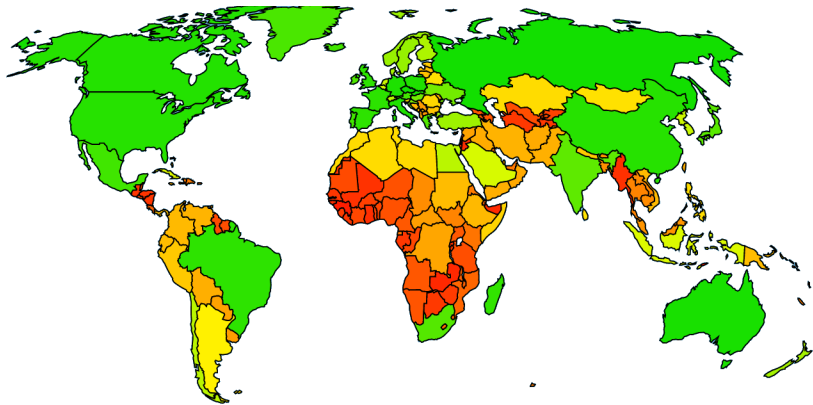


Recommender Systems and Education (with Report on Practical Experiences)

Radek Pelánek

Warm-up Quiz



This Lecture

educational applications with focus on

- relation to topics discussed so far (collaborative filtering, evaluation, ...)
- specific examples
- connections between seemingly different techniques from various research directions
- personalization and different types of recommendations
- my experience

Design Thinking Exercise

You are a member of a team developing a personalized learning system, e.g.:

- learning new language
- improving English vocabulary (advanced words)
- learning (advanced) math and machine learning
- *(your favourite topic that everybody should learn)*

You are responsible for the recommendation part of the project.

How would you approach the problem?

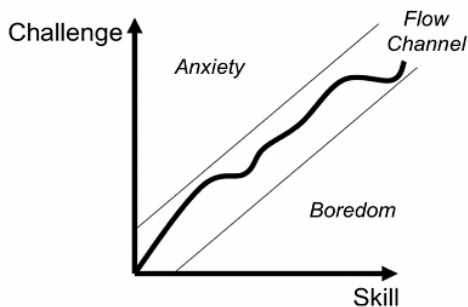
Designing New System: Questions

- 1 requirements:
 - What is the target group? Who are users?
 - What are user needs?
 - What should it do?
- 2 techniques, solutions:
 - How should it work?
 - What data you need?

Motivation: Personalization in Education

- each student gets suitable learning materials, exercises
- tailored to a particular student, adequate for his knowledge (mood, interests, ...)
- **mastery learning** – fixed outcome, varied time
(compared to classical education: fixed time, varied outcome)

Motivation: Flow, ZPD



"Flow" concept by Mihaly Csikszentmihalyi. Drawn by Senia Maymin.

Vygotsky, zone of proximal development

Personalization on Different Time Scales

time scale	learning unit	personalization
10 seconds	step	adaptive hints
1 minute	task	difficulty adjustment, personalized feedback
10 minutes	activity	mastery learning, activity recommendation
hours	course	course recommendation

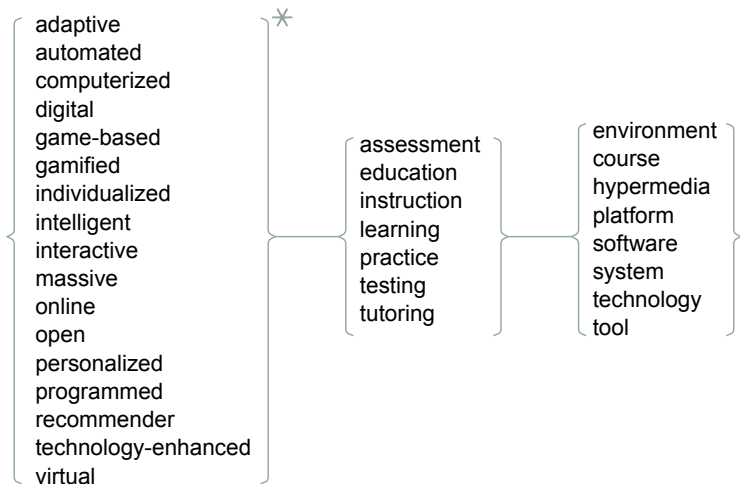
Adaptation and Personalization in Education

... gets lot of attention:

- Khan Academy
- Duolingo
- MOOC courses
- Carnegie Learning
- Pearson
- ReasoningMind
- and many others

Technology and Education

e-learning, m-learning, technology-enhanced learning, computer-based instruction, computer managed instruction, computer-based training, computer-assisted instruction, computer-aided instruction, internet-based training, flexible learning, web-based training, online education, massive open online courses, virtual education, virtual learning environments, digital education, multimedia learning, intelligent tutoring system, adaptive learning, adaptive practice, . . .



Adaptive, Intelligent, and Personalized: Navigating the Terminological Maze Behind Educational Technology

<i>Tasks</i>	<i>Description</i>	<i>Generic recommender</i>	<i>TEL recommenders</i>	<i>New requirements</i>
Existing User Tasks supported by Recommender Systems				
1. ANNOTATION IN CONTEXT	Recommendations while user carries out other tasks	E.g. predicting how relevant the links are within a web page	E.g. predicting relevance/usefulness of items in the reading list of a course	Explore attributes for representing relevance/usefulness in a learning context
2. FIND GOOD ITEMS	Recommendations of suggested items	E.g. receiving list of web pages to visit	E.g. receiving a selected list of online educational resources around a topic	None
3. FIND ALL GOOD ITEMS	Recommendation of all relevant items	E.g. receiving a complete list of references on a topic	E.g. suggesting a complete list of scientific literature or blog postings around a topic	None
4. RECOMMEND SEQUENCE	Recommendation of a sequence of items	E.g. receive a proposed sequence of songs	E.g. receiving a proposed sequence through resources to achieve a particular learning goal	Explore formal and informal attributes for representing relevancy to a particular learning goal

Recommender Systems in Technology Enhanced Learning

5. JUST BROWSING	Recommendations out of the box while user is browsing	E.g. people that bought this, have also bought that	E.g. receiving recommendations for new courses on the university site	Explore formal and informal attributes for representing relevance/usefulness in a learning context
6. FIND CREDIBLE RECOMMENDER	Recommendations during initial exploration/testing phase of a system	E.g. movies that you will definitely like	E.g. restricting course recommendations to ones with high confidence /credibility	Explore criteria for measuring confidence and credibility in formal and informal learning

TEL User Tasks that could be supported by Recommender Systems

1. FIND NOVEL RESOURCES	Recommendations of particularly new or novel items	E.g. receiving recommendations about latest additions or particularly controversial items	E.g. receiving very new and/or controversial resources on covered topics	Explore recommendation techniques that select items beyond their similarity
2. FIND PEERS	Recommendation of other people with relevant interests	E.g. being suggested profiles of users with similar interests	E.g. being suggested peer students in the same class	Explore attributes for measuring the similarity with other people
3. FIND GOOD PATHWAYS	Recommendation of alternative learning paths through learning resources	E.g. receive alternative sequences of similar songs	E.g. receiving a list of alternative learning paths over the same resources to achieve a specific learning goal	Explore criteria for the construction and suggestion of alternative (but similar) sequences

