Controllable-Choice Message Sequence Graphs

Martin Chmelík^{1,*} and Vojtěch Řehák^{2,**}

¹ Institute of Science and Technology Austria (IST Austria), Klosterneuburg, Austria martin.chmelik@ist.ac.at

> ² Faculty of Informatics Masaryk University, Brno, Czech Republic rehak@fi.muni.cz

Abstract. We focus on the realizability problem of Message Sequence Graphs (MSG), i.e. the problem whether a given MSG specification is correctly distributable among parallel components communicating via messages. This fundamental problem of MSG is known to be undecidable. We introduce a well motivated restricted class of MSG, so called controllable-choice MSG, and show that all its models are realizable and moreover it is decidable whether a given MSG model is a member of this class. In more detail, this class of MSG specifications admits a deadlockfree realization by overloading existing messages with additional bounded control data. We also show that the presented class is the largest known subclass of MSG that allows for deadlock-free realization.

1 Introduction

Message Sequence Chart (MSC) [16] is a popular formalism for specification of distributed systems behaviors (e.g. communication protocols or multi-process systems). Its simplicity and intuitiveness come from the fact that an MSC describes only exchange of messages between system components, while other aspects of the system (e.g. content of the messages and internal computation steps) are abstracted away. The formalism consists of two types of charts: (1) basic Message Sequence Charts (bMSC) that are suitable for designing finite communication patterns and (2) High-level Message Sequence Charts (HMSC) combining bMSC patterns into more complex designs. In this paper, we focus on the further type reformulated as Message Sequence Graphs (MSG) that has the same expressive power as HMSC but a simpler structure, and hence it is often used in theoretical computer science papers, see, e.g. [2,4,6,14,23].

Even such incomplete models as MSG can indicate serious errors in the designed system. The errors can cause problems during implementation or even make it impossible. Concerning verification of MSC models, researchers have studied a presence of a race condition in an MSC [3,7,11,23], boundedness of

^{*} The author was supported by Austrian Science Fund (FWF) Grant No P 23499-N23 on Modern Graph Algorithmic Techniques in Formal Verification, FWF NFN Grant No S11407-N23 (RiSE), ERC Start grant (279307: Graph Games), and Microsoft faculty fellows award.

^{**} The author is supported by the Czech Science Foundation, grant No. P202/12/G061.

A. Kučera et al. (Eds.): MEMICS 2012, LNCS 7721, pp. 118–130, 2013.

[©] Springer-Verlag Berlin Heidelberg 2013

the message channels [4], the possibility to reach a non-local branching node [6,20,14,17,18,12,21], deadlocks, livelocks, and many more. For a recent overview of current results see, e.g. [10].

In this paper, we focus on the realizability problem of MSG specifications, i.e. implementation of the specification among parallel machines communicating via messages. This problem has been studied in various settings reflecting parameters of the parallel machines, the environment providing message exchanges as well as the type of equivalence considered between the MSG specification and its implementation. Some authors restricted the communication to synchronous handshake [14,13], needed several initial states in the synthesized machines [5], or considered language equivalence with global accepting states in the implementation (the implementation accepts if the components are in specific combinations of its states) [22]. From our point of view, the crucial aspect is the attitude to non-accepted executions of the implementation. When language equivalence is taken into account, an intentional deadlock can prevent a badly evolving execution from being accepted [14]. In our setting every partial execution can be extended into an accepting one. Therefore, we focus on a deadlock-free implementation of a given MSG into Communicating Finite-State Machines (CFM) with FIFO communicating channels and distributed acceptance condition, i.e. a CFM accepts if each machine is in an accepting state. In [19], it has been shown that existence of a CFM realizing a given MSG without deadlocks is undecidable. When restricted to *bounded* MSG (aka regular MSG, i.e. communicating via finite/bounded channels, and so generating a regular language), the problem is EXPSPACE-complete [19].

In later work [14,5], a finite data extension of messages was considered when realizing MSG. This is a very natural concept because message labels in MSG are understood as message types abstracting away from the full message content. Hence, during implementation, the message content can be refined with additional (finite) data that helps to control the computation of the CFM in order to achieve the communication sequences as specified in the given MSG. The main obstacle when realizing MSG are nodes with multiple outgoing edges choice nodes. In a CFM realization, it is necessary to ensure that all Finite-State Machines choose the same successor of each choice node. This can be hard to achieve as the system is distributed.

