PatternHunter: Faster And More Sensitive Homology Search

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Abstract

Motivation: Genomics and proteomics studies routinely depend on homology searches based on the strategy of finding short seed matches which are then extended. The exploding genomic data growth presents a dilemma for DNA homology search techniques: increasing seed size decreases sensitivity whereas decreasing seed size slows down computation.

Results: We present a new homology search algorithm "PatternHunter" that uses a novel seed model for increased sensitivity and new hit-processing techniques for significantly increased speed. At Blast levels of sensitivity, PatternHunter is able to find homologies between sequences as large as human chromosomes, in mere hours on a desktop.

Availability: PatternHunter is available at http://www.bioinformaticssolutions.com, as a commercial package. It runs on all platforms that support Java.

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Introduction

We are interested in faster and more sensitive methods for finding all approximate repeats or homologies in one DNA sequence or between two DNA sequences, as performed by the popular Blastn (Altschul *et al*, 1990) program. One particular application of this task is in comparative genomics where large genomes or chromosomes such as the human one (International Human Genome Sequencing Consortium, 2001; Venter *et al*, 2001) need to be compared.

Many programs have been developed for the task. These include FASTA (Lipman and Pearson, 1985), SIM (Huang and Miller, 1991), the Blast family (Altschul *et al*, 1990; Gish, 2001; Altschul *et al*, 1997; Zhang *et al*, 2000; Tatusova and Madden, 1999), SEN-SEI (States, 2000), MUMmer (Delcher *et al*, 1999), QUASAR (Burkhardt *et al*, 1999), and REPuter (Kurtz and Schleiermacher, 1999). Smith-Waterman alignment which compares all bases against all bases is clearly too slow. Two lines of approach lead to improvements. The first is exemplified by Blast, which is used routinely by thousands of scientists. This approach finds short exact "seed" matches (hits), which are then extended into longer alignments. However, when comparing two very long sequences, FASTA, SIM, Blastn (BL2SEQ), WU-Blast, and Psi-Blast run very slow and need large amounts of memory. SENSEI is somewhat faster and uses much less memory than the above programs, but is currently limited to ungapped alignments. MegaBlast runs quite efficiently with its default gap scores and large seed length of 28 but turns out to have worse output quality and doesn't scale as well to huge sequences.

Another line of approach, exemplified by MUMmer, QUASAR and REPuter, uses suffix trees. Suffix trees suffer from two problems: They are meant to deal with precise matches and are limited to comparison of highly similar sequences (Delcher *et al*, 1999; Burkhardt *et al*, 1999; Kurtz and Schleiermacher, 1999). They are very awkward in handling mismatches. The second problem with suffix trees is that they have an intrinsic large space requirement.

We introduce novel seeding schemes and hitprocessing methods, which are implemented in our program PatternHunter. On a modern desktop, its running time ranges from seconds for prokaryotic genomes to minutes for arabidopsis chromosomes to hours for human chromosomes, with very modest memory use, and at provably higher sensitivity than the default Blastn.

Selecting Good Seeds: Expect Less to Get More

A dilemma for a Blast type of search is that large seeds lose distant homologies while small ones creates too many random hits which slow down the computation. We use a new idea that allows us to have a higher probability of a hit in a homologous region, even while having somewhat lower expected number of random hits.

Blast looks for matches of k (default k = 11 in Blastn and k = 28 in MegaBlast) consecutive letters as seeds. Instead we propose to use *non*-consecutive k letters as seeds. We call the relative positions of the k letters a *model*, and k its *weight*.