<i>Name</i>	<i>Short description</i>	<i>Advantages</i>	<i>Disadvantages</i>	<i>Usefulness for TEL</i>
<i>Collaborative Filtering (CF) techniques</i>				
User-based CF	Users who rated the same item similarly probably have the same taste. Based on this assumption, this technique recommends the unseen items already rated by similar users.	No content analysis Domain-independent Quality improves Bottom-up approach Serendipity	New user problem New item problem Popular taste Scalability Sparsity Cold start problem	Benefit from experience Allocate learners to groups (based on similar ratings)
Item-based CF	Focus on items, assuming that the items rated similarly are probably similar. It recommends items with the highest correlation (based on ratings for the items).	No content analysis Domain-independent Quality improves Bottom-up approach Serendipity	New item problem Popular taste Sparsity Cold start problem	Benefit from experience
Stereotypes or demographics CF	Users with similar attributes are matched, then it recommends items that are preferred by similar users (based on user data instead of ratings).	No cold start problem Domain-independent Serendipity	Obtaining information Insufficient information Only popular taste Obtaining metadata information	Allocate learners to groups Benefit from experience Recommendation from the beginning of the PRS

Personal recommender systems for learners in lifelong learning networks: the requirements, techniques and model

Content-Based (CB) techniques

Case-based reasoning	Assumes that if a user likes a certain item, s/he will probably also like similar items. Recommends new but similar items.	No content analysis Domain-independent Quality improves	New user problem Overspecialisation Sparsity Cold start problem	Keeps learner informed about learning goal Useful for hybrid RS
Attribute-based techniques	Recommends items based on the matching of their attributes to the user profile. Attributes could be weighted for their importance to the user.	No cold start problem No new user/new item problem Sensitive to changes of preferences Can include non-item-related features Can map from user needs to items	Does not learn with categories Ontology modelling and maintenance is required Overspecialisation	Useful for hybrid RS Recommendation from the beginning

Personal recommender systems for learners in lifelong learning networks: the requirements, techniques and model

Education and RecSys

many techniques applicable in principle, but application more difficult than in “product recommendation”

- longer time frame
- pedagogical principles
- domain ontology, prerequisites
- types of knowledge and learning processes (declarative vs procedural knowledge)
- learning outcomes not directly measurable

Evaluation

- evaluation even more difficult than for other recommender systems
- compare goals:
 - product recommendations: sales
 - text (blogs, etc) recommendations: clicks (profit from advertisement)
 - education: learning
- learning can be measured only indirectly
- hard to tell what really works

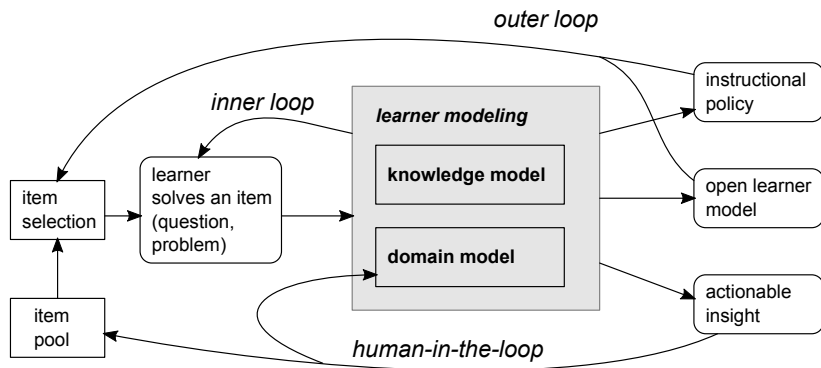
Student Modeling and Collaborative Filtering

user \sim student

product \sim problem, question

rating \sim student performance
(correctness of answer, problem solving time, number of hints taken)

Learner Modeling



Bayesian Knowledge Tracing, Logistic Models, and Beyond: An Overview of Learner Modeling Techniques

Case Studies

- our projects (FI MU) – “adaptive practice”
 - Problem Solving Tutor
 - “Slepé mapy” (Map Outlines) – geography
 - Umíme (česky, anglicky, matiku, ...) – umimeto.org
- Wayang Outpost – math
- ALEF – programming
- CourseRank – course recommender

Problem Solving Tutor

- math and computer science problems, logic puzzles
- performance = problem solving time
- focus: **predictions of times**
- recommendations – problems of similar difficulty

Problem Solving Tutor

PROBLEM SOLVING TUTOR



Body: 4464



Jste přihášen jako **radek** v individuálním módu

Můj účet

přepnout na **Výukový mód**

Odhlásit

PROBLÉMY

STATISTIKY

VÝSLEDKOVKA

Informatické



Interaktivní
Python



Konečné
automaty

```
#include <stdio.h>
int main() {
    int n, z;
    printf(" ");
    for (n = 1; n <= N;
        printf("%d ", z));
    printf("\n");
}
```

Programování
v C

pes zajíc
kočka rys
husa kozel

$^*[a-z](3,4)$$

Regulární
výrazy



Robot Karel



Robotanik



Želví grafika

Matematické

	X	Y	Z
A	1	1	1
B	0	0	0
C	1	1	1

Binární
křížovka



Grafář (nová
verze)



Matematické
pexeso 2



Obrazce



Rozbitá
kalkulačka



Transformace

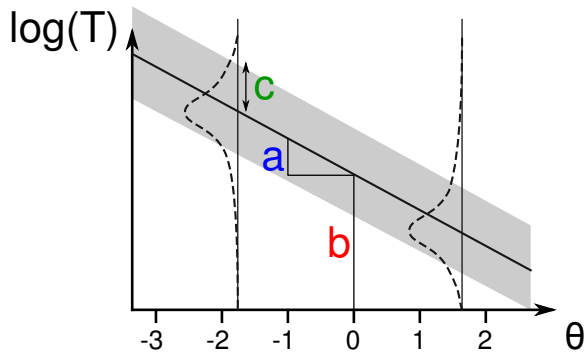


Výpočetní
stromy

Tutor: predictions

Kuželosečky - hyperboly Neřešeno Předpověď 1:12	Komplexní čísla - násobení Vyřešeno Čas 0:58	Logaritmy a mocniny - vzorečky Neřešeno Předpověď 1:14	Komplexní čísla - mocniny i Vyřešeno Čas 1:24	Vlastnosti funkcí Neřešeno Předpověď 1:17	Kuželosečky 2 Vyřešeno Čas 1:05	Zlomky Neřešeno Předpověď 1:19	Komplexní čísla - absolutní hodnoty Vyřešeno Čas 0:45	Logaritmy - hodnoty 2 Neřešeno Předpověď 1:23
Kvadratické rovnice - řešení Vyřešeno Čas 1:45	Vzdálenosti Vyřešeno Čas 1:16	Kuželosečky Neřešeno Předpověď 1:35	Množiny - základní operace Neřešeno Předpověď 1:42	Kombinační čísla Neřešeno Předpověď 1:42	Kvadratická funkce 2 Neřešeno Předpověď 1:44	Definiční obory a obory hodnot Neřešeno Předpověď 1:46	Logaritmy - vzorečky Vyřešeno Čas 2:42	Množiny Neřešeno Předpověď 1:56
Směs Neřešeno Předpověď 2:02	Derivace - goniometrické funkce Vyřešeno Čas 2:15	Součty Vyřešeno Čas 1:10	Kombinační čísla - vzorečky Neřešeno Předpověď 2:17	Komplexní čísla Neřešeno Předpověď 2:17	Úhly 2 Neřešeno Předpověď 2:29	Nerovnosti Neřešeno Předpověď 2:39	Kuželosečky - kružnice Neřešeno Předpověď 2:56	Limity funkcí Vyřešeno Čas 2:36

