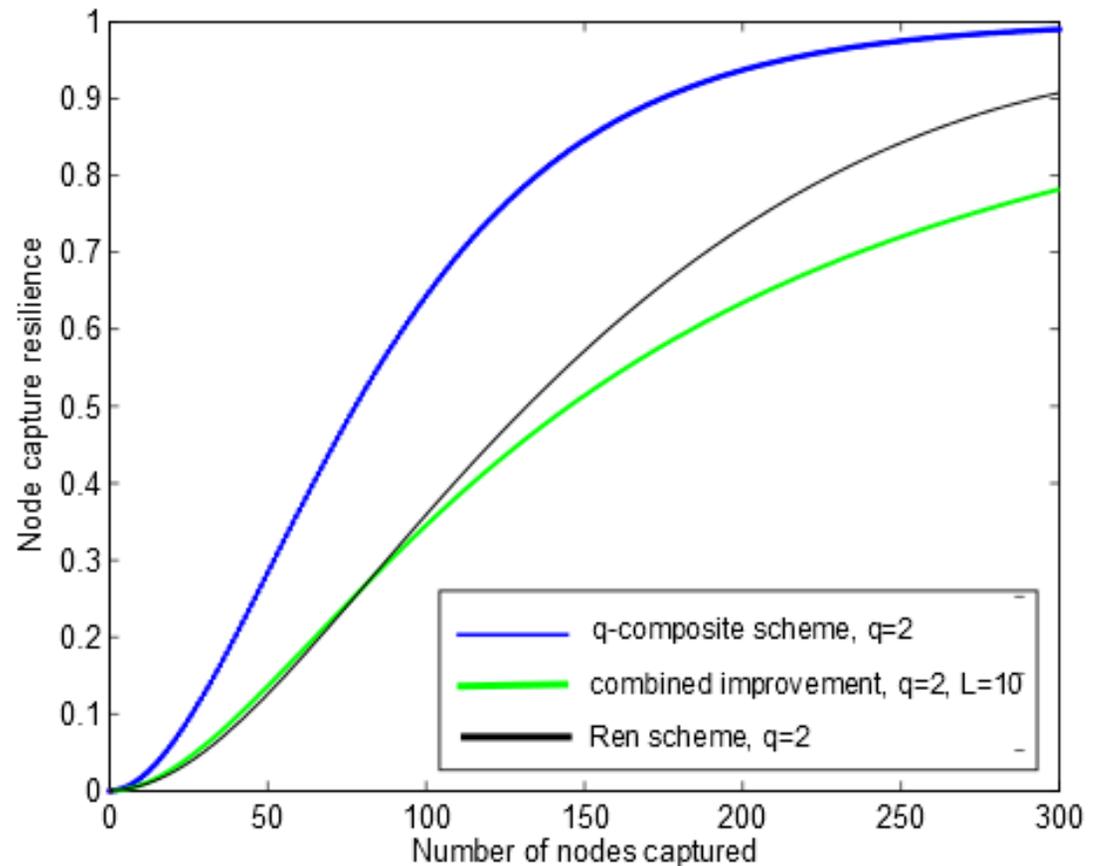
- Key-chain: $ncr = 2.5\%$

- Combined: $ncr = 2.2\%$



Comparison with Ren et al.

- *Ren et al. 2006*, random key predistribution based on keyed hash chains
- $P = 0.5$, $m = 90$
- Ren scheme setting
 - $R_0 = 10$, $R_1 = 79$,
 - $L = 1\ 000$, $K = 100\ 000$
- Combined improvement outperforms Ren scheme if number of nodes captured is high



Summary

- Eschenauer & Gligor 2002 is one of core schemes
 - many existing schemes extends or builds on it
- Two improvements of this core scheme proposed
 - security performance of extensions also influenced
- Hash collisions can be used in favor of security
 - limited length collisions with moderate CPU resources
- Unkeyed hash chain instead of single key used
- Both improvements combinable
- Results verified both analytically and with network simulator

Thank you for your attention.

