Math OCR – Why?	OCR for Mathematics – How?	DML-CZ OCR	Results	Summary and Further Work
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Optical Character Recognition of Mathematical Texts in the DML-CZ Project¹

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Starter, Motivation and Goa	lə			

What is this story about?

- important problem: from pixel sets to the information (when awake, your brain spends almost half of its capacity for this task)
- important application: how to have all the math papers published in a digital searchable for: imagine all mathematical information/knowledge available at your fingertips!
- pleasant surprises (unexpected connections, difficulties, solutions and beauty): it actually works reasonably well!
- No sex and violence, sorry.

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Motivation, Goals

- ① DML-CZ http://dml.cz, http://project.dml.cz
- ② not only page images, but added value wrt. Google Scholar
- 3 full text indexing, good searching (and ranking),
- well clasified papers, with hypertext links between them and referee databases (ZentralBlatt MATH and Math Reviews)
- (5) persistent and stable access, aimed at full (text) visibility in the global information space (Google Scholar, OAI-PMH servers, ...)

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Starter, Motivation and Goals

DML-CZ workflow steps



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Starter, Motivation and Goals

Top-level DML-CZ workflow overview (simplified)



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Proof. Let \hat{K} be a cube, $\hat{K} \subset \hat{C}$; put $K = q^{-1}(\hat{K})$. According to theorem 50 we have $K \in \mathfrak{A}$ and it follows from theorem 24 that

$$P(K, v) = \int f(x) dx$$
. (89)

The functional determinant T of the mapping $\psi = \varphi^{-1}$ fulfils the relation $T(\varphi(x))$. det M(x) = 1, so that

$$\int_{K} f(x) dx = \int_{K} f(\varphi(y)) \cdot |T(y)| dy = \int_{K} \hat{f}(y) dy. \quad (90)$$

From theorem 50 (and relation (86)) we see that $P(K, v) = P(\hat{K}, \hat{v})$; relations (89), (90) show therefore that $P(\hat{K}, \hat{v}) = \int \hat{f}(y) \, dy$, which completes the proof.

Remark. The reader may compare this paper with [6].

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Резюме

поверхностный интеграл

ЯН МАРЖИК (Jan Mařík), Прага.

(Поступило в редакцию 10/Х 1955 г.)

Пусть m — натуральное число: пусть \mathcal{K}_m — теморове евисниднов пространство. Для веняюто ограниченного вымеримого множества $A \subset \mathcal{K}_m$ положим $\|A\| = \sup \int_{-\infty}^{\infty} \frac{\partial v_i(x)}{\partial x_i} dx$, где v_1, \ldots, v_m — многочлены такие, что $\sum_{i=1}^{\infty} v_i^0(x) \le 1$ для всех $x \in A$. Пусть \mathfrak{A} — система всех ограниченных вымеримых множества A, для когорых $\|A\| < \infty$. Тоорема 18 гогда утверясают:

Пусть $A \in \mathfrak{A}$; пусть D — граница множества A. Тогда на системе В всех борелевских подмножеств множества D существует мера p и на

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ИОСИФ ВИССАРИОНОВИЧ СТАЛИН 1879—1953

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How to Find? Search!

- ① an entry gate to the digitized papers is **search**
- ② full text searching
- ③ searching for intext references
- ④ search and exchange of mathematical formulas: MathML, OpenMath
- (5) due to the massive size of digitized material, the only way is very good OCR, including math.

Math OCR – Why?	OCR for Mathematics – How?	DML-CZ OCR	Results	Summary and Further Work
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(Fine+Infty)Reader				

Existing OCR Systems

- Not to reinvent the wheel: trial of several OCR engines.
- ② No single OCR system with acceptable results: high error rate, working only for specific purposes (plain English text), direct use was not possible.
- ③ Fine Reader by ABBYY gave good results for (even multilingual) text, and allows for typeface learning.
- InftyReader by www.inftyproject.org the only available solution for structural math recognition.
- $\label{eq:solution}$ S No out-of-the-shelf solution.

Math OCR – Why? 000000	OCR for Mathematics – How? ○●	DML-CZ 0CR 000000	Results 00	Summary and Further Work
(Fine+Infty)Reader				

Our OCR Solution

- ① combining both, using FineReader and InftyReader in a pipe to let every system to do what it is good for, then 'vote'
- ② top-level (Java) program to **automate** the process **and fix** some indeficiencies
- ③ instant setup unusable: fine-tuning and gradually enhancing the OCR procedure and program parameters so that OCR results would be acceptable for DML-CZ purposes
- ④ trying to improve the results further by close cooperation with the team of prof. Masakazu Suzuki (Infty Project leader, Kyushu University, Japan), and hopefully with other (retrodigitization) projects efforts.