Model of Problem Solving Times



Parameter Estimation

- data: student s solved problem p in time t_{sp}
- we need to estimate:
 - student skills θ
 - problem parameters a, b, c
- stochastic gradient descent
- very similar to the “SVD” collaborative filtering algorithm

Evaluation of Predictions

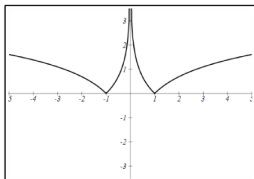
- 20 types of problems
- data: 5 000 users, 8 000 hours, more than 220 000 problems
- difficulty of problems: from 10 seconds to 1 hour
- offline evaluation: train, test set
- metrics: RMSE
- results:
 - significant improvement with respect to a baseline (mean times)
 - more complex models do not bring much improvement

same basic difficulty

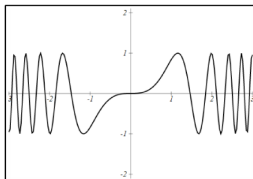
high discrimination

high randomness

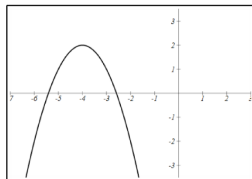
"safe" problem



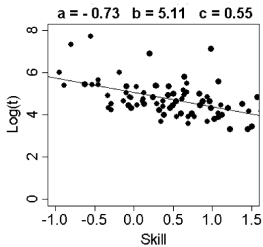
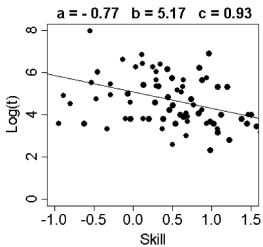
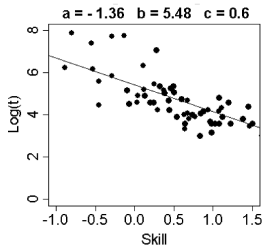
$\text{abs}(\log(\text{abs}(x)))$



$\sin(x^3)$

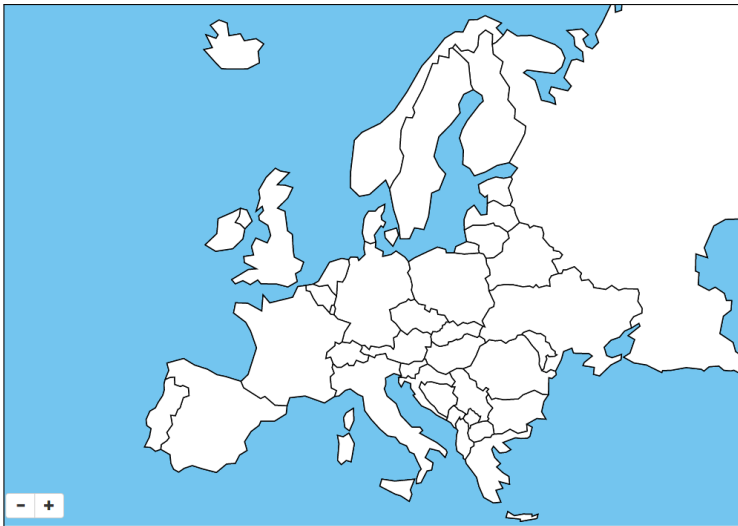


$-(x+4)^2+2$



Geography: Map Outlines

- adaptive practice of geography knowledge (facts)
- focus on **prior knowledge**
- choice of places to practice ~ recommendation (forced)

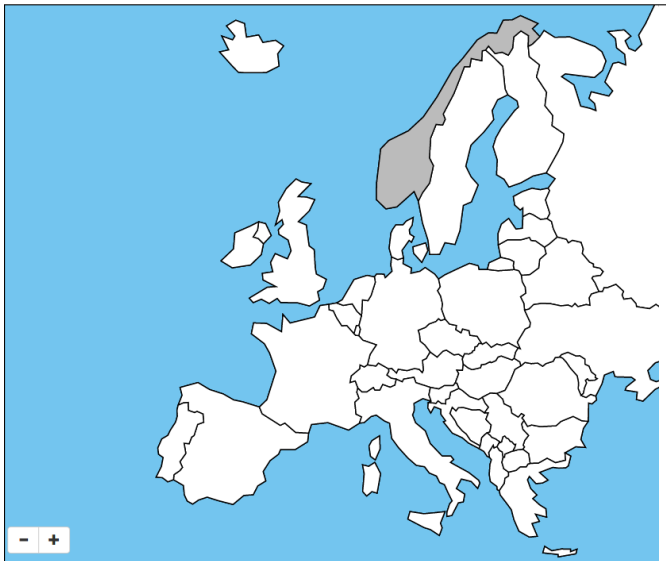


Vyber na mapě stát

 Švédsko

 Nevím

 Pokračovat



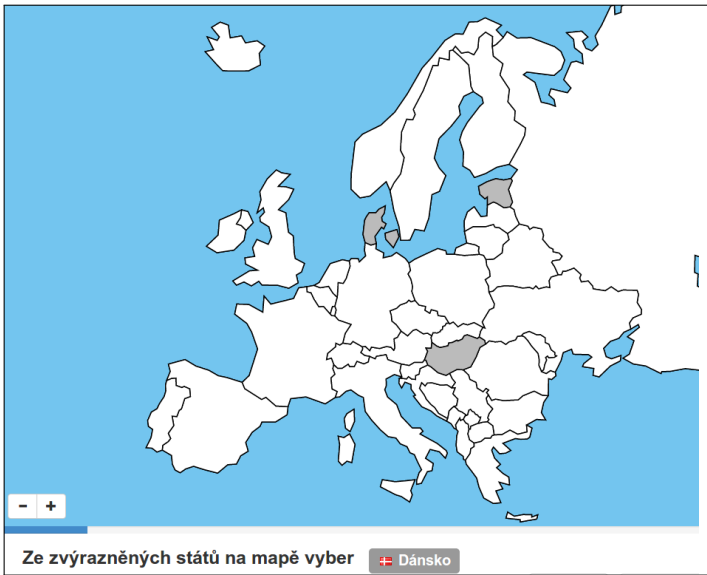
Jak se jmenuje stát zvýrazněný na mapě?