In [14], a class of so called *local-choice* MSG [18,6] was shown to include only MSG realizable in the above mentioned setting. Local-choice specifications have the communication after each choice node initiated by a single process — the choice leader. Intuitively, whenever a local-choice node is reached, the choice leader machine attaches to all its outgoing messages the information about the chosen node. The other machines pass the information on. This construction is sufficient to obtain a deadlock-free realization, for details see [14]. Another possible realization of local-choice MSG is presented in [17]. Due to [12], it is also decidable to determine whether a given MSG is language equivalent to some local-choice MSG and, moreover, each equivalent MSG can be algorithmically realized by a CFM. To the best of our knowledge, this is the largest class of deadlock-free realizable specifications in the standard setting, i.e. with additional data, FIFO channels, and local accepting states.

In this paper, we introduce a new class of *controllable-choice* MSG that extends this large class of realizable MSG. The crucial idea of controllable-choice MSG is that even some non-local-choice nodes can be implemented, if the processes initiating the communication after the choice can agree on the successor node in advance. This is achieved by exchanging bounded additional content in existing messages. We call choice nodes where such an agreement is possible *controllable-choice* nodes, and show that the class of MSG with these nodes is more expressive than the class of MSG that are language equivalent to localchoice MSG.

2 Preliminaries

In this section, we introduce the Message Sequence Chart (MSC) formalism that was standardized by the International Telecommunications Union (ITU-T) as Recommendation Z.120 [16]. It is used to model interactions among parallel components in a distributed environment. First, we introduce the basic MSC.

Basic Message Sequence Charts (bMSC). Intuitively, a bMSC identifies a single finite execution of a message passing system. Processes are denoted as vertical lines — instances. Message exchange is represented by an arrow from the sending process to the receiving process. Every process identifies a sequence of actions — sends and receives — that are to be executed in the order from the top of the diagram. The communication among the instances is not synchronous and can take arbitrarily long time.

Definition 1. A basic Message Sequence Chart (bMSC) M is defined by a tuple $(E, <, \mathcal{P}, \mathcal{T}, P, \mathcal{M}, l)$ where:

- E is a finite set of events,
- < is a partial ordering on E called visual order,
- \mathcal{P} is a finite set of processes,
- $-\mathcal{T}: E \rightarrow \{\text{send}, \text{receive}\}\$ is a function dividing events into sends and receives,
- $-P: E \rightarrow \mathcal{P}$ is a mapping that associates each event with a process,
- $-\mathcal{M}: \mathcal{T}^{-1}(\text{send}) \to \mathcal{T}^{-1}(\text{receive})$ is a bijective mapping, relating every send with a unique receive, such that a process cannot send a message to itself, we refer to a pair of events $(e, \mathcal{M}(e))$ as a message, and
- l is a function associating with every message (e, f) a label m from a finite set of message labels C, i.e. l(e, f) = m.

Visual order < is defined as the reflexive and transitive closure of $\mathcal{M} \cup \bigcup_{p \in \mathcal{P}} <_p$ where $<_p$ is a total order on $P^{-1}(p)$.

We require the bMSC to be *first-in-first-out (FIFO)*, i.e., the visual order satisfies for all messages (e, f), (e', f') and processes p, p' the following condition

$$e <_p e' \land P(f) = P(f') = p' \Rightarrow f <_{p'} f'.$$

Every event of a bMSC can be represented by a letter from an alphabet

$$\Sigma = \{p!q(m) \mid p, q \in \mathcal{P}, m \in \mathcal{C}\} \cup \{q?p(m) \mid p, q \in \mathcal{P}, m \in \mathcal{C}\}.$$

Intuitively, p!q(m) denotes a send event of a message with a label m from a process p to a process q, and q?p(m) represents a receive event of a message with a label m by q from a process p. We define a linearization as a word over Σ representing a total order of events that is consistent with the partial order <. For a given bMSC M, a language $\mathcal{L}(M)$ is the set of all linearizations of M.

Message Sequence Graphs. It turns out that specifying finite communication patterns is not sufficient for modelling complex systems. Message Sequence Graphs allow us to combine bMSCs into more complex systems using alternation and iteration. An MSG is a directed graph with nodes labeled by bMSCs and two special nodes, the initial and the terminal node. Applying the concept of finite automata [15], the graph represents a set of paths from the initial node to the terminal node. In MSG, every such a path identifies a sequence of bMSCs. As every finite sequence of bMSCs can be composed into a single bMSC, an MSG serves as a finite representation of an (infinite) set of bMSCs.