This seemingly simple change has a surprisingly large effect on sensitivity. An appropriately chosen model can have a significantly higher probability of having at least one hit in a homologous region, compared to Blast's consecutive seed model, even while having a lower expected number of hits¹. For example, in a region of length 64 with 70% identity, Blast's consecutive weight 11 model has a 0.30 probability of having at least one hit in the range, while a nonconsecutive model of the same weight has a 0.466 probability of getting a hit, see Figure 1. On the other hand, the expected number of hits in that region by the Blast consecutive model is 1.07, while the nonconsecutive model expects 0.93 hits. This is because the length 11 model can shift over 54 places within the length 64 window, while the length 18 model has only 47 places to fit. The reason for the increased sensitivity is that the events, of having a match at different positions, become more independent for spaced models. If a model and a shifted copy share many 1s in the same position, then a base mismatch in any of these shared positions will make both matches fail, hence the corresponding matching events are far from independent. Independent events are better at pooling their success probabilities together. Generally, the fewer bases shared by a model and any of its shifted copies, the higher its sensitivity is. Clearly, by this measure, consecutive models are the worst, since shift of 1 shares all but one bases.

For convenience, we denote a model by a 0-1 string, where the 1-positions represent required matches, while the 0s are "don't cares". For example, if we use a weight six model 1110111, then actgact v.s. acttact is a seed match, as well as actgact v.s. actgact. So Blast uses models of the form 1^k . Blast actually matches two or three bytes, each containing four bases, simultaneously, and extends these hits to the left and right. This is fine for the default of k = 11 because any length 11 match necessarily contains a match of two bytes, but for k smaller than 11, it will miss some seeds.

Suppose a substring s from the query sequence is similar to a same-length substring t from the target sequence. Let v = v(s, t) be a 0-1 string indicating the matches between s and t, i.e. v[i] = 1 if and only if s[i] = t[i]. Say that a model m covers a binary string u of the same length if $m[i] \le u[i]$, i.e. u has a 1 wherever

m has a 1. Then a hit between s and t occurs wherever the model covers a substring of v(s, t).

To evaluate a model, we compute its probability of generating a hit in a fixed length region of given similarity, by dynamic programming (which works fine up to model size 20 and quickly becomes prohibitive in both time and space beyond that). We somewhat arbitrarily chose a region length of 64 because in practice ungapped homologies are typically of size 20 to 200 bases. Note that the shorter the region length, the more a (longer) spaced model suffers by having fewer places to fit. For weight 11, the most sensitive model is 111010010100110111 with sensitivity 0.467122 for 70% similarity. Figures 1 and 2 compare the nonconsecutive model 110100110010101111 with Blast's consecutive models. This model, found heuristically before we discovered the dynamic programming algorithm, is slightly suboptimal, with a sensitivity of 0.465485, and was used in all experiments in this paper for weight 11. The new PatternHunter uses the optimal model 111010010100110111 and will support user-defined, randomly generated, and neighbourhood models in future. Using different models allows PatternHunter to have different outputs in different runs, thus increasing the sensitivity. Neighbourhood models use multiple similar models simultaneously to further increase sensitivity. For each similarity percentage shown on the x-axis, the percentage of regions acquiring at least 1 hit is plotted on the y-axis as the sensitivity at that similarity level in Figure 1. Recalling our earlier discussion of independence, the (near) optimality of these two models is witnessed by the fact that any shift shares no more than five bases.

The current 1.4 version of Blast triggers an extension if two disjoint hits are found on the same diagonal within a certain distance (Altschul *et al*, 1997). The increased selectivity more than offsets the loss in sensitivity, so that it can use a smaller weight model and still generate fewer extensions than an equally sensitive 1 hit model of larger weight. The same can be done with spaced models, with the advantage that hits are no longer required to be disjoint in order to gain a lot of sensitivity. Figure 2 compares the sensitivity of a double hit spaced weight 11 model against single hit weight 11 and 12 consecutive models.

SENSEI uses a default seed size of eight; Figure 3 compares its sensitivity with that of a spaced weight nine model.

The expected number of hits in a region can be easily calculated as in the following Lemma.

Lemma 1 The expected number of hits of a weight W, length M model within a length L region of similarity $0 \le p \le 1$, is $(L - M + 1)p^W$.

