Measuring Item Similarity in Introductory Programming: Python and Robot Programming Case Studies

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ABSTRACT
A personalized learning system needs a large pool of items for learners to solve. When working with a large pool of items, it is useful to measure the similarity of items. We outline a general approach to measuring the similarity of items and discuss specific measures for items used in introductory programming. Evaluation of quality of similarity measures is difficult. To this end, we propose an evaluation approach utilizing three levels of abstraction. We illustrate our approach to measuring similarity and provide evaluation using items from three diverse programming environments.

INTRODUCTION
A key part of learning is active solving of educational items (problems, questions, assignments). For high-quality education, we need large pools of items to solve. Even teachers in classical education often work with many items. In personalized computerized educational systems, the need for a large pool of items is even higher – if we want to provide a personalized experience for individual learners, we need to be able to choose from a wide set of items.

To use a large item pool efficiently, we need to be able to navigate it. For this, it is very useful to be able to measure the similarity of individual items. How can we measure the similarity of educational items? From a spectrum of similarity measures, how do we pick a suitable one? These are the basic questions that we address in this paper.

Similarity measures have many applications, particularly in adaptive learning systems. Similarity measure can be very useful for automatic recommendations of activities. If a learner solved an item, but with a significant effort, it may be useful to recommend as a next item another very similar item, so that the learner can get more practice. On the other hand, if a learner solved the current item easily, it is more meaningful to recommend dissimilar items. If a learner struggles with an item, the system may provide a hint or a suitable worked example (a solution to a similar item) based on the similarity measure. Similarity measure can be used in learner and domain modeling: based on the similarity between items, we may define knowledge components and estimate knowledge of learners. Similarity measures may be useful in the user interface, e.g., for enabling learners to navigate the item pool and manually pick an item to solve, or for visualization of the open learner model.

In addition to the use in automatic adaptation, similarity measures can be also very useful for empowering humans by providing useful and actionable insight (see [1] for a general discussion of this approach). For developers of learning systems and content creators, similarity measure facilitates the management of an item pool, e.g., the identification of redundant, duplicate, or missing items. Suitably presented data on item similarity may be very useful for teachers, instructional designers, or textbook authors. Such data may be useful for example for guiding the choice of items for an exam – typically we want items in an exam to be similar, but not very similar to items practiced during learning. Data on item similarity may provide impulses for the organization of classes, instructional materials, or creation of other educational resources (e.g., worked examples). In systems with crowdsourced content creation, the size of item pool may be very large and similarity measures may be fundamental for efficient utilization of available resources.

In most domains, there is no single correct measure of item similarity. Particularly there may be a difference between item similarity based on superficial features (a cover story) and deep features (a principle of solution), which are related to different perspectives of novices and experts. For some applications, it may be useful to work with several similarity measures.
Write a function that outputs divisors of a given number.

def divisors(n):
    for i in range(1, n + 1):
        if n % i == 0:
            print(i, end=" ")
    print()

In this work we focus on the study of similarity of programming problems in the context of introductory programming, specifically for programming exercises in Python and programming problems with a robot on a grid, using a simplified graphical programming language as used for example in popular Hour of code activities. Figure 1 provides examples of problems and solutions from the three specific environments that we use throughout this paper. There are other domains with complex items, where measuring the similarity of items may be useful, for example mathematics, physics, or chemistry. Introductory programming has the advantage that the item statements and solutions are more easily processed and learners’ solutions are also readily available. Progress on a programming problem is done directly on a computer and easily stored; as opposed to physics problems, which are still more naturally solved on a paper. Currently, we focus only on programming problems, but the general approach is applicable also to other settings – therefore, we use the general term item in our discussion.

The general approach to measuring and using similarity of educational items is outlined in Figure 2: based on the available data we compute similarity, which can be utilized in many ways. Several sources of data can be used for measuring the similarity:

- an item statement: specification of the item that a learner should solve, e.g., as a natural language description of the task or an input-output specification,
- item solutions: in the case of programming a solution to an item is a program written in a given programming language; we can use a sample solution provided by the item author or solutions submitted by learners,
- data about learners’ performance: for example item solving times, number of attempts needed, or hints taken.