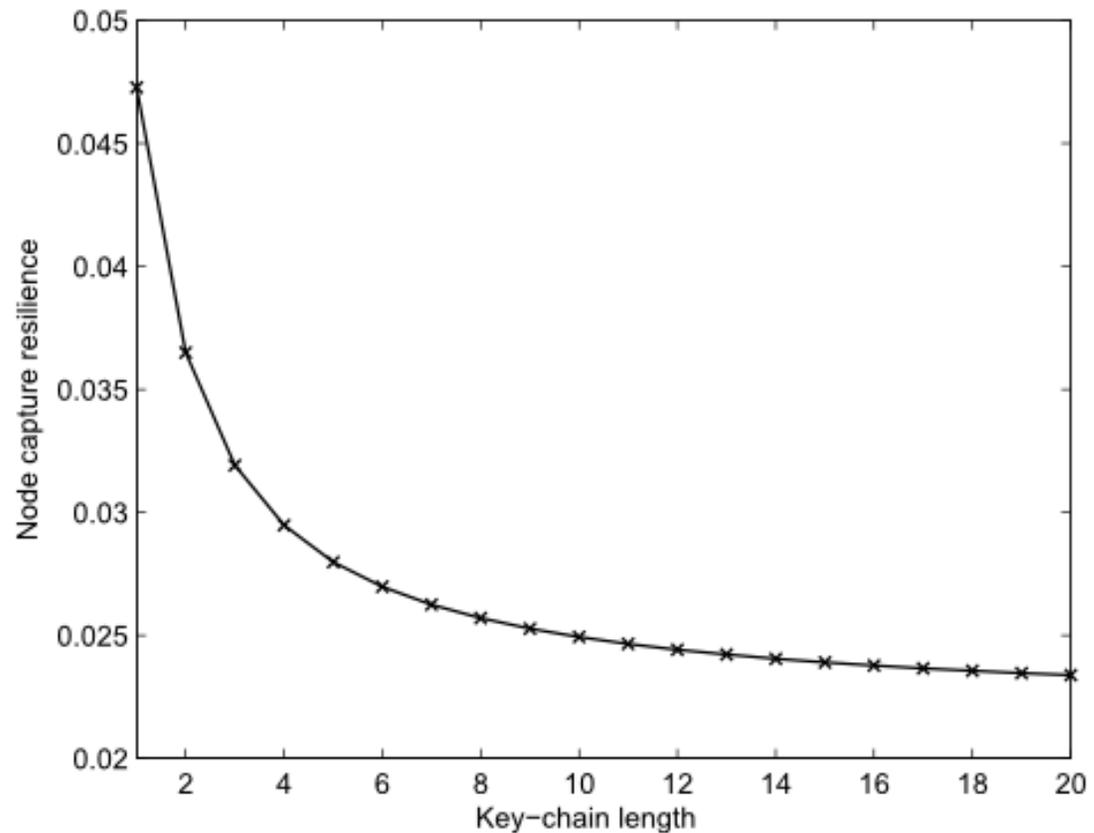
Any questions?

References

- [Eschenauer & Gligor 2002] Eschenauer, L., Gligor, V.D.: A key-management scheme for distributed sensor networks. In: 9th ACM conference on Computer and Communications Security, CCS'02, pp. 41-47. ACM, New York (2002)
- [Chan et al. 2003] Chan, H., Perrig, A., Song, D.: Random key predistribution schemes for sensor networks. In: Symposium on Security and Privacy, 2003, pp. 197-213. IEEE, (2003)
- [van Oorschot & Wiener 1999] van Oorschot, P.C., Wiener, M.J.: Parallel collision search with cryptanalytic applications. *Journal of Cryptology*, 12(1):1-28, (1999)
- [Ren et al. 2006] Ren, K., Zeng, K., Lou, W.: A new approach for random key pre-distribution in large-scale wireless sensor networks. *Wireless Communications and Mobile Computing*, 6(3):307-318, (2006)