 Finsko

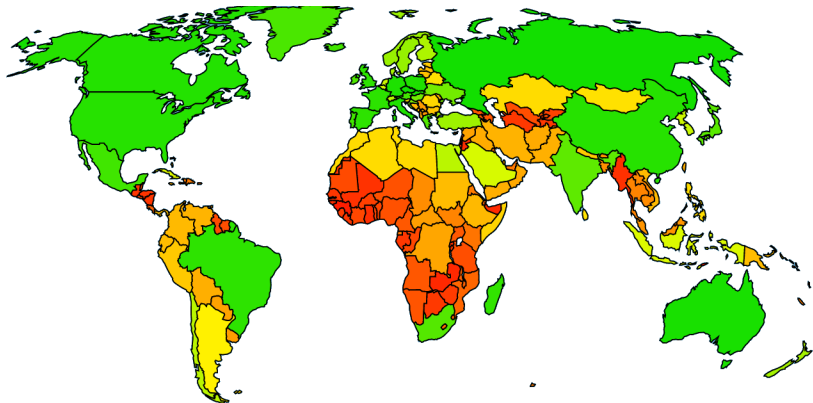
 Norsko

 Švédsko

 Nevím



Geography – Difficulty of Countries



Geography – Model

Model (prior knowledge):

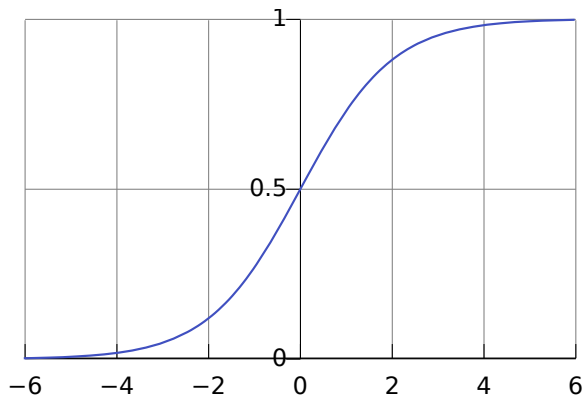
- global skill of a student θ_s
- difficulty of a country d_c

Probability of correct answer = logistic function (difference of skill and difficulty):

$$P(\text{correct} | d_c, \theta_s) = \frac{1}{1 + e^{-(\theta_s - d_c)}}$$

Logistic Function

$$\frac{1}{1 + e^{-x}}$$



Geography – Model

- Elo rating system (originally from chess)

$$\theta := \theta + K(R - P(R = 1))$$

$$d := d - K(R - P(R = 1))$$

- magnitude of update \sim how surprising the result was
- related to stochastic gradient descent, “SVD” algorithm in collaborative filtering (but only single latent factor)

Geography – Current Knowledge

- estimation of knowledge after sequence of answers for a particular place
- extension of the Elo system
- short term memory, forgetting

Geography – Question Selection

question selection (based on predicted probability of correct answer) \sim item recommendation (based on predicted rating)

based on students' history of answers, we want to create a new question

how?

Geography – Question Selection

question selection (based on predicted probability of correct answer) \sim item recommendation (based on predicted rating)

scoring function – linear combination of several factors:

- predicted success rate, target success rate
- viewed recently
- how many times asked

Geography – Multiple Choice Questions

- number of options – based on estimated knowledge
- choice of options – ???

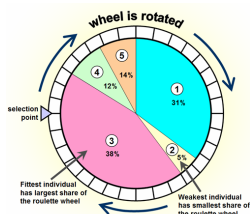
Example:

- correct answer is Hungary
- we need 3 distractors
- which countries should we use?

Geography – Distractors

choice of options (distractors) – confused places (\sim collaborative filtering aspect)

realization: roulette wheel selection (as used in genetic algorithms)



Geography – Evaluation

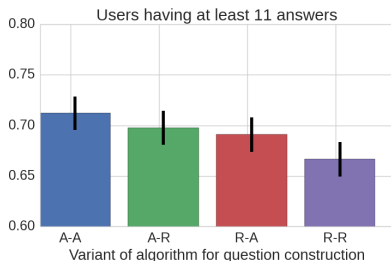
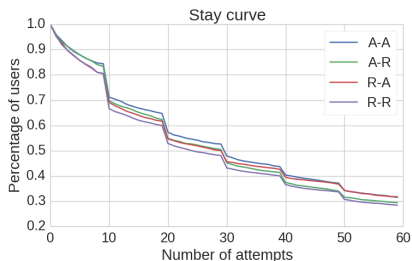
- evaluation of predictions
 - offline experiment
 - comparison of different models (basic Elo, extensions, ...)
 - issue with metrics: RMSE, AUC (\Rightarrow “Metrics for Evaluation of Student Models” paper)
- evaluation of question construction (“recommendations”)
 - online experiment, AB testing
 - issue with metrics: enjoyment vs learning

AB Testing

4 groups:

Target item	Options
adaptive	adaptive
adaptive	random
random	adaptive
random	random

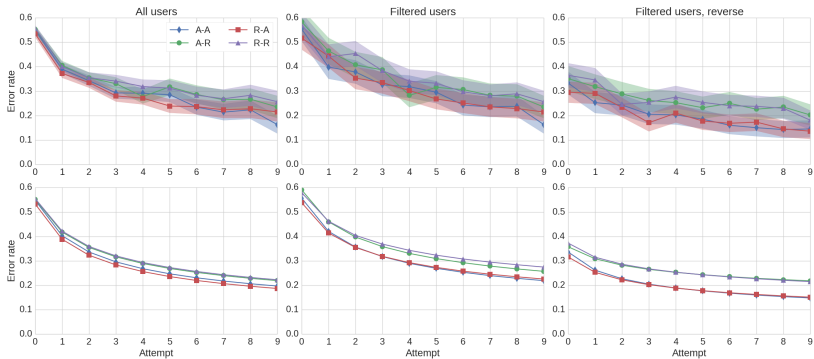
Measuring Engagement – Survival Analysis



Measuring Learning

- we cannot measure knowledge (learning) directly
- estimation based on answers
- adaptive questions – fair comparison difficult
- use of “reference questions” – every 10th question is “randomly selected”
- problem with attrition (different number of answers per student)

Measuring Learning – Learning Curves



Other AB Experiments

- difficulty of questions
- choice of distractors (competitive vs adaptive)
- maximal number of distractors
- user control of difficulty

AB experiments

- ~ 1000 users per day
- sometimes minimal or no differences between experimental conditions (in the overall behaviour)
- reasons:
 - conditions not sufficiently different (differences manifest only sometimes)
 - disaggregation (users, context) shows differences, which cancel out in overall results

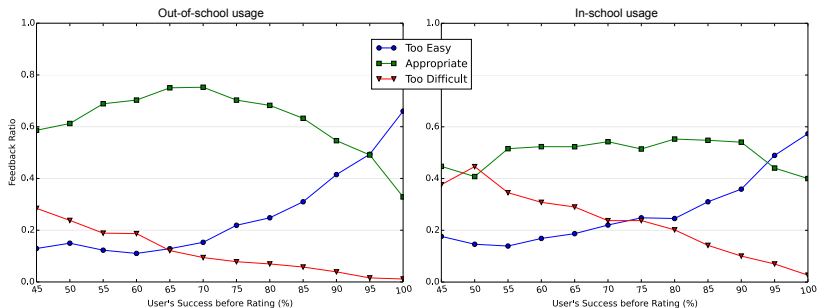
Your Intuition?

What is suitable target difficulty of questions?