In analyzing and applying similarity it is useful to explicitly distinguish two matrices, which naturally occur in computations:

- a feature matrix, in which rows correspond to items and columns to features of items (e.g., keywords occurring in an item statement or an item solution),
- an item similarity matrix, which is a square matrix $S$, where $S_{ij}$ denotes similarity of items $i$ and $j$.

Figure 2 shows typical steps in the computation and application of similarity. For each step there are many possible choices for their specific realization. For example, the Arrow I (computing a similarity matrix from a feature matrix) can be done using Euclidean distance, Pearson correlation coefficient, cosine similarity, and many other measures. Similarly, there are many specific ways how to transform an item solution into a feature matrix (Arrow B) and many algorithms for performing clustering (Arrow H). Moreover, individual steps are independent and can be combined.

In this work we focus on measuring similarity, i.e., constructing the item similarity matrix. We do not discuss in detail different applications, since it is necessary at first to properly clarify how to compute similarity. Our main contributions are the following. We provide overview and terminology for the problem of “measuring the similarity of programming items” and a systematic mapping of available choices and approaches to the problem. As opposed to related work, which typically utilizes only a single setting, we explore and evaluate different approaches to computing similarity in the context of three different programming environments (Python programming and two robot programming environments). We systematically analyze the role of different choices in the computation in item similarity, utilizing analysis with three levels of abstraction.

**RELATED WORK**

The overall approach outlined is Figure 2 is related to the distinction between pairwise data clustering versus feature vector clustering, which has been studied in the general machine learning research [9, 22].

A specific domain in which item similarities and clusters have been extensively explored are recommender systems, e.g.,
in neighborhood-based methods [6], item-item collaborative filtering [4], and content based techniques [14]. Similarity measures has been used for clustering of items [17, 18] and also for clustering of users [23].

In the domain of educational data mining, previous research explored similarity based on performance data. In [20], authors study similarity of items and focus on comparison of different similarity measures. In [12], authors study similarity and clustering of users and provide detailed description of processing pipelines for computing similarity. Another related line of research in educational data mining is based on the concept of a Q-matrix [24, 2]. A Q-matrix can be seen as a generalization of a clustering; it provides mapping between items and concepts, one item can belong to several concepts. The Q-matrix can be constructed or refined based on the performance data [5].

In the context of programming, previous research have studied similarity of programs for a single programming problem. This has been done in two different settings. At first, in plagiarism detection [13], where the goal is to uncover programs that have been copied (and slightly obfuscated). At second, in the analysis of submissions in massive open online courses, where a single assignment can have a very large number of submissions. The goal of the analysis in this context is to get insight into the learning process or multiply instructor leverage by propagating feedback [19, 16, 25], or to automatically generate hints or examples based on learners’ submissions [21, 11, 8]. These works often use computation of similarity between programs as one of the steps, employing techniques like bag-of-words program representation, analysis of abstract syntax trees, and tree edit distance. We employ these techniques for our analysis.

The most closely related work is by Hosseini et al. [10], who consider specifically the question of similarity of programming items or items and worked out examples, using introductory programming problems concerning the Java language. They, however, use only items of the type “What is the output of a given program?”, whereas we consider more typical programming problems where learners are required to write a program.

**ITEMS IN INTRODUCTORY PROGRAMMING**

Throughout the paper we use the general notation of educational items, since many aspects of our work are generally applicable. Our focus is, nevertheless, on programming problems. To further specify the context of our research, we now describe examples of specific introductory programming environments and programming items. These environments and items are also used in evaluation.

**Programming in Python**

The standard item in introductory programming is to write a program implementing a specified functionality in a general purpose programming language. Examples of such items are “Write a function that outputs divisors of a given number.”, “Write a function that outputs ASCII art chessboard of size N.”, “Write a function that replaces every second letter in a string by X.”, or “Write a function that outputs frequencies of letters in a given text.”.

An item statement in this context is given by a natural language description of the task (as illustrated above), usually with some examples of input-output behavior. An item typically contains also a sample solution, which can be used for automatic evaluation of learners solutions.