 $^{^1{\}rm For}$ statistical purposes, we count overlapping hits separately, while the Blast program ignores hits overlapping the last recorded one.



Figure 1: 1-hit performance of weight 11 spaced model versus weight 11 and 10 consecutive models, coordinates in logarithmic scale.



Figure 2: 2-hit performance of weight 11 spaced model versus single hit weight 11 and 12 consecutive models.

Proof: The expected number of hits is the sum, over the (L-M+1) possible positions of fitting the model within the region, of the probability of W specific matches, the latter being p^W .

Observations:

- Figures 1, 2, 3 show that the steeper curve of the spaced seed model has *smaller* hit probability in low similarity regions, with respect to the closest consecutive model in terms of sensitivity. In fact, Figures 1 and 3 show that we can use a spaced model of weight 9 to replace a consecutive weight 8 model, gaining sensitivity above 64% similarity, or use a weight 11 spaced model to replace a weight 10 consecutive model gaining sensitivity above 60%. Note that increasing the weight by 1 reduces the number of random hits by approximately a factor of four.
- It has been brought to our attention, that a re-



Figure 3: 1-hit performance of weight eight consecutive model versus weight nine nonconsecutive model

lated but conceptually different approach, has been applied to ungapped homology search in (Buhler, 2001; Califano and Rigoutsos, 1995).

(Buhler, 2001) applies a random hashing/projection technique known as locally-sensitive hashing (LSH) (Indyk et al, 1998), as follows. In each of hundreds of iterations, a newly chosen random hash function is applied to every region of a fixed size (of about 100), and regions mapping to the same value are fully compared. Similar overlapping regions on the same diagonal are then merged into ungapped alignments. Unlike Blast, a long ungapped alignment can only be found if the regions found to be similar cover its whole length. Earlier, a similar idea has been applied in Flash (Califano and Rigoutsos, 1995), which used shorter regions. Both papers focused on covering a homology entirely with hits, instead of doing hit-extension in Blast style.

Retrospectively, our carefully chosen deterministic spaced seed model maximizes the chance of any HSP to contain *at least one* seed, while minimizing random hits. Experiments show that SEN-SEI (States, 2000) (which is also limited to ungapped alignment), at its default size 8 seed, is faster than LSH.

PatternHunter: Compare Whole Genomes On Your Desktop

We have implemented PatternHunter in Java using the spaced seed model and various algorithmic improvements using advanced data structures.

Hit Generation

PatternHunter uses a method of generating hits similar to that of MegaBlast. ² For each position in one sequence, compute an index from fitting the model at that particular position. This index is $2 \times$ weight bits long (two bits per base). Then do a lookup in a big table which gives the first position in the other sequence where the model matches. This gives the first hit. Subsequent hits are found using another table, which for each position gives the next position where the model matches. This table requires one int (four bytes) per base. If the number of hits found for one index is large then because of the relative cost of computing the index becomes negligible.

For each hit, we look up its diagonal in another hashtable, the hit table, to find the rightmost matched position on that diagonal. If this position is to the right of the hit then we ignore the hit as being part of an already found match.

If the double hit option is chosen then in absence of a recent hit on the same diagonal, we merely record the new one.

Hit Extension

Next we extend this hit in a greedy fashion to the left and right, stopping when the score drops by a certain amount. If the resulting segment pair has a score below a certain minimum, then we ignore it, else we have a Highscoring Segment Pair (HSP). The position of the last comparison, which reached the dropoff score, is stored in the hit table, so that future equivalent hits within this HSP can be recognized as redundant.

Gapping extension

To find the best way to extend a HSP to the left across gaps, we try all candidates from a diagonal-sorted set of recently found HSP, after adding to this set some new HSPs found by local hit generation. We use a variation of a red-black tree to implement the set of HSPs sorted by diagonal. HSPs are inserted in the tree once an optimal gapped alignment to its left is found, and retired from the tree once newly generated HSPs are too far beyond its right endpoint to make use of it. Retired alignments are put into a priority queue according to their scores.