Definition 2. A Message Sequence Graph (MSG) is defined by a tuple G = $(\mathcal{S}, \tau, s_0, s_f, L)$, where \mathcal{S} is a finite set of states, $\tau \subset \mathcal{S} \times \mathcal{S}$ is an edge relation. $s_0 \in \mathcal{S}$ is the initial state, $s_f \in \mathcal{S}$ is the terminal state, and $L: \mathcal{S} \to \text{bMSC}$ is a labeling function.

W.l.o.g., we assume that there is no incoming edge to s_0 and no outgoing edge from s_f . Moreover, we assume that there are no nodes unreachable from the initial node and the terminal node is reachable from every node in the graph.

Given an MSG $G = (S, \tau, s_0, s_f, L)$, a path is a finite sequence of states $s_1 s_2 \dots s_k$, where $\forall 1 \leq i < k : (s_i, s_{i+1}) \in \tau$. A run is defined as a path with $s_1 = s_0$ and $s_k = s_f$.

Intuitively, two bMSCs can be composed to a single bMSC by appending events of every process from the latter bMSC at the end of the process from the precedent bMSC. Formally, the sequential composition of two bMSCs $M_1 =$ $(E_1, <_1, \mathcal{P}, \mathcal{T}_1, P_1, \mathcal{M}_1, l_1)$ and $M_2 = (E_2, <_2, \mathcal{P}, \mathcal{T}_2, P_2, \mathcal{M}_2, l_2)$ such that the sets E_1 and E_2 are disjoint (we can always rename events so that the sets become disjoint), is the bMSC $M_1 \cdot M_2 = (E_1 \cup E_2, <, \mathcal{P}, \mathcal{T}_1 \cup \mathcal{T}_2, P_1 \cup P_2, \mathcal{M}_1 \cup \mathcal{M}_2, l_1 \cup l_2),$ where < is a transitive closure of $<_1 \cup <_2 \cup \bigcup_{p \in \mathcal{P}} (P_1^{-1}(p) \times P_2^{-1}(p))$. Note that we consider the weak concatenation, i.e. the events from the latter bMSC may be executed even before some events from the precedent bMSC.

Now, we extend the MSG labeling function L to paths. Let $\sigma = s_1 s_2 \dots s_n$ be a path in MSG G, then $L(\sigma) = L(s_1) \cdot L(s_2) \cdot \ldots \cdot L(s_n)$. For a given MSG G, the language $\mathcal{L}(G)$ is defined as $\bigcup_{\sigma \text{ is a run in } G} \mathcal{L}(L(\sigma))$. Hence, two MSG are said to be language-equivalent if and only if they have the same languages.

Communicating Finite-State Machines. A natural formalism for implementing bMSCs are Communicating Finite–State Machines (CFM) that are used for example in [3,1,14]. The CFM consists of a finite number of finite-state machines that communicate with each other by passing messages via unbounded FIFO channels.

Definition 3. Given a finite set \mathcal{P} of processes and a finite set of message labels \mathcal{C} , the Communicating Finite-State Machine (CFM) \mathcal{A} consists of Finite-State Machines (FSMs) $(\mathcal{A}_p)_{p\in\mathcal{P}}$. Every \mathcal{A}_p is a tuple $(\mathcal{S}_p, \mathcal{A}_p, \rightarrow_p, s_p, F_p)$, where: $-\mathcal{S}_p$ is a finite set of states,

 $\begin{aligned} -A_p &\subseteq \{p!q(m) \mid q \in \mathcal{P}, m \in \mathcal{C}\} \cup \{p?q(m) \mid q \in \mathcal{P}, m \in \mathcal{C}\} \text{ is a set of actions,} \\ - &\rightarrow_p \subseteq \mathcal{S}_p \times A_p \times \mathcal{S}_p \text{ is a transition relation,} \end{aligned}$

- $-s_p \in \mathcal{S}_p$ is the initial state, and
- $-\hat{F}_p \subseteq \hat{S}_p$ is a set of local accepting states.

We associate an unbounded FIFO error-free channel $\mathcal{B}_{p,q}$ with each pair of FSMs $\mathcal{A}_p, \mathcal{A}_q$. In every configuration, the content of the channel is a finite word over the label alphabet \mathcal{C} .