For our analysis we consider programming problems in Python, which is a typical language used for introductory programming. We use 28 items from the system tutor.fi.muni.cz, for these items we have data about learner performance (time taken to solve the problem). We
also use 72 items for which we have only the item statement – these items are used in a large university programming class, but without data collection.

**Robot Programming**

A less standard, but very popular approach to teaching basic programming concepts is to use a simplified programming environment to program robots on a grid. Problems of this type are often used in the well-known *Hour of code* activity, with participation of millions of learners.

An item in this context is given by a specific world, which is typically a grid with a robot and some obstacles or enemies, and some restrictions placed on a program, e.g., there is often a limit on the number of commands, so that the problem has to be solved using loops instead of long list of simple commands. Solutions are written in a restricted programming language, which contains elementary commands for a robot (move forward, turn, shoot) and basic control flow commands. The program is often specified using graphical interface, a common choice today is the Blockly interface [7].

For our analysis we use two environments of this type (illustrated in Figure 1). *Robotanist* (available at the web tutor.fi.muni.cz) uses very simple programming commands (arrows for movement, colors for conditions), but the solution of problems is often nontrivial due to limits on the number of commands. Solutions thus require careful decomposition into functions and use of recursion. For this environment we have 74 items, including data on learners’ performance (over 110 thousand problem solving times). *RoboMission* (en.robomise.cz) uses a richer world (e.g., meteorites, worm holes, colors, diamonds) and is programmed in the Blockly interface using a richer set of commands (movement, shooting, several types of conditions, repeat and while loops). For this environment we have 75 items. Data on learners’ performance are available, but are not yet sufficiently large, therefore we use only the item statement and sample solutions for our analysis.

**COMPUTING SIMILARITY**

We structure the discussion of similarity computation into two steps. At first, we cover the basic processing of input data to get a feature matrix or a similarity matrix. At second, we consider transformations of the computed matrices.

In our discussion we use similarity measures (higher values correspond to higher similarity). Related work sometimes considers distance (dissimilarity) measures (lower values correspond to higher similarity). This is just a technical issue, as we can easily transform similarity into dissimilarity by subtraction.

**Processing the Input Data**

In this step we need to get from the raw input data to the matrix form. The details of these steps depend on the type of data and specifics of the used items – the input data may include natural language text, programs written in a programming language, formal description of the robot world, etc.

**Item Statement**

To compute similarity based on an item statement, it is natural to go through the feature matrix (Arrow A). The choice of features depends on the specific type of programming environment.

For the standard programming items where the item is specified using a natural language, the features have to be obtained from this text. A basic technique is to use the bag-of-words model, i.e., representing the text by a vector with the number of occurrences of each word (with standard processing, e.g., lemmatization and omission of stop words). Other features may be derived from the input-output specification, e.g., features describing types of variables (e.g., integer, string, list).

In the case of robot programming, an item is typically specified by a robot world description and a set available commands. Natural language description may be present, but typically does not contain fundamental information. Basic features thus correspond to the aspects of the word and the used programming language, e.g., in the RoboMission setting these are word concepts like diamond, worm hole, meteorite and programming aspects like the limit on the number of commands.

**Item Solution**

Another approach to measuring similarity of items is to utilize solutions, i.e., programming codes that solve an item. The basic approach is to utilize a single solution – either the sample solution provided by the item author, or the most common learner solution. Here we have two natural approaches to computing similarity: via feature matrix or by direct computation of similarities.

With the features approach (Arrow B) we analyze the source code (typically using traversal of the abstract syntax tree) to compute features describing occurrence of programming concepts and keywords like while, if, return, print, or use of operators. The basic approach is again the bag-of-words model, only applied to programming keywords instead of words in a natural language. In this representation we lose information about the structure of the program – we only retain the presence of concepts and the frequency of their occurrence. In addition to features corresponding to keywords, we can use features like the use of functions, the nested depth, or the length of a code. In some settings it may also be possible to use features based on input-output behavior (e.g., type of the input and output).