Math OCR – Why?	OCR for Mathematics – How?	DML-CZ OCR	Results	Summary and Further Work	
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Workflow of DML-CZ at Various Levels of Detail

DML-CZ OCR Workflow Diagram



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DML-CZ OCR Workflow - middle level of details I

- 1 Choosing the testbed data (30.000 pages of CMJ since 1951).
- ② Scanning 600 DPI, 4-bit depth (soft binarization advantage).
- ③ Lookup for hot typefaces used in CMJ.
- $\circledast\,$ Training the Fine Reader (FR) 8.0 OCR engine for the fonts used.
- ⑤ Training the Lingua::Ident Perl module for language identification of languages used in CMJ (EN, RU, F, GE, CZ, SK): very reliable statistical method based on character bigrams and trigram counts.
- ⑥ FR scanning using general setup profile (no specific language vocabulary used).
- $\ensuremath{\textcircled{O}}$ Evaluating the language of the scanned block.
- ③ Calling FR to scan for the 2nd time with profile appropriate to the recognized language(s).

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 Workflow of DML-CZ at Various Levels of Detail
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DML-CZ OCR Workflow – middle level of details II

- Export the result as layered PDF (+FineReader XML).
- 2 Importing this PDF by InftyReader.
- InftyReader recognition and storing the result Infty Markup Language IML (XML+MathML) and 上EX.
- Running (our Java) program OMLCorrector to fix some Infty Reader indeficiencies in IML.
- Running (our Java) program OCRJoiner to compare characters in bounding boxes by FR and InftyReader and store the final result in IML.
- $\textbf{6} \quad \text{Use the resulted files in further DML-CZ workflow}.$

Math OCR – Why?	OCR for Mathematics – How?	DML-CZ OCR	Results	Summary and Further Work
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Workflow of DML-CZ at Variou	us Levels of Detail			

OCR XML Postprocessing

<mblock>

```
....
<munit entity="1" ocrparam="685,1746,704,1758,0">
check
<mlink type="under">
<munit ocrparam="684,1761,707,1794,0">s</munit>
</mlink>
</munit>
....
<mblock>
is transformed to
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. . .

<char ocrparam"684,1746,707,1794" entity="1">š</char>

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Workflow of DML-CZ at Various Levels of Detail

DML-CZ OCR Workflow Implementation Gory Details





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Gradual Improvements o	FOCR			
Evaluation				

Type of errors: T (text), D (diacritics), M (mathematics), L (layout) Steps: 1 (FR1), 2 (FR2), 3 (Infty), 4 (OCRJoiner), 5 (IMLCorrector)

Step	Т	D	М	L
1	10	0	224	82
2	4	0	170	78
3	4	0	168	71
4	14	0	24	15
5	14	0	24	15

Math OCR – Why?	OCR for Mathematics – How?	DML-CZ 0CR	Results	Summary and Further Work
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Gradual Improvements of OCR				

DML-CZ OCR Results

FR 1	FR 2	FR8.0 PE	IR	IR fixed
84,99%	88,03%	88,46%	97,48%	97,48%
86,93%	88,76%	88,07%	98,97%	98,97%
89,19%	92,35%	91,53%	99,18%	99,18%
93,40%	93,52%	95,78%	99,15%	99,19%
91,09%	91,62%	92,15%	99,87%	99,87%
79,46%	80,05%	82,25%	99,61%	99,61%
92,59%	93,39%	93,71%	99,09%	99,09%
91,33%	91,33%	98,30%	98,18%	98,61%
88,65%	89,90%	91,23%	98,97%	99,02%
	FR 1 84,99% 86,93% 89,19% 93,40% 91,09% 79,46% 92,59% 91,33% 88,65%	FR 1FR 284,99%88,03%86,93%88,76%89,19%92,35%93,40%93,52%91,09%91,62%79,46%80,05%92,59%93,39%91,33%91,33%88,65%89,90%	FR 1FR 2FR8.0 PE84,99%88,03%88,46%86,93%88,76%88,07%89,19%92,35%91,53%93,40%93,52%95,78%91,09%91,62%92,15%79,46%80,05%82,25%92,59%93,39%93,71%91,33%91,33%98,30%88,65%89,90%91,23%	FR 1FR 2FR8.0 PEIR84,99%88,03%88,46%97,48%86,93%88,76%88,07%98,97%89,19%92,35%91,53%99,18%93,40%93,52%95,78%99,15%91,09%91,62%92,15%99,87%79,46%80,05%82,25%99,61%92,59%93,39%93,71%99,09%91,33%91,33%98,30%98,18%88,65%89,90%91,23%98,97%

Math OCR – Why?	OCR for Mathematics – How?	DML-CZ OCR	Results	Summary and Further Work
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Conclusions

- 🖙 less than 1% error rate (counting **all** types of errors).
- still space for improvements (better text/math separation and Unicode support in InftyReader)
- Image possible merging of DML-CZ OCR (FR based) with Infty into one application?
- problems during FR SDK recognition of low quality images solved in the latest version of SDK

Math OCR – Why? 000000	OCR for Mathematics – How? 00	DML-CZ OCR 000000	Results 00	Summary and Further Work
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That's it!

Thanks for all contributions we build upon The end of the story Questions?

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