Whenever an FSM \mathcal{A}_p wants to send a message with a label $m \in \mathcal{C}$ to \mathcal{A}_q , it enqueues the label m into channel $\mathcal{B}_{p,q}$. We denote this action by p!q(m). Provided there is a message with a label m in the head of channel $\mathcal{B}_{p,q}$, the FSM \mathcal{A}_q can receive and dequeue the message with the label m. This action is represented by q!p(m). A configuration of a CFM $\mathcal{A} = (\mathcal{A}_p)_{p\in\mathcal{P}}$ is a tuple C = (s, B), where $s \in \prod_{p\in\mathcal{P}}(\mathcal{S}_p)$ and $B \in (\mathcal{C}^*)^{\mathcal{P}\times\mathcal{P}}$ — local states of the FSMs together with the contents of the channels. Whenever there is a configuration transition $C_i \xrightarrow{a_i} C_{i+1}$, there exists a process $p \in \mathcal{P}$ such that the FSM \mathcal{A}_p changes its local state by executing action $a_i \in \mathcal{A}_p$ and modifies the content of one of the channels.

The CFM execution starts in an *initial configuration* $s_0 = \prod_{p \in \mathcal{P}} \{s_p\}$ with all the channels empty. The CFM is in an *accepting configuration*, if every FSM is in some of its final states and all the channels are empty. We will say that a configuration is a *deadlock*, if no accepting configuration is reachable from it. A CFM is *deadlock-free* if no deadlock configuration is reachable from the initial configuration. An *accepting execution* of a CFM \mathcal{A} is a finite sequence of configurations $C_1 \xrightarrow{a_1} C_2 \xrightarrow{a_2} \ldots \xrightarrow{a_{n-1}} C_n$ such that C_1 is the initial configuration and C_n is an accepting configuration. The word $a_1a_2 \cdots a_{n-1}$ is then an *accepted word* of \mathcal{A} . Given a CFM \mathcal{A} , the *language* $\mathcal{L}(\mathcal{A})$ is defined as the set of all accepted words of \mathcal{A} .

3 Controllable-Choice Message Sequence Graphs

For a given MSG we try to construct a CFM such that every execution specified in the MSG specification can be executed by the CFM and the CFM does not introduce any additional unspecified execution.

Definition 4 ([1]). An MSG G is realizable iff there exists a deadlock-free CFM \mathcal{A} such that $\mathcal{L}(G) = \mathcal{L}(\mathcal{A})$.

One of the most natural realizations are projections. A projection of a bMSC M on a process p, denoted by $M|_p$, is the sequence of events that are to be executed by the process p in M. For every process $p \in \mathcal{P}$, we construct a FSM \mathcal{A}_p that accepts a single word $M|_p$. This construction is surprisingly powerful and models all of the bMSC linearizations.

Proposition 1. Let M be a bMSC, then CFM $\mathcal{A} = (M|_p)_{p \in \mathcal{P}}$ is a realization, *i.e.* $\mathcal{L}(M) = \mathcal{L}(\mathcal{A})$.

It turns out that the main obstacle when realizing MSG are nodes with multiple outgoing edges — choice nodes. It is necessary to ensure that all FSMs choose the same run through the MSG graph. This can be hard to achieve as the system is distributed.

In what follows, we present a known class of local-choice MSG specifications that admits a deadlock-free realization by adding control data into the messages. Then, we define a new class of *controllable-choice* MSG and compare the expressive power of the presented classes.

Local-Choice MSG. is a Class Studied by Many Authors [6,20,14,17,18,12]. Let M be a bMSC, we say that a process $p \in \mathcal{P}$ initiates the bMSC M if there exists an event e in M, such that P(e) = p and there is no other event e' in bMSC M such that e' < e. For a given MSG, every node $s \in \mathcal{S}$ identifies a set triggers(s), the set of processes initiating the communication after the node s. Note that it may not be sufficient to check only the direct successor nodes in the MSG.

Definition 5. Let $G = (S, \tau, s_0, s_f, L)$ be an MSG. For a node $s \in S$, the set triggers(s) contains process p if and only if there exists a path $\sigma = \sigma_1 \sigma_2 \dots \sigma_n$ in G such that $(s, \sigma_1) \in \tau$ and p initiates bMSC $L(\sigma)$.

Definition 6. A choice node u is a local-choice node iff triggers(u) is a singleton. An MSG specification G is local-choice iff every choice node of G is local-choice.

Local-choice MSG specifications have the communication after every choice node initiated by a single process — the choice leader. In [14] a deadlock-free realization with additional data in messages is proposed. It is easy to see that every MSG specification G is deadlock-free realizable if there is a local-choice MSG G' such that $\mathcal{L}(G) = \mathcal{L}(G')$. Note that the equivalence can be algorithmically checked due to [12].