The second approach is to compute directly item similarity matrix (Arrow C) by computing edit distance between the selected solutions for the two items. The edit distance can be computed in several ways:

- tree edit distance [3] for the abstract syntax tree, potentially with some specific modifications for programs (in the specific programming language),

- the basic Levenshtein edit distance for the canonized code, which is applicable particularly for the robot programming exercises, where programs can be relatively easily canonized.
We can, however, compute similarity directly from the per-
we can process them using a number of transformations. In
with respect to a specific performance measure (the correlation
The basic feature matrix obtained by data processing contains
These data can be transformed into features (Arrow D) like
The suitable choice of a similarity measure depends also on
Examples of simple transformations are binarization (very
coarse grained normalization), normalization by dividing by
a maximal value for each feature to get values into the [0, 1]
interval, or log transform (to limit the influence of outlier
values). A typical transformation, particularly in the context of
the bag-of-words features, is the TF-IDF (term frequency-
itself document frequency) transformation.

Often we can obtain several feature matrices (or item similarity
matrices) corresponding to different data sources or multiple
solutions. We can combine these matrices in different ways,
the basic ones being: average (assuming additive influence of
data sources), min (assuming conjunctive influence of data
sources), max (assuming disjunctive influence of data sources).

Computing Similarity
When we compute the similarity matrix based on the feature
matrix (Arrow I) or on its projection into $R^m$ (Arrow M), we
have a vector of real values for each item; the similarity of a
tuple of items is computed as the similarity of their vectors.
This is a common operation in machine learning, with many
choices available. The common choices are cosine similarity,
Pearson correlation coefficient, and Euclidean distance
(transformed into similarity measure by subtraction). These
measures are used widely in recommender systems, with the
experience that the choice of suitable measure depends on a
particular data set [6].

The suitable choice of a similarity measure depends also on the
steps used to compute the feature matrix and on the purpose
of computing similarity. As an example, consider two
programming problems, where solutions use the same
keywords (keywords), but one of the solutions is longer and uses
the keywords multiple times. If we use normalization, the
feature vectors will be (nearly) the same and the items
will end up as very similar for any similarity measure. If we do
not use normalization, the items will end up as very similar
when we use cosine similarity and correlation coefficient, but
as different when we use Euclidean distance. We cannot give
a simple verdict, which one of these is better, since this may
depend on the intended application.

Projections
From feature matrix or item similarity matrix we can compute
projection to $R^d$ (Arrow G and Arrow L). Such projection is
typically used for application, particularly for visualization
of items. It can, however, also be a useful processing step
in the computation of item similarities, for example in the
case of correlated features we can use the principal compo-
nent analysis (PCA) for decorrelating features (Arrow G) and
then compute similarities based on the principal components
(Arrow M).

There are many techniques for computing low dimensional
projections, for feature matrix (Arrow G) the popular choices
include the basic linear PCA and the nonlinear t-SNE [15],
for similarity data (Arrow L) the basic technique is the (non-
metric) multidimensional scaling.
**EVALUATION**

As the previous section shows, there is a wide number of techniques that can be used for computation of similarity. Moreover, individual steps can be combined in many ways. What is a good approach to computing similarity? Which decisions matter?

Evaluation of similarity measures is difficult, because there is no clear criterion of quality of measures. The suitability of measure depends on a particular way it is used in a specific application. However, it is very useful to get an insight into similarity measures in application independent way. To this end we analyze similarity measures at several levels of abstraction:

1. **Similarity of items for a specific similarity measure.** This allows us to get the basic understanding of what kind of output we can obtain.

2. **Agreement of different measures (across all items).** This allows us to get understanding how much do the choices made in the computation matter.

3. **Analysis of different agreement measures.** To measure agreement between similarity measures we must also choose some method of quantification (Arrow $K$). There are several natural candidates. Does it matter, which one we choose?

Finally, as an illustration of an application specific evaluation, we consider evaluation of measures with respect to clustering of items.

We perform our analysis across different contexts – different programming environments and sets of items. We use the settings described in Section 3, i.e., Python, Robotanist, RoboMission. This gives us an insight into how the observed results generalize.