Target success rate:

- 50 %
- 65 %
- 80 %
- 95 %

Difficulty and Explicit Feedback



- <http://www.umimecesky.cz/> – Czech grammar and spelling
- <http://www.umimeanglicky.cz/> – English (for Czech students)
- <http://www.umimematiku.cz/> – math
- and more... <https://www.umimeto.org/>

Czech Grammar – Project Evolution

- initial version
 - target audience: adults
 - single exercise type
 - coarse-grained concepts
 - focus on adaptive choice of items
- current version
 - target audience: children
 - many exercise types
 - fine-grained concepts
 - focus on mastery learning
 - recommendations of practice sets
 - several domains

Grammar – Basic Exercise

Míra zvládnutí: první úspěchy



You _ playing tennis.

was

were

Personalization: Mastery Learning


- skill of the learner – estimated based on the performance, taking into account:
 - correctness of answers
 - response time
 - time intensity of items (median response time)
 - probability of guessing
- mastery criterion – comparison of skill to threshold
- progress bar – visualization of skill

Grammar

Be, have, do

To be in present simple

 lehké

To do, to have, to be in present simple 


 lehké

 střední

To do, to have, to be: questions and negatives 

 lehké

 střední

To do, to have, to be in past simple 

 lehké

 střední

Be, have, do: mix

 lehké

 střední

Tenses

Talking about the present

Present simple tense 

 lehké

 střední

 těžké

Present tense: questions and negatives 

 lehké

 střední

Present simple vs. present continuous 

 lehké

 střední

 těžké

Activity Recommendations

Will vs. going to

Rozhodovačka • těžké

Koukej! To letadlo spadne!


Look! The plane crash!

is going to will

Zaměstnání

Zápis slovíček • střední

chemik



Exotická zvířata


Výběr z možností • těžké

lobster

humer
lachtan
puma
vanus

Části těla

Pexeso • těžké

živá	eyelid		scar
nostril	klobuk	throat	noční díška

Zero article

Rozhodovačka • střední

Set para do nemocnice ušít roztavce v daktung.

I went to hospital yesterday to do an interview with the doctors.

- the

Frázová slovesa: get, take

Rozhodovačka • těžké

Letadlo vzlietá v 11 hodin.

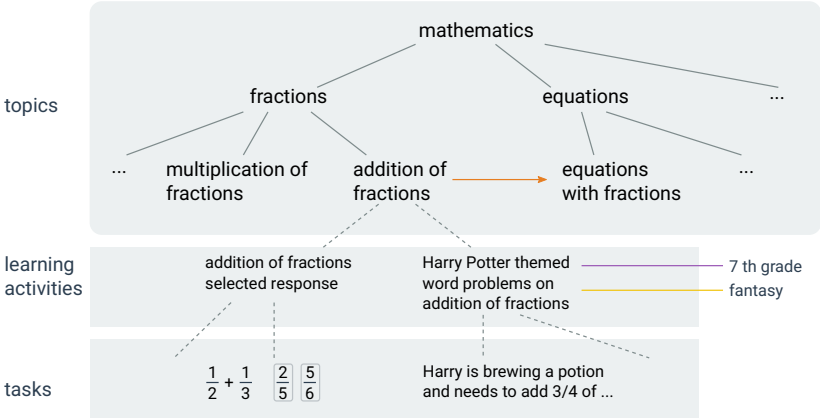
The plane takes at 11 o'clock.

off on

Recommendations Goals

- **predicting intentions**
 - something the students would like to do on their own
 - follow-up topics, homeworks
 - related to follow-up recommendations in other setting (e.g., news)
- **facilitating exploration**
 - guiding students towards content they might not actively seek out on their own
 - related to serendipity
- **reinforcing knowledge**
 - spaced repetition, interleaved practice
 - specific to education

Domain Model



relations

- taxonomy
- prerequisite
- - - membership
- grade mapping
- interests

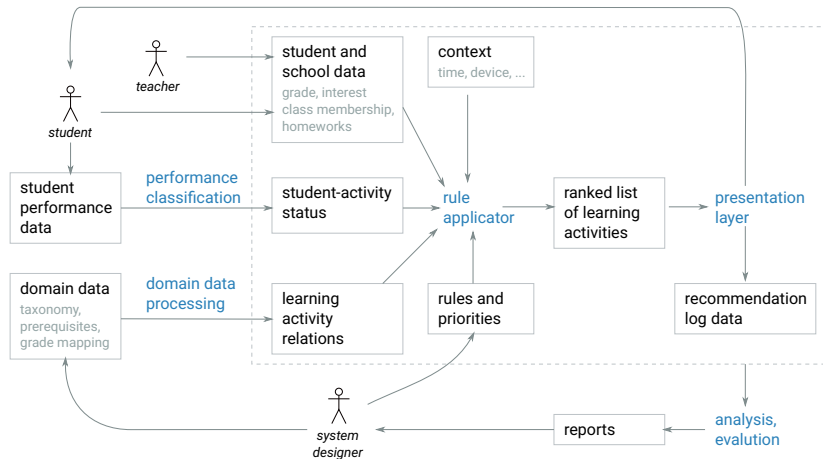
Recommendations Situations

	predicting intentions	facilitating exploration	reinforcing knowledge
homepage	✓✓	✓✓	✓✓
follow-up	✓✓✓	✓	
navigation defaults	✓✓✓	✓	✓
special		✓✓	✓✓✓

Recommendation Approach

- IF-THEN rules with priorities
- IF *condition* THEN *recommendation*
- conditions:
 - student state / previous activity
 - practice set features / relations

Recommmendation Framework



Recommendation Rules

Rule examples:

- X mastered easily and Y follows X with respect to difficulty \Rightarrow recommend Y, high priority
- X mastered weakly and Y precedes X with respect to topic \Rightarrow recommend Y, middle priority
- X mastered weakly T days ago \Rightarrow recommend Y, priority depends on T
- user grade G, X is popular for G \Rightarrow recommend X, low priority

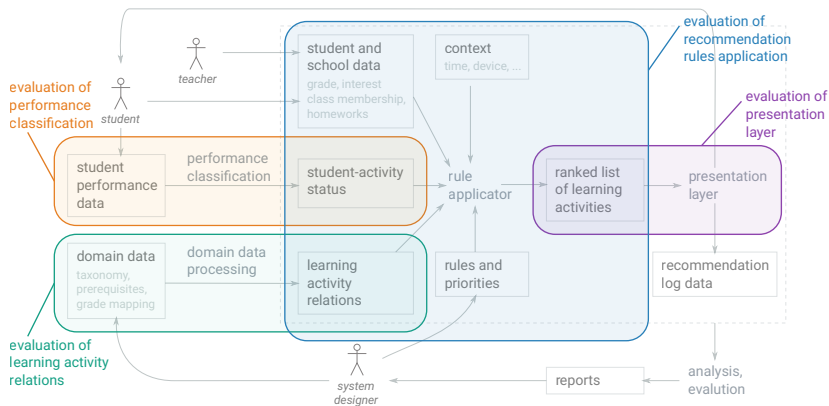
Recommendation Rules

different situations use different rules

- homepage
- follow-up recommendations
- spaced repetition recommendations

Evaluation Approach

formative, stupidity-avoiding, short-term evaluation \Rightarrow
iterative improvement of the system