Controllable Specifications. The difficulties when realizing MSG are introduced by choice nodes. In local-choice MSG, the additional message content is used to ensure a single run through the graph is executed by all FSMs. In case of controllable-choice MSG, the additional content serves the same purpose but besides informing about the node the FSMs are currently executing the FSMs also attach a prediction about its future execution. This allows us to relax the restriction on choice nodes and allows certain nonlocal choice nodes to be present in the specification. However, it is necessary to be able to resolve every occurrence of the choice node, i.e. make the decision in advance and inform all relevant processes.

Definition 7. Let $M = (E, <, \mathcal{P}, \mathcal{T}, P, \mathcal{M}, l)$ be a bMSC and $P' \subseteq \mathcal{P}$ be a subset of processes. A send event $e \in E$ is a resolving event for P' iff

$$\forall p \in P' \; \exists e_p \in P^{-1}(p) \; such \; that \; e < e_p.$$

Intuitively, resolving events of M for P' can distribute information to all processes of P' while executing the rest of M, provided that other processes are forwarding the information.

Definition 8. Let $G = (S, \tau, s_0, s_f, L)$ be an MSG. A choice node u is said to be controllable-choice iff it satisfies both of the following conditions:

- For every path σ from s_0 to u there exists a resolving event in bMSC $L(\sigma)$ for triggers(u).
- For every path $\sigma = s_1 s_2 \dots u$ such that $(u, s_1) \in \tau$, there exists a resolving event in bMSC $L(\sigma)$ for triggers(u).

Intuitively, a choice node is controllable-choice, if every path from the initial node is labeled by a bMSC with a resolving event for all events initiating the communication after branching. Moreover, as it is necessary to attach only bounded information, the same restriction is required to hold for all cycles containing a controllable-choice node. In [9] we propose an algorithm that determines whether a given choice node is a controllable-choice node.

Definition 9. An MSG specification G is controllable-choice iff every choice node is either local-choice or controllable.

Note that there is no bound on the distance between the resolving event and the choice node it is resolving.

Local-Choice vs. Controllable-Choice MSG. In the following, we show that the controllable-choice MSG are more expressive than local-choice MSG. It is easy to see that every local-choice MSG is also a controllable-choice MSG and that not every controllable-choice MSG is local-choice. In the following theorem, we strengthen the result by stating that the class of MSG that are language equivalent to some controllable-choice MSG is more expressive than the class of MSG that are language-equivalent to some local-choice MSG.

Theorem 1. The class of MSG that are language-equivalent to some localchoice MSG, forms a proper subset of MSG that are language-equivalent to some controllable-choice MSG.

Proof. Consider a MSG $G = (S, \tau, s_0, s_f, L)$ with three nodes s_0, s_f and s, such that $(s_0, s), (s, s), (s, s_f) \in \tau$ and the only non–empty bMSC is L(s) with two

processes p, q. The projection of events on p is p!q(m), p?q(m') and similarly for q the projection is q!p(m'), q?p(m). Note that the only choice node s is controllable as both send events are resolving events for both of the processes.

The MSG G violates a necessary condition to be language equivalent to a local-choice specification. Intuitively, the condition states that its language must be a subset of a language of a generic local-choice equivalent MSG (for more details see [12]).

4 Realizability of Controllable-Choice MSG

In this section we present an algorithm for realization of controllable-choice MSG. The class of local-choice specifications admits a natural deadlock-free realization because every branching is controlled by a single process.

As the *triggers* set for controllable-choice nodes can contain multiple processes, we need to ensure that all of them reach a consensus about which branch to choose. To achieve this goal, we allow the FSMs in certain situations to add a behavior prediction into its outgoing messages. Those predictions are stored in the finite-state control units and are forwarded within the existing communication to other FSMs.

The length of the prediction should be bounded, as we can attach only bounded information to the messages and we need to store it in the finite-state control unit. Therefore, it may be necessary to generate the behavior predictions multiple times. As the realization should be deadlock-free, we must ensure that the predictions are not conflicting — generated concurrently by different FSMs. To solve this we sometimes send together with the prediction also an event where the next prediction should be generated.

Definition 10. A prediction for an MSG $G = (S, \tau, s_0, s_f, L)$ is a pair $(\sigma, e) \in S^* \times (E \cup \bot)$, where E is the set of all events of bMSCs assigned by L, the path σ is called a prediction path, and e, called a control event, is an event from $L(\sigma)$. A prediction path must satisfy one of the following conditions:

- The prediction path σ is the longest common prefix of all MSG runs. This special initial prediction path is named initial Path.
- The prediction path σ is the shortest path $\sigma = \sigma_1 \sigma_2 \dots \sigma_n$ in G satisfying 1. $\sigma_n \in \mathcal{L}$, or
 - 2. $\sigma_n \in \mathcal{U} \land \exists 1 \leq i < n : \sigma_i = \sigma_n, or$
 - 3. $\sigma_n = s_f$,

where $\mathcal{L} \subseteq \mathcal{S}$ is the set of all local-choice nodes and $\mathcal{U} \subseteq \mathcal{S}$ is the set of all controllable-choice nodes.