**Similarity of Items for a Specific Measure**

We start with the basic kind of analysis – exploration of results obtained using a specific similarity measure; i.e., we pick a specific way to compute item similarity matrix and then explore the matrix, its visualization and projection.

Figure 3 shows two similarity matrices for 72 Python programming problems. The matrix based on sample problem solutions is dense – many keywords (e.g., `print`, `for`) are shared by many items. The matrix based on item statements is sparse – in this case we are using very brief item statements (typically one sentence), and thus items share words only with several other items.

Figure 4 shows a projection into a plane of a feature matrix for items from RoboMission. Features are based on both item statement and sample solution (bag-of-words), with log and IDF transformation, and divided by the maximum value. Because statement features have significantly higher counts, these transformations are important in order for the projection to be influenced by both the statement and the solution. Without these transformations, items from different levels end up noticeably more mixed up in the projection.

The usefulness of measures based on the performance data clearly depends on the size of available data – we need sufficiently large data so that the measures are stable. As a basic check of stability we split the performance data into two independent halves, compute the measure for each half, and then check their agreement. We performed this evaluation for our Python programming data and the Robotanist problem, where we have problem solving times available. The resulting correlation is 0.54 (27 Python problems) and 0.28 (74 Robotanist problems) – high enough to conclude that there is a significant underlying signal in the performance data (and not just a random noise), but clearly the size of data is not yet sufficiently large to provide stable similarity measure for practical applications. We experimented with restricting the data to only items which were solved by large number of learners. When we use items with at least 400 solutions, the measures are getting stable (correlation over 0.8 in both cases), but we have data of this size only for about one half of our items.

**Agreement between Measures**

Our main goals in this paper are related to this level of analysis – dealing with questions like “What is the relation between dif-
different similarity measures?” and “Which steps in the pipeline are most important?”.

To analyze agreement between two similarity measures, we first compute the item similarity matrix for of each of them (obtaining two matrices of the type displayed in Figure 3) and then compute the agreement as a correlation of values in these two similarity matrices. For a set of similarity measures, this gives us a matrix of agreement values, as illustrated in Figure 5 and Figure 6. These figures are for the RoboMission environment, but they illustrate trends that we see across all our data sets.

Similarity measures based on item statement vs. solution are only weakly related; they focus on different aspects of items and their similarity (see Figure 5). However, the relationship can be stronger, if the item statements include more details or constraints about the solution, such as a set of allowed programming blocks that the learners can use to build their solution.

Avoid one source of data being far more important than the other. This issue can be seen in Figure 5 – without IDF normalization, the measures that use all features are correlated to those that use item statement, but not to those that use the solution.

Figure 6 shows relations between measures that utilize different types of solutions. Here we use data on Python programming, where learners solutions are available, and compare measures of similarity based on the sample solution (provided by the author of the item), the top most common learners’ solutions, and the averages of several top solutions. The measures based on sample solution and top learner solution have high overall correlation, but for individual items they may differ significantly – in some cases the sample solution and top learner solution may be very different as even simple programming problems like computing factorial can be written in widely different ways: using for loop, while loop, or recursion. When data on learner solutions are available, using the average of the 3 most common solutions seems to be good, robust approach.

For the Robotanist and Python programming, where we have data on learners’ performance, the correlation between measures based on solution and measures based on performance is between 0.2 and 0.4. This is a weak agreement, but since the measures based on performance are not yet stable, even this weak agreement may indicate a relationship between these different approaches to measuring similarity. This relationship needs to be explored for larger data sets.

**How to Measure Agreement?**

In the previous analysis we used simple correlation to measure agreement, i.e., to quantify agreement of two similarity matrices, we flatten them into vectors and then compute Pearson’s correlation coefficient over these vectors. But there are other choices to measuring agreement. Particularly in applications, where the intended use of similarity measures is to pick the closest neighbors (e.g., recommendation of similar exercises),
it may be more relevant to measure the agreement of rankings or agreement on top $N$ positions.