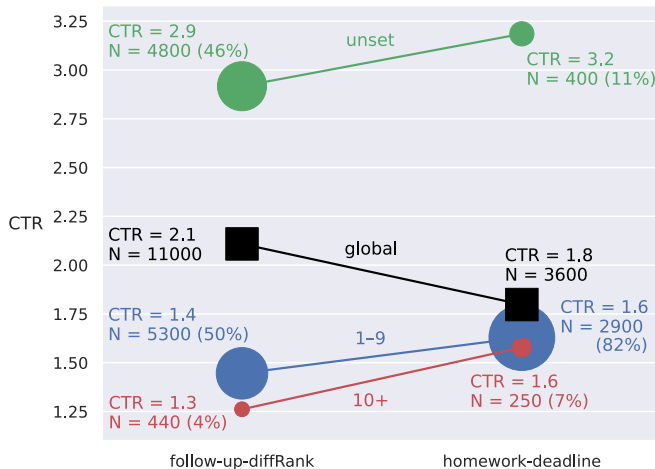


Evaluation Illustration: CTR

Table 7 Click-through rates for a selection of rules across a selection of situations, subjects, and populations. Recommendation situations: Homepage, Next to solve, Navigation in the exercise dashboard. Subjects: English, Mathematics, Computer Science. Grades: unset, primary and secondary school (grades 1–9), high school, and older (grade 10+).

	situation			subject			grade		
	Home	Next	Navig.	Eng.	Math	CS	unset	1–9	10+
follow-up-diffRank	1.2	3.1	3.5	2.7	2.0	1.1	2.9	1.4	1.3
follow-up-kc	1.1	1.6	2.5	1.9	1.3	0.7	1.7	1.1	1.1
pred-for-weak-kc	0.8	0.7	2.1	1.1	0.8	0.4	1.1	0.7	0.9
pred-for-weak-diffRank	1.2	0.8	2.0	1.4	0.9	0.7	1.3	0.9	0.6
repetition-for-weak	0.5	0.6	2.3	0.8	0.5	0.3	0.8	0.4	0.7
repetition-for-normal	0.4	0.6	1.7	0.8	0.5	0.3	0.7	0.4	0.8
homework-follow	1.2	5.1	0.0	0.7	1.0	1.8	2.0	1.1	1.0
homework-deadline	1.8	0.0	0.0	1.1	1.8	2.3	3.2	1.6	1.6
featured	0.7	0.6	4.1	1.1	1.0	0.9	0.8	1.6	1.2
peers	1.0	0.8	2.2	1.1	0.7	1.6	1.6	1.0	0.6

Evaluation Warning: Simpson's Paradox



Umíme to – Data Analysis

“design adaptation”, “avoiding stupidity”

data \Rightarrow analysis \Rightarrow insights \Rightarrow revision of items or system
behaviour

- difficulty of items
- survival analysis, length of practice
- response times
- item similarities

Item Similarities and Clustering

- closely related to item-item collaborative filtering
- item similarities: Pearson correlation of answers
- clustering: k -means
- visualization: tSNE
- key issue: do we have enough data?

Note on Different Approaches

using data, models for:

- “automatic” interventions
 - recommendations
 - personalization choices
 - mastery learning
- support for “manual” interventions
 - items behaviour
 - system behaviour
 - user behaviour

“asking right questions” often more important than “using sophisticated methods”

Illustrations of Other Techniques and Tools

- learning networks
- intelligent tutoring systems
- addressing metacognition and affect
- limited time recommendations
- course recommendations

Learning Networks

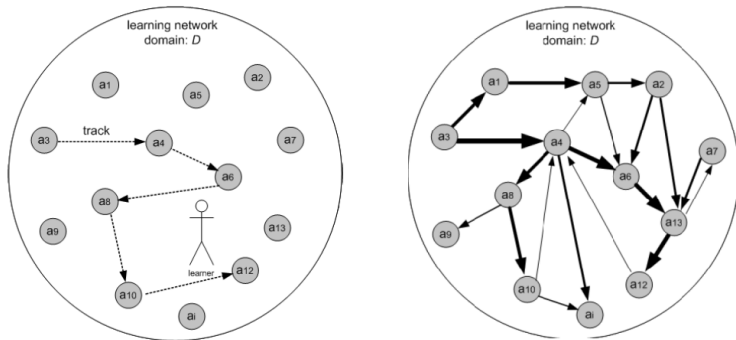


Fig. 2. Evolution of a learning network (left: starting phase with a first learner moving through possible learning activities; right: advanced phase showing emerging learning paths from the collective behavior of all learners)

Intelligent Tutoring Systems

- interactive problem solving
- behavior
 - outer loop – selection/recommendation of “items” (problems, exercises)
 - inner loop – hints, feedback, ...
- adaptation based on learner modeling
- knowledge modeling more involved than “taste modeling” (domain ontology, prerequisites, ...)

Carnegie Learning: Cognitive Tutor

Carnegie Learning's Algebra I

File Tutor Go To View Help

22 - Systems of Linear Inequalities
1 - Solving systems of linear inequalities

Sam Sample
SYLT-3X-2&YGT-5X+12

Look Ahead Problems Look Back

Linear Combination Solver Glossary Hint Done

GRAPHSETUP

Graph the inequalities $y > -5x + 12$ and $y < -3x - 2$ to find their solution set. Also, find their point of intersection.

Choose a graphing method for $y > -5x + 12$

Slope-Intercept

Slope \blacksquare

Y Intercept \bullet (,)

Choose a graphing method for $y < -3x - 2$

Slope-Intercept

Slope \blacksquare

Y Intercept \bullet (,)

Shade for the Equation $y > -5x + 12$

or

or

Carnegie Learning: Cognitive Tutor

Carnegie Learning's Algebra I

File Tutor Go To View Help

26 - Quadratic Models and Vertical Motion
1 - Using the Vertical Motion Model

Sam Sample
Bottle Rocket

Look Ahead Problems Look Back

Solver Glossary Hint Done

Scenario
(Metric units),
 v is the initial velocity of the object,
 h is the initial height above the ground.

Suppose that a bottle rocket is shot from ground level with an initial upward velocity of 80 feet per second. Further imagine that the bottle rocket turns out to be a dud. That is, it does not explode in mid-air but simply travels upward to some maximum height then falls back to the ground.

Use the formula above to write an expression for the height of the bottle rocket in terms of the time after it was shot.
Note: Since the bottle rocket is being shot from ground level, its initial height is 0 feet.

1 How high will the bottle rocket be 1 second after it was shot?
2 How high will the bottle rocket be 4.5 seconds after it was shot?
3 How many seconds after it was shot will the bottle rocket first be 96 feet high?
4 How many seconds after it was shot will the bottle rocket next be 96 feet high?
Please graph the height of the bottle rocket as a function of the time since it was shot.

5 What is the maximum height that the bottle rocket will reach?
6 When is the first time that the bottle rocket will be 75 feet high?
7 How many seconds after being launched will the bottle rocket hit the ground?

WORKSHEET

Expression	t	$-16t^2 + 80t$
Question 1	1	64
Question 2	4.5	36
Question 3	2	96
Question 4	3	96
Question 5	2.5	
Question 6	1.25	75
Question 7	5	0

Graph Point 1
Graph Point 2
Graph Point 3
Graph Point 4
Graph Point 5
Graph Point 6
Graph Point 7

GRAPHER Draw Curve X Interval 1.0 Y Interval 20

200

0.0

0.0 10.0

Wayang Outpost

- *A Multimedia Adaptive Tutoring System for Mathematics that Addresses Cognition, Metacognition and Affect*
- adaptive tutoring system for math
- Wayang Outpost → MathSpring,
<http://mathspring.org/>
- specific feature: focus on affect and metacognition

Wayang Outpost

The interface is titled "Expressions with Variables" and shows a "Skill Level" progress bar at 50%. The main text reads: "Dion wants to earn a minimum quiz average of 92% in his biology course. His grades so far are 89%, 95%, and 85%. Which inequality below represents the possible scores for his next quiz which will allow Dion to achieve his goal?"