We refer to the first node and to the last node of a prediction path σ by $firstNode(\sigma)$ and $lastNode(\sigma)$, respectively.

Lemma 1. If the prediction path σ ends with a controllable-choice node u, the bMSC $L(\sigma)$ contains a resolving event for triggers(u) on $L(\sigma)$.

Proof. There are two cases to consider

- If $\sigma = initialPath$, then $firstNode(\sigma) = s_0$ and as node u is controllablechoice, the path σ contains a resolving event for triggers(u).
- Otherwise, the controllable-choice node u occurs twice in the path σ . As every cycle containing a controllable-choice node has to contain a resolving event for the node, there is a resolving event for triggers(u) on path σ .

As there are no outgoing edges allowed in s_f , the terminal node $s_f \notin \mathcal{U}$. \Box

Note, that the number of events in a given MSG is finite and the length of each prediction path is bounded by $2 \cdot |S|$.

When the CFM execution starts, every FSM is initialized with an initial prediction — (*initialPath*, e_i) — and starts to execute the appropriate projection of L(initialPath). The value of e_i depends on the *initialPath*. Let *lastNode*(*initialPath*) = σ_n . In case of $\sigma_n \in \mathcal{U}$, the event e_i is an arbitrary resolving event from L(initialPath) for triggers(σ_n). It follows from Lemma 1 that there exists such an event. If $\sigma_n \in \mathcal{L} \cup \{s_f\}$, we set $e_i = \bot$.

Every FSM stores two predictions, one that is being currently executed and a future prediction that is to be executed after the current one. Depending on the *lastNode* of the current prediction, there are the following possibilities where to generate the future prediction.

- If *lastNode* of the current prediction is in \mathcal{L} , the future prediction is generated by the local-choice leader, while executing the first event after branching.
- If *lastNode* of the current prediction is in \mathcal{U} , the future prediction is generated by an FSM that executes the control event of the current prediction, while executing the resolving event.
- If the *lastNode* of the current prediction is s_f , no further execution is possible and so no new prediction is generated.

When an FSM generates a new prediction, we require that there exists a transition in the MSG from the last node of the current prediction path to the first node of the future prediction path, as the concatenation of prediction paths should result in a path in the MSG. If an FSM generates a future prediction ending with a controllable-choice node u, it chooses an arbitrary resolving event for triggers(u) to be the resolving event in the prediction. The existence of such an event follows from Lemma 1. To ensure that other FSMs are informed about the decisions, both predictions are attached to every outgoing message. The computation ends when no FSM is allowed to generate any future behavior.

4.1 Algorithm

In this section, we describe the realization algorithm. All the FSMs execute the same algorithm, an implementation of the FSM \mathcal{A}_p is described in Algorithm 1. We use an auxiliary function **path** that returns a prediction path for a given prediction. Every FSM stores a queue of events that it should execute — *eventQueue*. The queue is filled with projections of bMSCs labeling projection paths — $L(\text{prediction path})|_p$ for FSM \mathcal{A}_p . The execution starts with filling the queue with the projection of the *initialPath*.

Algorithm 1. Process *p* implementation

| Higorithm 1. Freedos p implementation | | |
|--|---|--|
| 1: | Variables : <i>currentPrediction</i> , <i>nextPrediction</i> , <i>eventQueue</i> ; | |
| 2: | $currentPrediction \leftarrow (initialPath, e_i);$ | |
| 3: | $nextPrediction \leftarrow \bot;$ | |
| 4: | $eventQueue \leftarrow \mathbf{push}(L(initialPath) _p);$ | |
| 5: | while true do | |
| 6: | if <i>eventQueue</i> is empty then | |
| 7: | getNextNode(); | |
| 8: | $e \leftarrow \mathbf{pop}(eventQueue);$ | |
| 9: | if e is a send event then | |
| 10: | if e is the resolving event in $currentPrediction$ then | |
| 11: | $node \leftarrow lastNode(\mathbf{path}(currentPrediction));$ | |
| 12: | $nextPrediction \leftarrow \mathbf{guessPrediction}(node);$ | |
| 13: | ${\bf send}(e, current Prediction, nextPrediction);$ | |
| 14: | if e is a receive event then | |
| 15: | $\mathbf{receive}(e, cP, nP);$ | |
| 16: | if $nextPrediction = \bot$ then | |
| 17: | $nextPrediction \leftarrow nP;$ | |