Do the results presented in the previous section depend on our choice of the approach to measuring agreement? To explore this question we went with our analysis up one level of abstraction. Now we analyze the relationship between different measures of agreement of similarity measures. Specifically, we compare measures of agreement based on correlation of flatten matrices and measures of agreement based on top $N$ positions. When measuring agreement of two similarity matrices $S_1$ and $S_2$ with respect to top $N$ positions, we use the following approach: for each item we find $N$ most similar items with respect to $S_1$ and $S_2$; we compute the size of intersection of these two sets; finally, we average over all items and normalize by $N$.

Evaluation works in this way: we pick several similarity measures, for each of them we compute similarity matrix (as in Figure 3); then for each measure of agreement we compute the agreement matrix of all the chosen similarity measures (as in Figure 5); finally, we compare these agreement matrices. Example of this analysis is in Figure 8. There is some difference between using correlation and “Top 5” measure of agreement, but this difference should not have large impact on conclusions about the choice of similarity measures. Note that for this analysis we use the basic correlation, which is again an ad hoc choice, but for now we have decided to stop our analysis here and not to pursue other levels of abstraction.

**Impact on Measure Application**

Our focus in this paper is on evaluation of different similarity measures in a general scenario. However, the evaluation can also target on a specific application for the similarity measure. In this section, we present an example of such analysis.

In the production system, items in RoboMission are divided into 9 levels, which were specified manually by the system developers. We examine how well we are able to reconstruct this labeling using different similarity measures. For each similarity measure, we compute the similarity matrix and then use k-means clustering for this matrix with $k$ set to 9 (the number of levels). The obtained clusters are compared with the manual labeling using the Rand Index.

The results (averaged over 10 runs) are shown in Table 1. As the manually created levels differ mainly by used programming concepts, such as loops and conditionals, it helps to multiply solution features to give them higher weight. However, if the item statements were more important for the division into levels, then the statement features should have the higher weights instead. The weights can be even learned to optimize an objective function for given application, provided there is enough data to avoid overfitting.

**Table 1. Agreement between manual labeling and clusterings obtained by k-means algorithm for similarity matrices for different similarity measures. Transformations used with bag-of-words features: log, dividing by maximum value, multiplying by IDF, multiplying all solution features by the factor of 5.**

<table>
<thead>
<tr>
<th>Similarity Measure</th>
<th>Rand Index</th>
</tr>
</thead>
<tbody>
<tr>
<td>Bag / log+max+idf+weights / correlation</td>
<td>0.49</td>
</tr>
<tr>
<td>Bag / log+max+idf+weights / euclidean</td>
<td>0.39</td>
</tr>
<tr>
<td>TED</td>
<td>0.30</td>
</tr>
<tr>
<td>Bag / log+max+idf / euclidean</td>
<td>0.29</td>
</tr>
<tr>
<td>Bag / bin / euclidean</td>
<td>0.28</td>
</tr>
<tr>
<td>Bag / log+max / euclidean</td>
<td>0.28</td>
</tr>
<tr>
<td>Bag / bin / correlation</td>
<td>0.27</td>
</tr>
<tr>
<td>Levenshtein</td>
<td>0.26</td>
</tr>
<tr>
<td>Bag / log+max+idf / correlation</td>
<td>0.26</td>
</tr>
<tr>
<td>Bag / log+max / correlation</td>
<td>0.22</td>
</tr>
<tr>
<td>Bag / log / euclidean</td>
<td>0.18</td>
</tr>
<tr>
<td>Bag / log / correlation</td>
<td>0.14</td>
</tr>
<tr>
<td>Bag / no transformation / euclidean</td>
<td>0.11</td>
</tr>
<tr>
<td>Bag / no transformation / correlation</td>
<td>0.09</td>
</tr>
</tbody>
</table>

**DISCUSSION**

We propose a systematic approach to defining and analyzing item similarity. We discuss the issue specifically in the context of introductory programming, but the approach is general and can be applied also for other complex items, e.g., in mathematics of physics.
**Systematic Approach to Similarity Measures**

Measuring similarity of items is a complex problem, because it can be tackled in many ways (particularly for complex items like programming problems) and it is hard to evaluate the quality of measures. We propose a systematic approach to studying similarity measures (outlined in Figure 2), which makes explicit the many choices that we need to make to specify a similarity measure.