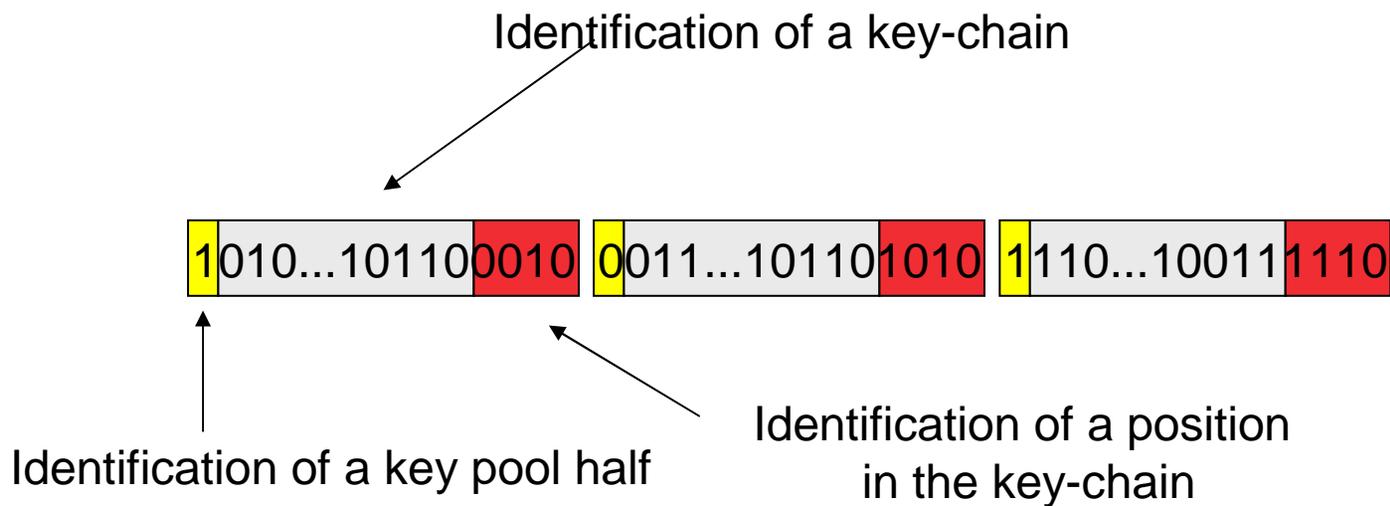
Key-chain length

- The longer the chain the better the resilience, but ...
- Effective chain length is ...
 - number of different keys assigned to sensors
 $P=0.33$
 - dependent on number of sensors
 $m=200$
 - dependent on number of keys
 $q=2$
- Practical value is ...
 $n=50$



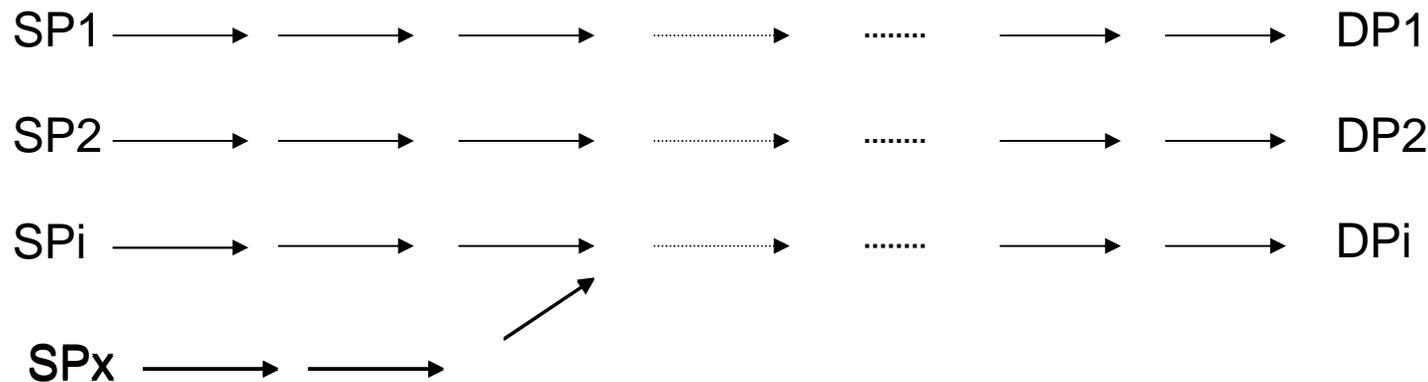
Seed based predistribution

- Generate pseudorandom stream using neighbor ID and pseudorandom number generator



