## 2014 - Exercises XI.

1. Decrypt the following cryptotext.

2. Read carefully the following comics. The image can be downloaded here

3. Consider the following generalized Dining Cryptographers protocol for $n$ players $P_{1}, P_{2}, \ldots, P_{n}$ and messages of length $n$ :
Suppose that each pair of players $\left(P_{i}, P_{j}\right)$ shares a set of keys $k_{i, j}(\omega)$ for $i, j, w \in\{1,2, \ldots, n\}$, where $k_{i, j}(\omega)=k_{j, i}(\omega)$ and $k_{i, i}(\omega)=0$. Each player $P_{i}$ computes a vector of values:

$$
W_{i}=\left\{W_{i}(1)=\oplus_{j=1}^{n} k_{i, j}(1), W_{i}(2)=\oplus_{j=1}^{n} k_{i, j}(2), \ldots, W_{i}(n)=\oplus_{j=1}^{n} k_{i, j}(n)\right\}
$$

When broadcasting the messages, every player $P_{i}$ chooses a random position $c_{i}$, applies XOR to her message $m_{i}$ and $W_{i}\left(c_{i}\right)$ to obtain a new vector

$$
V_{i}=\left\{W_{i}(1), W_{i}(2), \ldots, m_{i} \oplus W_{i}\left(c_{i}\right), \ldots, W_{i}(n)\right\}
$$

and makes this vector public.
(a) Show that if every $c_{i}$ is unique then the vector $V=\oplus_{i=1}^{n} V_{i}$ contains all the messages posted by all players.
(b) What happens if two players choose the same position, $i e . c_{j}=c_{i}$ for two players $P_{i}$ and $P_{j}$.
(c) What happens when a dishonest player sets the vector $V_{i}$ to a random vector.
4. Think hard, each exercise needs deliberation.