The solution process is shown in a central area:

$$\frac{\text{Sum of the values}}{\text{Number of values}} \geq 92 \longrightarrow \frac{89 + 95 + 85 + x}{4} \geq 92$$

Solve for x.

$$269 + x \geq 368$$
$$\cancel{269} + x - \cancel{269} \geq 368 - 269$$

A pencil icon is shown below the equations.

On the left side, there are navigation icons: "HELP" (with a question mark), "DRAW" (with a pencil), and "EX:" (with a film strip). At the bottom left, there are buttons for "Formulas", "new problem", "resources", and "village".

On the right side, an animated character is sitting at a desk. The desk has a label "problem_553" and buttons for "Go To", "problem_553", "Hide me", and "Mute".

Fig. 1 The Wayang Outpost Math Tutor interface. An animated companion provides individualized comments and support

Wayang Outpost: Open Learner Model

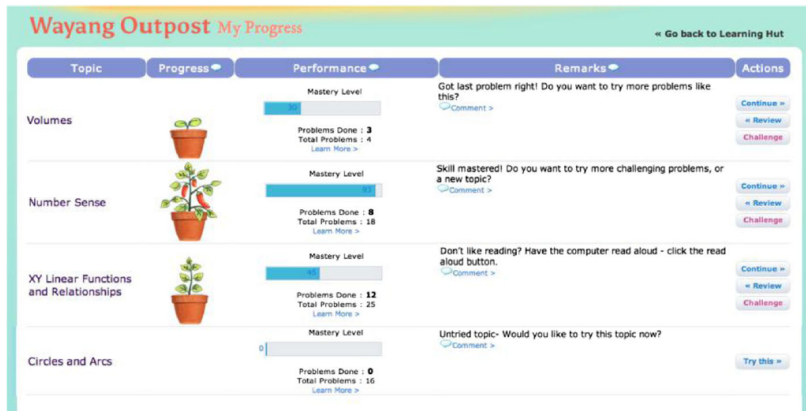


Fig. 9 The open student model in Wayang is called the Student Progress Page (SPP). It encourages students to reflect on their progress for each topic (column 1). The plant (column 2) demonstrates the tutor's assessment of student effort, while the mastery bar (column 3) records presumed knowledge (according to Bayesian Knowledge Tracing). The tutor comments on its assessment of the student's behavior (column 4) and offers students the choice to continue, review or challenge themselves and make informed decisions about future choices (column 5)

Wayang Outpost: Affect, Metacognition

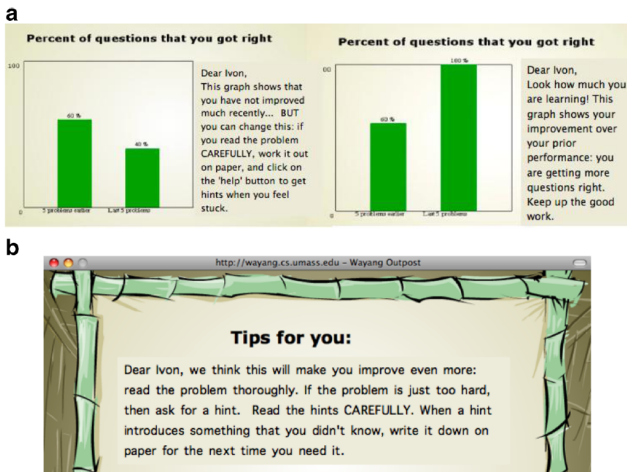


Fig. 11 a. Progress Charts in Wayang show students the accuracy of their answers. b. Tips in Wayang encourage good learning habits

Wayang Outpost: Affective Learning Companions



Fig. 14 Animated pedagogical agents display a range of emotions. Companions act out their emotion and resolve negative ones, expressing full sentences of affective and metacognitive nature, to support growth of mindset towards the view that intelligence is a state (and thus changeable)

Effort Based Tutoring

Table 1 The effort-based tutoring algorithm informs pedagogical moves and affective decisions (last two columns) for each student on each problem. The algorithm first infers a reason for students behavior (fourth column) based on the number of incorrect student answers, hints requested and the amount of time spent (first three columns). Then the algorithm decides which pedagogical action the tutor should take (last two columns). The algorithm encourages transfer of student knowledge to subsequent questions of similar difficulty (rows 2, 4, 9), encouraging students to transfer skills and “fade” their need for help

Observed behavior and inferred reason for this behavior			Pedagogical Model Moves Cognitive or Affective or Metacognitive		
Incorrect	Hints	Time	Most Likely Reason	Decision	Affective/Metacog. Decisions
1 $< E(I) - \delta_{IL}$	$< E(H) - \delta_{HL}$	$< E(T) - \delta_{TL}$	Mastery without effort	Increase Problem Difficulty	Show learning progress
2 $< E(I) - \delta_{IL}$	$< E(H) - \delta_{HL}$	$> E(T) + \delta_{TH}$	Mastery with high effort	Maintain Problem Difficulty	Affective feedback: Praise Effort
3 $< E(I) - \delta_{IL}$	$> E(H) + \delta_{HH}$	$< E(T) - \delta_{TL}$	Hint abuse, low effort	Reduce Problem Difficulty	Deemphasize importance of immediate success
4 $< E(I) - \delta_{IL}$	$> E(H) + \delta_{HH}$	$> E(T) + \delta_{TH}$	Towards mastery, effort	Maintain Problem Difficulty	Praise effort
5 $> E(I) + \delta_{IH}$	$< E(H) - \delta_{HL}$	$< E(T) - \delta_{TL}$	Quick guessing, low effort	Reduce Problem Difficulty	Deemphasize importance of immediate success
6 $> E(I) + \delta_{IH}$	$< E(H) - \delta_{HL}$	$> E(T) + \delta_{TH}$	Hint avoidance and high effort	Reduce Problem Difficulty	Offer hints upon incorrect answer in the next problem
7 $> E(I) + \delta_{IH}$	$> E(H) + \delta_{HH}$	$< E(T) - \delta_{TL}$	Quick guess and hint abuse	Reduce Problem Difficulty	Deemphasize importance of immediate success
8 $> E(I) + \delta_{IH}$	$> E(H) + \delta_{HH}$	$> E(T) + \delta_{TH}$	Low mastery and High Effort	Reduce Problem Difficulty	Emphasize importance of effort and perseverance
9 Otherwise	Expected Behavior	Maintain Problem Difficulty			

Note: Expected response (correct, hints, time) based on answers of other students \sim collaborative filtering

Wayang Outpost: Evaluation

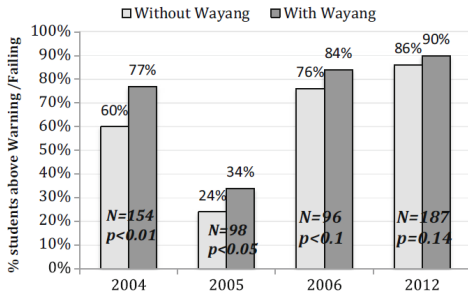


Fig. 4 Massachusetts Statewide Standardized Test (MCAS) passing rates for experimental groups (using Wayang, dark grey) and control groups (in regular math class, light grey), within the same school, same grade and same teachers. Passing rates include several ratings above warning/failing

Wayang Outpost: Evaluation

MCAS 2012 scores for Grade 7 students in a Small Town Middle School in the State of Massachusetts, USA. N=99.