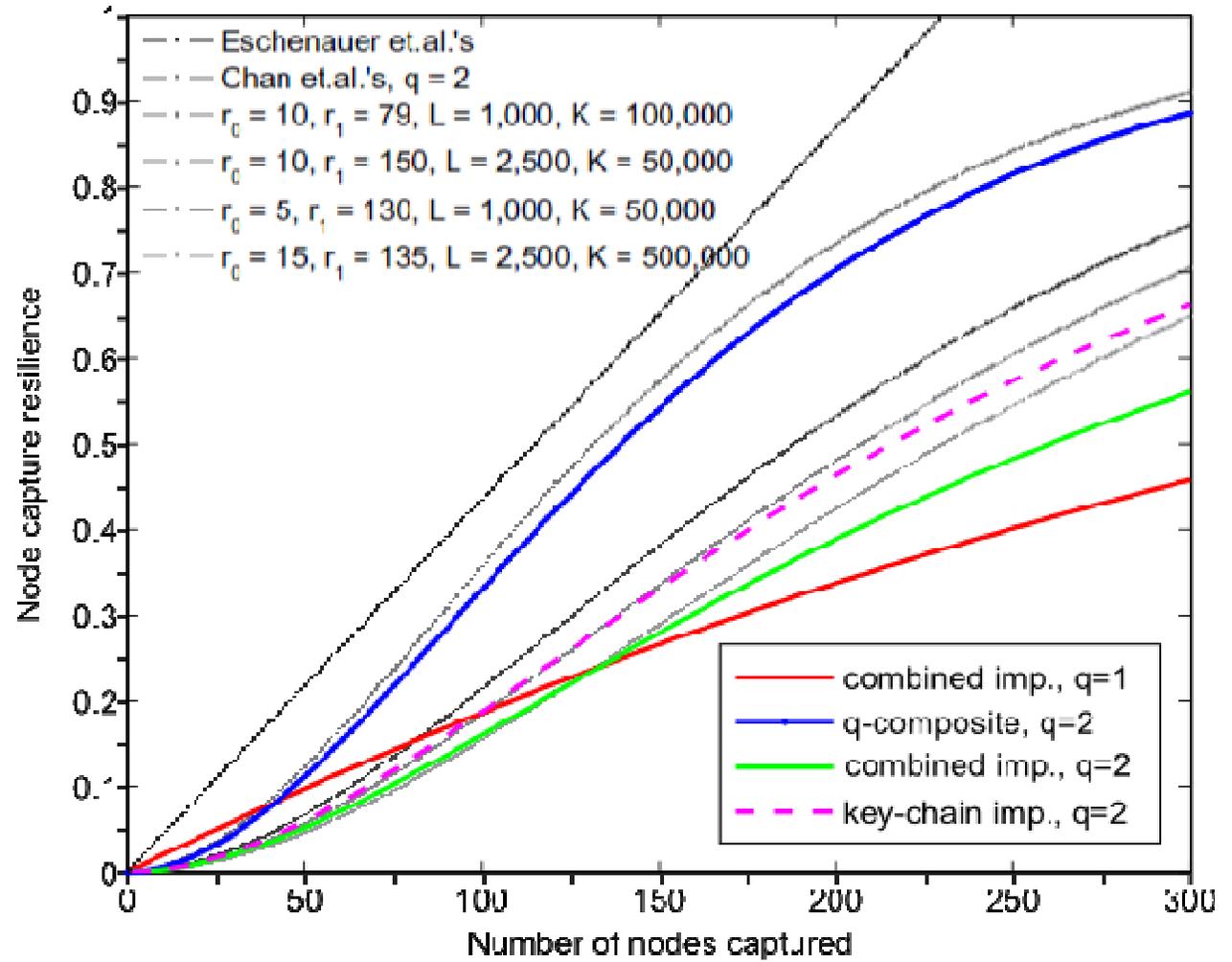
Key pool construction

- Van Oorschot and Wiener's parallel collision search
 - time-memory trade-off approach
- SP – random 80-bit starting point
- DP – 80-bit distinguished point, fixed number of leading zeros
- (SP_i, DP_i) pairs stored in memory



Comparison with Ren et al.

