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Distributed LTL Model-Checking in SPIN*

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Abstract

Distributed version of the SPIN model checker has not been extended to allow distributed model-checking of LTL formulas. This paper explores the possibility of performing nested depth first search algorithm in distributed SPIN. A distributed version of the algorithm is presented, and its complexity is discussed.

1 Introduction

Verification of complex concurrent systems requires techniques to avoid the state-explosion problem. Several methods to overcome this barrier have been proposed and successfully implemented in automatic verification tools. As a matter of fact, in application of such tools to practical verification problems the computational power available (memory and time) is the main limiting factor. Recently, some attempts to use multiprocessors and networks of workstations have been undertaken.

In [UD97] the authors described a parallel version of the verifier Mur φ . The table of all reached states is partitioned over the nodes of the parallel machine thus allowing the table to be larger than on a single node and perform the explicit state enumeration in parallel. A similar approach to parallel/distributed version of reachability analysis has been taken in [LS99]. The distributed version of SPIN [Hol97] uses different ways to partition the state space than Parallel Mur φ . Yet another distributed reachability algorithm has been proposed in [AAC87], but has not been implemented.

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The authors of the distributed version of SPIN have not considered the implementation of LTL model-checking based on nested depth first search because their algorithm performs a non-nested depth first visit of the state space. In this paper, we present a distributed algorithm which uses nested depth first visits to check LTL formulas. The basic idea is as follows. The algorithm starts to explore the state space in the same way as the distributed SPIN does, that is it uses (non-nested) distributed depth first visits. When a nested DFS procedure should be started for an accepting state of the Büchi automaton, called here a *seed*, the seed is remembered in a special data structure (dependence structure), nested DFS procedure is not started and the algorithm continues its distributed search. Nested DFS procedures for seeds are started separately in appropriate order given by the dependency structure and only one nested DFS procedure can be started at a time. The algorithm thus performs a limited nested depth first search and requires some synchronisations during its execution. Our aim was to experimentally explore how much will the synchronisation influence the overall behaviour of the tool. To our surprise, even using this very simple method one is able to deal with verification problems larger that those that can be analysed with a single workstation running the standard (non-distributed) version of SPIN.

The experimental version of the algorithm has been implemented and a series of preliminary experiments has been performed on a cluster of nine PC based Linux workstations interconnected with a 100Mbps Ethernet and using MPI library. We intent to report on the experimental work separately.

The rest of the paper is organised as follows. We start with a section which briefly describes the distributed version of SPIN. The following section explores in more detail the main reasons why it is difficult to extend directly the distributed SPIN to check LTL formulas and also suggests some possible solution. Then we describe the additional data structures required by our algorithm and present the pseudo-code of the algorithm. Finally, complexity and effectiveness of the algorithm are discussed.

2 Distributed SPIN

In this section we briefly summarise the main idea of the distributed version of SPIN as presented in [LS99]. The algorithm partitions the state space into subsets according to the number of network nodes (computers). Each node is responsible for its own part of the state space. When a node computes a new state, first it checks (using the procedure Partition(s)) if

the state belongs to its own state subset or to the subset of another node. If the state is local, the node continues locally, otherwise a message containing the state is sent to the owner of the state. Local computations proceed in the depth first search manner using the procedure DFV (a slight modification of the SPINs DFS procedure). However, due to the distribution of work, the *global* searching does not follow the depth first order. This is also one of the reasons why this algorithm cannot be used for LTL modelchecking. The algorithm uses a new data structure U[i] holding the information about pending requests on the node *i*. The distributed algorithm terminates when all the U[i] queues are empty and all nodes are idle. To detect termination a *manager process* is used. Each node sends to the manager a message when it becomes idle and a different one when it becomes busy. Correct termination requires the re-confirmation from each node and the overall number of messages sent and received must be equal.

The pseudo-code bellow illustrates the original algorithm used in the distributed version of SPIN.

```
procedure START(i, start_state);
begin
  V[i] := {}; { already visited states }
  U[i] := {}; { pending queue }
  j := Partition(start_state);
  if i = j then
  begin
    U[i] := U[i] + start_state;
  end;
  VISIT(i);
end;
procedure VISIT(i);
begin
  while true do
  begin
    while U[i] = {} do begin
                        end;
    S := extract(U[i]);
    DFV(i,S);
  end;
end;
```

```
procedure DFV(i, state);
begin
  if not state in V then
  begin
    V[i] := V[i] + state;
    for each sequential process P do
    begin
      nxt = all transitions of P enabled in state;
      for each t in nxt do
      begin
        j = Partition(st);
        if j = i then
        begin
          DFV(i, st);
        end
        else
        begin
          U[j] := U[j] + st;
        end;
      end;
    end;
  end;
end;
```

3 Problems with Extending the Distributed SPIN

When we want to adopt directly the technique of nested DFS approach to distributed computing we encounter two main problems. By simply allowing more nested DFS procedures for different seeds we may obtain an incorrect result, which can be demonstrated by the following example:



If two nested DFS procedures were run simultaneously on both seeds A and B then the cycle through the state B might not be detected. The outcome depends on the relative speeds of both nested DFS procedures. In case that the nested DFS procedure originating from A visits the state C first, the nested DFS procedure starting in B will not be allowed to continue through C and, as a result, the cycle B, C, D, B will not get detected.