Function 2. getNextNode function for process p

| 1: Function getNextNode() | |
|---|--|
| 2: $node \leftarrow lastNode(path(currentPrediction));$ | |
| 3: if $node \in U \land p \in triggers(node)$ then | |
| 4: $currentPrediction \leftarrow nextPrediction;$ | |
| 5: $nextPrediction \leftarrow \bot;$ | |
| 6: $eventQueue \leftarrow push(L(path(currentPrediction)) _p);$ | |
| 7: else if $node \in \mathcal{L} \land p \in triggers(node)$ then | |
| 8: $currentPrediction \leftarrow guessPrediction(node);$ | |
| 9: $nextPrediction \leftarrow \bot$ | |
| 10: $eventQueue \leftarrow push(L(path(currentPrediction)) _p);$ | |
| 11: else | |
| 12: $currentPrediction \leftarrow \bot;$ | |
| 13: $nextPrediction \leftarrow \bot;$ | |
| 14: $\mathbf{polling}();$ | |
| 15: end function | |

Function 3. Polling function for process p

| 1: Function polling() |
|---|
| 2: while true do |
| 3: if p has a message in some of its input buffers then |
| 4: $\mathbf{receive}(e, cP, nP);$ |
| 5: $currentPrediction \leftarrow cP;$ |
| 6: $nextPrediction \leftarrow nP;$ |
| 7: $eventQueue \leftarrow \mathbf{push}(L(\mathbf{path}(currentPrediction)) _p);$ |
| 8: $\mathbf{pop}(eventQueue);$ |
| 9: return; |
| 10: end function |

The FSM executes a sequence of events according to its *eventQueue*. In order to exchange information with other FSMs, it adds its knowledge of predictions to every outgoing message, and improves its own predictions by receiving messages from other FSMs.

When the FSM executes a control event of the current prediction, it is responsible for generating the next prediction. The function **guessPrediction**(u) behaves as described in the previous section. It chooses a prediction (σ , e), such that (u, firstNode(σ)) $\in \tau$. If $lastNode(\sigma) \in U$, then e is a chosen resolving event in bMSC $L(\sigma)$ for the triggers set of the $lastNode(\sigma)$. Otherwise, we leave $e = \bot$.

If the *eventQueue* is empty, the FSM runs the **getNextNode** function to determine the continuation of the execution. If the *lastNode* of the current prediction is a controllable-choice node and p is in the *triggers* set of this node, it uses the prediction from its variable *nextPrediction* as its *currentPrediction*. The variable *nextPrediction* is set to \bot .

If the *lastNode* of the currentPrediction is a local-choice node and p is the leader of the choice, it guesses the prediction and assigns it to the appropriate variables. Otherwise, the FSM forgets its predictions and enters a special polling state. This state is represented by the **Polling** function. Whenever the FSM receives a message, it sets its predictions according to the message. The pop function on line 8 ensures the consistency of the *eventQueue*.

An execution is finished successfully if all the FSMs are in the polling state and all the buffers are empty. The correctness proof of the following theorem can be found in the full version [8].

Theorem 2. Let G be a controllable-choice MSG. Then the CFM \mathcal{A} constructed by Algorithm 1 is a deadlock-free realization i.e. $\mathcal{L}(G) = \mathcal{L}(\mathcal{A})$.

5 Conclusion

In this work we studied the message sequence graph realizability problem, i.e., the possibility to make an efficient and correct distributed implementation of the specified system. In general, the problem of determining whether a given specification is realizable is undecidable. Therefore, restricted classes of realizable specifications are in a great interest of software designers.

In recent years, a promissing research direction is to study deadlock-free realizability allowing to attach bounded control data into existing messages. This concept turns out to be possible to realize reasonable specifications that are not realizable in the very original setting. In this work we introduced a new class of so called controllable-choice message sequence graphs that admits a deadlockfree realization with additional control data in messages. In other words, we have succesfully extended the class of MSG conforming in the established setting of realizability. Moreover, we have presented an algorithm producing realization for a given controllable-choice message sequence graphs.