- $P = 0.5, m = 161$



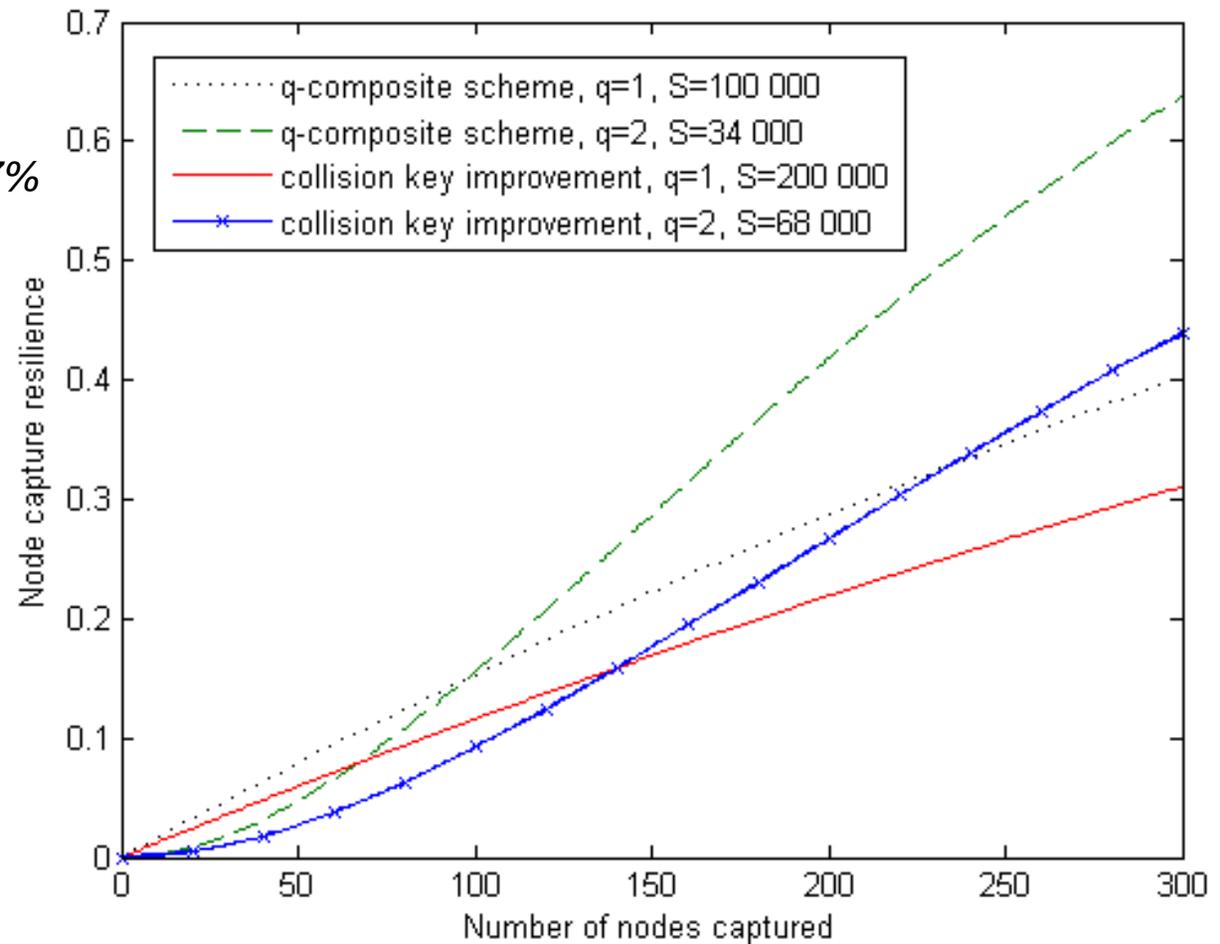
Collision key improvement – evaluation

- $P = 0.33, m = 200$

- For $q = 2$ and $n = 50$

- q -composite $ncr = 4.7\%$

- Improved $ncr = 2.7\%$



Key chain improvement - evaluation

- $P = 0.33, m = 200$

- For $q = 2$ and $n = 50$

- q -composite $ncr = 4.7\%$

- Improved $ncr = 2.5\%$