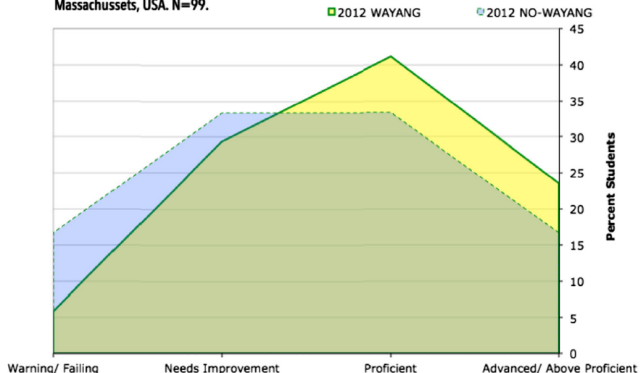


Fig. 5 Area chart comparison of performance for a 7th grade of students on the Massachusetts Comprehensive Assessment System (MCAS), for students using vs. not using Wayang Outpost. Students represented by the *yellow/green polygon* used Wayang Outpost and students represented by the *blue polygon* did not use the tutor. Distribution of students using Wayang Outpost shifts to the right indicating that more students passed the exam and received a grade of “proficient” or “advanced” when using Wayang Outpost. Groups of students were matched in terms of teacher of seventh grade students

Wayang Outpost: Evaluation

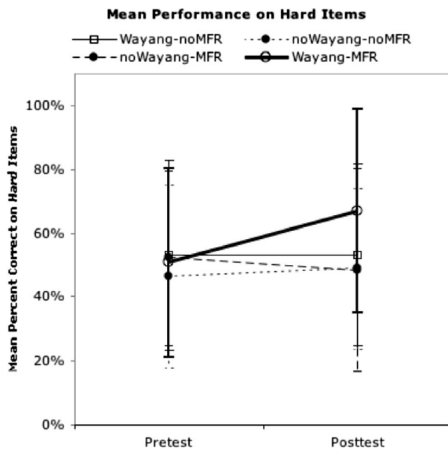


Fig. 7 Mean improvement (and standard deviations) on hardest items of the math pre/posttest. The *thick line* represents students who received both the Wayang Tutor and math facts retrieval training software; all other groups did not really improve on these harder multi-step items

Wayang Outpost: Evaluation

Table 2 Students in the experimental group (last row) received tips and charts every 6 problems. Means and standard deviations in performance measures before and after tutoring for the three groups

Group	Math Pretest	Math Posttest	Passing Rate in State Standard Exam
No Tutor Control			76 % (N=38)
Tutor Control	40 % (20) (N=40)	40 % (28)* (N=40)	79 % (N=34)
ProgressTips Tutor	33 % (19) (N=36)	42 % (22)* (N=36)	92 % (N=24)

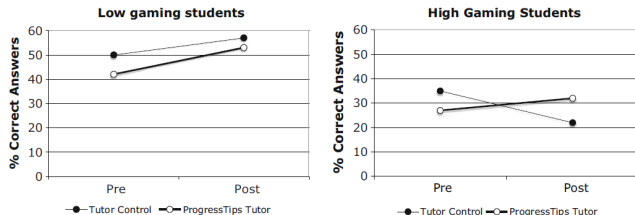
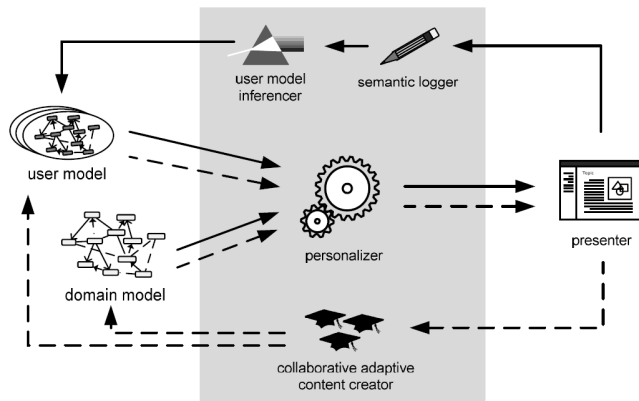


Fig. 12 High gaming students improve math performance when they receive progress tips and interventions (*left*) but not when they don't receive interventions (*right*)

- PeWe (Personalized Web) Group at UISI FIIT STU, Bratislava
- adaptive education (mainly) for programming exercises
- specific aspect: recommendations for limited time



ALEF: A Framework for Adaptive Web-Based Learning 2.0, Šimko, Barla, Bieliková

1 **Odporúčané**

- Funkcia FIRST
- Funkcie APPEND a LIST
- Špecifikácia typu zoznam
- Elementárne operácie

2 Zvoľte si tému

- Paradigmy programovania
- Výrazy**
- Výrazy a príkazy
- Vlastnosti číselných výrazov
- funkcionálne programovanie
- Základné prvky jazyka lisp
- Lisp-zoznam
- Programovacie techniky
- Pohľad na rekursiu

Chat (15)

Nezabudnite, že takmer každý výžubový text obsahuje niekoľko otázok, pomocou ktorých získate spätnú väzbu o vašich znalostiach.

Funkcia REST

Komplementárnou funkciou k FIRST je funkcia REST, ktorá vráti celý zvyšok zoznamu bez prvého prvku. Poznamenajme, že funkcia REST vždy vráti zoznam.

Obt. 1 znázorňuje príklad použitia oboch funkcií FIRST aj REST.

```

graph LR
    A["(7 2 14)"] --> B["FIRST"]
    A --> C["REST"]
    B --> D["7"]
    C --> E["(2 14)"]
  
```

5 Filtrik napísal: hodnotenie: +6

Aplicácia funkcie REST na prázdný zoznam je predse definovaná v Common Lispe a vracia typ bodka-dvojica

Funkcie FIRST a REST. Aplikácia funkcie REST na prázdný zoznam a atóm nie je definovaná. Funkcie FIRST a REST môžeme kombinovať a tým vytvorí ďalšie výberové operácie. Napr.:

```

* (FIRST (REST '(7 2 14)))
2
  
```

3 **Príklad firstk**

Zadanie:
Definujte funkciu, ktorá vráti prvých K prvkov zoznamu.

(firstk 2 '(a b c)) : -> (a b)
(firstk 0 '(a b c)) : -> NIL
(firstk 7 '(a b c)) : -> (a b c)

[Poznáť odpoveď](#) [Nepoznáť odpoveď](#)

◀ Prechádzajúci Nasledujúci ▶

4 Otázky

Vyhodnot nasledujúcu formu
(FIRST '(A B ()))

Odpovede:

- (A) X
- NIL
- A ✓
- (A B)

Počíta sa tá otázka? Áno / Nie

Znam otázku Nahodná otázka

Otázky a odpovede

CourseRank

- recommendations of whole courses
- course evaluation and planning social system
- ranking of courses, grade distribution, other statistics
- originally Stanford, later many (US) universities, out of order now
- similar features e.g. in Coursera
- some attempts done in IS MU (but hard to practically apply in real university setting)

Summary

personalized education \leftrightarrow recommender systems

- many similarities
- specific challenges
- difficult evaluation