References

- Alur, R., Etessami, K., Yannakakis, M.: Inference of message sequence charts. In: Proc. of ICSE, pp. 304–313 (2000)
- Alur, R., Etessami, K., Yannakakis, M.: Realizability and verification of MSC graphs. Theor. Comp. Science 331(1), 97–114 (2005)
- Alur, R., Holzmann, G.J., Peled, D.: An Analyzer for Message Sequence Charts. In: Margaria, T., Steffen, B. (eds.) TACAS 1996. LNCS, vol. 1055, pp. 35–48. Springer, Heidelberg (1996)
- Alur, R., Yannakakis, M.: Model Checking of Message Sequence Charts. In: Baeten, J.C.M., Mauw, S. (eds.) CONCUR 1999. LNCS, vol. 1664, pp. 114–129. Springer, Heidelberg (1999)
- Baudru, N., Morin, R.: Safe implementability of regular message sequence chart specifications. In: Proc. of ACIS, pp. 210–217 (2003)
- Ben-Abdallah, H., Leue, S.: Syntactic Detection of Process Divergence and Nonlocal Choice in Message Sequence Charts. In: Brinksma, E. (ed.) TACAS 1997. LNCS, vol. 1217, pp. 259–274. Springer, Heidelberg (1997)
- Chen, C.-A., Kalvala, S., Sinclair, J.E.: Race Conditions in Message Sequence Charts. In: Yi, K. (ed.) APLAS 2005. LNCS, vol. 3780, pp. 195–211. Springer, Heidelberg (2005)
- Chmelík, M., Řehák, V.: Controllable-choice message sequence graphs. CoRR, abs/1209.4499 (2012)
- Chmelík, M.: Deciding Non–local Choice in High–level Message Sequence Charts Bachelor thesis, Faculty of Informatics, Masaryk University, Brno (2009)
- Dan, H., Hierons, R.M., Counsell, S.: A framework for pathologies of message sequence charts. Information and Software Technology (in press, 2012)
- Elkind, E., Genest, B., Peled, D.A.: Detecting Races in Ensembles of Message Sequence Charts. In: Grumberg, O., Huth, M. (eds.) TACAS 2007. LNCS, vol. 4424, pp. 420–434. Springer, Heidelberg (2007)
- 12. Genest, B., Muscholl, A.: The Structure of Local-Choice in High-Level Message Sequence Charts (HMSC). Technical report, LIAFA, Université Paris VII (2002)
- Genest, B., Muscholl, A., Kuske, D.: A Kleene Theorem for a Class of Communicating Automata with Effective Algorithms. In: Calude, C.S., Calude, E., Dinneen, M.J. (eds.) DLT 2004. LNCS, vol. 3340, pp. 30–48. Springer, Heidelberg (2004)
- Genest, B., Muscholl, A., Seidl, H., Zeitoun, M.: Infinite-State High-Level MSCs: Model-Checking and Realizability. Journal of Computer and System Sciences 72(4), 617–647 (2006)
- 15. Gill, A.: Introduction to the Theory of Finite-state Machines. McGraw-Hill (1962)
- ITU Telecommunication Standardization Sector Study group 17. ITU recommandation Z.120, Message Sequence Charts, MSC (2004)
- Jard, C., Abdallah, R., Hélouët, L.: Realistic Implementation of Message Sequence Charts. Rapport de recherche RR-7597, INRIA (April 2011)
- Ladkin, P.B., Leue, S.: Interpreting Message Flow Graphs. Formal Aspects of Computing 7(5), 473–509 (1995)
- Lohrey, M.: Realizability of high-level message sequence charts: closing the gaps. Theoretical Computer Science 309(1-3), 529–554 (2003)

- Mooij, A.J., Goga, N., Romijn, J.M.T.: Non-local Choice and Beyond: Intricacies of MSC Choice Nodes. In: Cerioli, M. (ed.) FASE 2005. LNCS, vol. 3442, pp. 273–288. Springer, Heidelberg (2005)
- 21. Mousavi, A., Far, B., Eberlein, A.: The Problematic Property of Choice Nodes in high-level Message Sequence Charts. Tech. report, University of Calgary (2006)
- Mukund, M., Narayan Kumar, K., Sohoni, M.: Synthesizing Distributed Finite-State Systems from MSCs. In: Palamidessi, C. (ed.) CONCUR 2000. LNCS, vol. 1877, pp. 521–535. Springer, Heidelberg (2000)
- Řehák, V., Slovák, P., Strejček, J., Hélouët, L.: Decidable Race Condition and Open Coregions in HMSC. Elect. Communications of the EASST 29, 1–12 (2010)