In general, whenever the subgraphs generated by two different seeds do not have an empty intersection there is a possibility that some cycle may not be detected. A simple criterion to determine whether it is possible to run two or more nested DFS procedures in parallel is to find out whether the corresponding intersections are empty or not. However, verifying this condition could result in searching the entire state space which may be too ineffective.

An obvious solution to this problem is to store for each state the information in which nested DFS procedure the state was visited. This would mean to store a nontrivial amount of information because each state might be a seed, in which case the space complexity of the additional storage may turn out to be quadratic with respect to the number of states. This is the reason why we do not allow to run more nested DFS procedures simultaneously.

Another problem is the following. The original distributed version of SPIN from [LS99] does not preserve the depth-first-search order of visited nodes. This is not a problem in the case of reachability analysis because the only relevant information is whether a given state was visited or not. However, this may pose a threat to the correctness of the full model checking procedure which is shown on the following example:



A correct run through this graph (when DFS procedure goes back we use a dashed edge, runs of nested DFS are put into brackets), in which the cycle through *C* is detected, is:

$$[1, 2, 3, 4, \overline{4}, \overline{3}, [3, 4, 2, \circ]^C$$

An incorrect run, in which the correct order of seeds is not preserved, is for instance

$$[1, 2, 3, 4, \overline{4}, \overline{3}, \overline{2}, \overline{1}, [1, 2, 3, 4, \overline{4}, \overline{3}, \overline{2}, \overline{1}]^A, [3.\overline{3}]^C$$

A possible solution to this problem was proposed in [LS99]. It is based on the original distributed SPIN procedure for reachability analysis and consists of adding synchronisation to the distributed algorithm. The synchronisation is done by sending suitable acknowledgements that will exclude the possibility of a seed being processed before another seed that is "below" avoiding thus incorrect runs where cycles may not be detected. This solution cuts off any parallelism and so in fact does not perform better than the plain sequential algorithm.

What we propose here is an attempt to provide a more subtle solution that makes it possible to effectively tackle larger tasks than standard SPIN within reasonable space limits. The idea is to reduce the necessary synchronisation by using additional data structures with limited space requirements.

Yet another important issue that must be taken into consideration is that a distributed version of SPIN and hence our extension is based on the original (sequential) SPIN and it should not exclude the use of the other main memory and complexity reduction techniques available in SPIN, such as state compression, partial order reduction, and bit state hashing. The approach we consider here is compatible with such mechanisms as much as possible.

4 Distributed Model-Checking Algorithm

From the discussion in the previous section it is clear that it is crucial to take care about the order in which individual nested DFS procedures are performed. We need to make sure that the following invariant will always hold for each distributed computation:

A nested DFS procedure is allowed to begin from a seed S if and only if all seeds below S have already been tested for cycle detection.

Different states, hence also seeds, of the state space are processed on different nodes in accordance with the partition function. Hence, it may occur that for a seed S, a computation of the subgraph generated by S is interrupted and continues on a different node. We need to keep track of such situations.

In order to represent dependencies between states (corresponding to computations transferred to other nodes) we shall build a dynamic structure that will keep this necessary information. We need to remember the states which caused the computation to be transferred to other nodes and we call them *boarder states* (see Figure 1). We shall also include all the seeds that appear during the computation in order to ensure the correct order of performed nested DFS procedures. Each node maintains its own structure and we call it *DepS* (Dependency Structure).

4.1 Dependency Structure

Dependency structure (DepS) for a node n is a graph whose vertices are either seeds of the local state space of the node n or the border states for the node n indexed by a set of node names. A border state of node n is a state belonging to the node n whose incoming or outcoming edge crosses to another node. A border state for a node n is either the border state of node n whose predecessor is a border state of another node or a border state of another node whose successor is the border state of node n (see Figure 1 for a graphical explanation). The starting state of the entire state space is also a vertex in the DepS for the node running manager process. Note that a seed (or the starting state) can be a border state. In this case it will occur only once in the structure (as a seed and and a border state at the same time). Indexes in vertices corresponding to border states represent the nodes from which the computation was transferred to the border state.



Figure 1: Border States and Seeds

The edges in the DepS for a node *n* represent the reachability relation between states (and provide the crucial information to perform nested DFS procedures in a "correct order"). The dependency structure is a forest-like structure and is built dynamically during the computation of DFS procedure. All vertices in the structure are the states actually *visited* by the algorithm during depth-first search. For each vertex its immediate successors contain the states (seeds or border states) which the vertex is "waiting for" in the sense that the states must be processed (checked for nested DFS in case of seeds) before the state corresponding to the vertex can be processed.

The structure DepS is changing dynamically as the computation continues. Whenever DFS procedure comes to a not yet visited seed or a border state a new vertex corresponding to the state is added to the structure as the immediate successor of the last visited state which is present in the structure. Moreover, in the case of a border state a request to continue with DFS procedure is sent to the node of the border state (if not already sent before).