The local hit generation finds triple hits of the small model 1101 in a limited length region to the left of the HSP and stores them in the tree if they have a certain minimum length.

For each candidate HSP to gap a newly found HSP to, we compute the gapping cost as the sum of the gap open plus gap extension penalties plus the cost of adjusting either HSP in size to make a perfect fit. From this data the best HSP, if any, to link to, is chosen and used to compute the optimal partial alignment score. Overlapping alignments are not reported.

Implementation

PatternHunter is implemented in Java, hence platformindependent. We have made great efforts to write simple, clean, and short code. The executable size of PatternHunter is 40KB, only 1% of the size of Blast, while offering a large fraction of its functionality.

With two input sequences of length n and m, m > n, and model weight 11, PatternHunter uses 16 Megabytes for the hashtable entries and 4n bytes for the array of next-occurrence indices. Together with n + m bytes to store the inputs, and a variable amount for other data structures, PatternHunter uses about $(4^{W+1} +$ $m + (5 + \epsilon)n)$ bytes of memory, in addition to the Java Virtual Machine's memory footprint (which can range from half a Mbyte to a dozen Mbytes). Here, W is the model weight, and $\epsilon > 0$ is a small constant depending on the options PatternHunter uses. For the default $W = 11, 4^{W+1}$ amounts to 16Mbytes. Typically ϵ is much smaller than 1. We conclude that the reason this theoretical estimation is not exactly reflected in Figure 7 is that the java virtual machine does not do garbage collections often when there are still enough free memory in the heap to use. Our recent experiments on larger human chromosomes demonstrated that our estimation in memory is accurate. This allows PatternHunter to work on complete chromosomes of the human genome on a modern desktop computer with 2 gigabytes of memory.

Results

Here, we report several test runs of PatternHunter with comparison to other programs. Since the Blast family, especially the newly improved Blastn, is the industry standard, and widely recognized for its sensitivity (Blastn, SENSEI) and speed (Blastn, MegaBlast), we limit ourselves to comparison with these programs. All experiments are performed on a 700 MHz Pentium III PC with 1Gbyte of memory. The table in Figure 7 compares PatternHunter with the latest versions of Blastn and MegaBlast, downloaded from the NCBI website on July 9th 2001. All programs were run without filtering (bl2seq option -F F) to ensure identical input to the actual matching engines. The table in Figure 8 compares PatternHunter with SENSEI; note that SEN-SEI, as currently available, does not do any gapped

²Note that (Mega)Blast computes its indices more efficiently by packing four bases into one byte.

alignments. One may suspect that PatternHunter sacrifices quality for speed. Figures 4, 5, 6 show the opposite. In Figure 4, MegaBlast using seed weight 28 (MB28) misses over 700 high scoring alignments. Using the same parameters, PatternHunter outputs better results than Blastn, is 20 times faster and uses one tenth the memory, Figure 5. Notice the quick growth of Blastn/MegaBlast time/space requirements, indicating poor scalability. Only MegaBlast (MB28) at its default affine gap costs allowed us to continue the comparison, without running out of memory, but with vastly inferior output quality compared to PatternHunter (PH2), which uses only one fifth the time and one quarter the space, Figure 6. Finally, PatternHunter has recently been used to compare the human genome with 16 million reads of the unassembled mouse genome, a total of nine billion base pairs. PH2, weight 12, finishes in 20 (Pentium III) CPU-days. PH2, weight 11, finishes in 80 CPU-days. The results will be available at http://genome.cse.ucsc.edu/ While MegaBlast is designed for high speed on highly similar sequences and Blastn for sensitivity, PatternHunter simultaneously exceeds Blastn in sensitivity, MegaBlast in speed (on long sequences), and both in memory use. Written in Java, it runs any genome anywhere.