We also propose a systematic approach to analyzing similarity measures. Without going into details of specific application, we cannot objectively compare measures. However, it is not reasonable to do the evaluation only with respect to the final application. Consider for example the use of similarity measures in recommendation of items in an learning system. Evaluating the quality of recommendations is a complex task even if we compare just a single version of the recommendation algorithm to a control group. It is not feasible to evaluate variants of the recommendation algorithm for many similarity measures.

We thus need to analyze similarity measures even without considering specifics of a particular application. Such evaluation cannot give us verdicts about which measures are good or bad. But we can evaluate which decisions in the similarity computations are really important – which computation pipelines lead to different results. In this way we can narrow the number of measures that need to be explored for a particular application from hundreds to few cases.

We propose to perform the evaluation on several levels of abstraction. All these evaluations lead to results in the form of a matrix (visualized in the form of heatmap in our figures). The interpretation of these matrices, however, differs:

1. At the first level, we analyze the similarity of items with respect to specific measure (Figure 3).
2. At the second level, we analyze agreement between different similarity measures (Figure 5). Each cell of the matrix is now computed by comparing two similarity matrices from the first level of analysis.
3. At the third level, we analyze the impact of agreement measure (Figure 8). Each cell of the matrix now corresponds to comparison of two agreement matrices from the second level of analysis.

**Recommendations for Similarity Computation**

The suitable choice of a similarity measure depends, of course, on a particular setting (programming environment, characteristics of available input data) and the particular application of the measure. However, it is useful to have a basic default choice which can serve as a baseline, which can be further improved.

Based on our explorations, we propose to use the following steps to compute such a default similarity measure:

1. Use item solutions as input data.
2. Compute feature matrix based on the data using the basic bag-of-words approach – computing number of occurrences of natural programming keywords.
3. Normalize the feature matrix, specifically using some variant of the TF-IDF transformation.

The aspect that can most importantly change the results of the computation is the first step – the choice of input data. We believe that item solutions are good default, because for introductory programming problems they are basically always available and the basic bag-of-word analysis can be easily performed in different settings. For performance data to be useful, it is necessary to collect large data on learner behavior, which limits their applicability. The form of item statement data can depend on particular application (e.g., it differs significantly between our robot programming problems and Python programming problems), which makes its use more application specific.

**Limitations and Future Work**

A strong and unique aspect of our work is that we performed our exploration in three different programming environments, which forced us to approach the computation of similarity measures in a general way and allowed us to check generality of the results. A limitation is the size of used item sets – with respect to real life applications these are still limited. For each environment we used between 25 and 75 items. For realistic applications of similarity measures in adaptive systems, a larger item set would be needed. Although we believe that the larger item set should not significantly change the results, it would be useful to explore similarity measures over large data sets.

We provide analysis of similarity measures mostly in application independent way. As argued above, we believe that this is a necessary step. Based on the results of the current analysis, it would be useful to analyze selected similarity measures with respect to specific applications. Specific question that requires attention is that whether different applications require different similarity measures, or whether we can use one reasonably general similarity measure.

In the current work we discuss only flat features – each feature is treated independently from others and all are treated on the same level. In programming, however, features are typically interconnected and can be naturally expressed using taxonomy or ontology. For example, we can have a feature “binary operator” with subfeatures addition, multiplication, division, etc.

In the processing of item statements we may want to distinguish superficial similarity (related to the story or general topic of an item) and intrinsic similarity (related to the way an item is solved). The basic bag-of-word model that we discussed for processing item statements would not be able to distinguish between these. For example in mathematics, word problems typically contain significant story aspect and the basic use of bag-of-word model would lead to dominance of the superficial similarity based on the story. In the programming problems that we used the story aspects is not used, but in another programming settings it may be more relevant. The superficial
similarities may also be useful for applications (e.g., we may want to present the learner a sequence of problems with a similar story), but it should be treated separately from the intrinsic similarity.

REFERENCES

7. Neil Fraser. 2015. Ten things we’ve learned from Blockly. In Blocks and Beyond Workshop (Blocks and Beyond), 2015 IEEE. IEEE, 49–50.