Figure 4: Input: *H. influenza* and *E. coli.* Run times are shown in Figure 7. Score is plotted as a function of the rank of the alignment, with both axes logarithmic. MegaBlast (MB28) misses over 700 alignments of score at least 100. MB11 is MegaBlast with seed size 11 (50 times slower and 10 times more memory use than PH2), indicating the missed alignments by MB28 are mainly due to seed size.

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Figure 5: Input: *H. influenza* and *E. coli*. Run times are shown in Figure 7. PatternHunter produces better quality output than Blastn while running 20 times faster.

2001; Indyk *et al*, 1998) to our attention. We thank Larry Miller for working on related projects, David Lipman for comments and bringing (Califano and Rigoutsos, 1995) to our attention, Xiaoqui Huang for his comments, Dan Brown and Jim Kent for letting us using PatternHunter to mouse-human genome comparison, David States for providing information on SENSEI, and the referees for their useful suggestions. BM was supported by NSERC Research Grant OGP0046506. JT was supported by BSI. ML was supported in part by NSERC Research Grant OGP0046506, a CITO grant, and NSERC's Steacie Fellowship. Both BM and ML's work was done when they were at University of Waterloo.

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Figure 6: Input: A. thaliana chr 2 and chr 4. Run times are shown in Figure 7. PatternHunter (PH2) outscores MegaBlast in one sixth of the time and one quarter the memory. Both programs used MegaBlast's non-affine gap costs (with gapopen 0, gapextend -7, match 2, and mismatch -6) to avoid MegaBlast from running out of memory. For comparison we also show the curve for MegaBlast with its default low complexity filtering on, which decreases its runtime more than sixfold to 3305 seconds.

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ŝ	Seq1	Size	$\operatorname{Seq2}$	Size	PH	PH2	MB28	Blastn
M. pn	eumoniae	828K	M. genitalium	589K	10s/65M	4s/48M	1s/88M	$47 \mathrm{s} / 45 \mathrm{M}$
E	E. coli	4.7M	H_{\cdot} influenza	1.8M	34s/78M	14s/68M	5s/561M	716s/158M
A.thal	iana chr 2	19.6M	A.thaliana chr 4	17.5M	$5020 \mathrm{s}/279 \mathrm{M}$	498s/231M	$21720 { m s}/1087 { m M}$	∞
H. sapa	$iens \ chr \ 22$	35M	H. sapiens chr 21	26.2M	$14512 \mathrm{s}/419 \mathrm{M}$	$5250 \mathrm{s}/417 \mathrm{M}$	∞	∞

Figure 7: Performance Comparison: If not specified, all with match 1, mismatch -1, gap open -5, gap extension -1. PH denotes PatternHunter with seed weight 11, PH2 denotes same with double hit model (sensitivity similar to Blast's single hit size 11 seed, Figure 2) MB28 denotes MegaBlast with default seed size 28, and default affine gap penalties. Blastn (via BL2SEQ) uses default seed size 11. Table entries under PH, PH2, MB28 and Blastn indicate time (seconds) and space (megabytes) used; ∞ means out of memory or segmentation fault.

Seq1	Size	$\operatorname{Seq2}$	Size	PH(9)	PH(11)	SENSEI
E. coli	4.7M	H. influenza	1.8M	$279 \mathrm{s}/67 \mathrm{M}$	34s/78M	780s/64M
A. thaliana chr 2	$19.6 \mathrm{M}$	A.thaliana chr 4	17.5M	$677 \mathrm{m}/282 \mathrm{M}$	84m/279M	$781 \mathrm{m}/415 \mathrm{M}$

Figure 8: PatternHunter with seed weights 9,11, 1-hit model vs SENSEI's weight 8 seed. SENSEI only does ungapped alignments. PatternHunter's weight 9 spaced seed has higher single-hit sensitivity than SENSEI's 8 as shown in Figure 3.