During the computation each node receives requests from other nodes to continue a walk through the state space. These requests are remembered in a local queue of pending requests and the queue is processed in the standard FIFO manner. For each request it is first checked whether the state is in the set of visited states. If it is, then it is checked whether there is any vertex in the (local) DepS structure containing the same state. If yes, then the "name" of the node who sent the request is added to its index. If the request is not in the DepS structure and it is in the set of visited states, then an acknowledgement of the request is sent back. If the request is not in the set of visited states (hence not in DepS) a new *root* vertex is added to DepS with the "name" of sending node as its index.



Figure 2: Example of dependency structures

Removing a vertex from the dependency structure is possible only when DFS procedure went up through the state already. The removing procedure first checks whether the state associated with the vertex is a seed, in which case the state is added to the global queue of seeds waiting for nested DFS procedure. For any state all acknowledgements are generated according to the (vertex's) index. Then the vertex is removed from the structure. Removing any vertex may make its parent's successor list empty and so cause also removing of the parent and parent's parent and so on.

Whenever the DFS procedure goes up through a state with a vertex in DepS, it is checked whether the vertex is a leaf of the tree. If it is the case the removing procedure is initiated. Removing procedure can also be initiated by incoming acknowledgements.

In the Figure 2 the dependency structures for nodes I, II and III are shown before removing any vertex.

4.2 Manager process

Distributed SPIN uses a manager process that is in charge of starting the verification program in a predetermined set of network nodes, and of stopping it after having detected termination and collects the results. In our version of distributed SPIN we will in addition require that the manager process is in charge of initiating the nested DFS procedures in accordance with the method described in previous sections.

All nodes involved in the computation communicate with the manager process by sending information about their status. The status of each node is determined by: *DFS status, nDFS status, numbers of sent and received requests (DFS and nDFS packets)*. The DFS status can be *busy, idle-empty-DepS* and *idle-nonempty-DepS*. The nDFS status can be only *busy* or *idle*. In this way, the manager process has a local representation of the current state of all the nodes.

Nested DFS procedures

As we have mentioned before, our approach relies on the requirement that only one nested DFS procedure is allowed at a time. This is the reason for sending the seed to the manager process instead of starting the nested DFS procedure immediately during the DFS procedure. The manager process maintenance global queue of seeds waiting for their nested DFS procedures. It starts the nested DFS procedures for the first seed in the queue if and only if no other nested DFS procedure is running. The seed is removed from the queue after the manager process has started the nested DFS procedure for it. The information necessary to decide on starting a new nested DFS procedure can be obtained in the same way as described in [LS99], that is by checking the nDFS status of all nodes to be equal to *idle* and checking that the global number of all nDFS packets sent equals the global number of all nDFS packets received.

Termination detection

The distributed algorithm must terminate when there is no waiting seed in the global queue, no nested DFS procedure is running, the global numbers of sent and received DFS packets equals and all nodes have an *idle-empty-DepS* DFS status.

Termination detection can be handled in similar way as it is done by the distributed SPIN. The only exception is the situation when the global numbers of sent and received DFS packets equals, no computer has the *busy* DFS status, but some node has the *idle-nonempty-DepS* DFS status. In this case the manager process asks all the nodes with the *idle-nonempty-DepS* DFS status for some information about their *DepS* structures. The nodes reply by sending the following elements of their *DepS* structure: $X_Z \xrightarrow{u} Y$, where X is a node from the *DepS* structure which has a nonempty index Z, Y is the node according to the boarder state which is the X waiting for. The edge has a label u which is a flag whether there is a seed between X and Y including X and excluding Y in the original *DepS* structure. So u can be either 1 = with a seed or 0 = without a seed. After receiving all the elements, the manager process builds a temporary graph from incoming elements. After that it finds the maximal strongly connected component in the graph which has no outgoing edges using standard Tarjan's algorithm [Tar72]. Note, that such a strongly connected component must exist. The manager process checks for the presence of an edge with label 1 in the strongly connected component. If there is no such edge then an acknowledgement is generated for arbitrary node from the found component. After the acknowledgement is sent out to the appropriate node the whole graph is forgotten and the distributed computation continues in standard way. In the other case, i.e. when there is a cycle labelled by 1 in the temporary graph, it is clear that a cycle through an accepting state must exist in the original state space and therefore the verified property does not hold. In this case the algorithm terminates immediately. The whole situation is shown in the Figure 3.

4.3 The Algorithm

Our algorithm extends the distributed algorithm from [LS99] and it uses the same distributed method for reachability analysis. This ensures that we do not exclude the use of the main memory and complexity reduction techniques available in SPIN.

The main idea of the entire distributed model-checking algorithm is the



Elements sent to manager process are: $B_{\{II\}} \xrightarrow{1} C, A_{\{I\}} \xrightarrow{1} B, C_{\{I\}} \xrightarrow{0} B$ Constructed graph is: $A_{\{I\}} \xrightarrow{1} B_{\{II\}} \xrightarrow{1} C_{\{I\}}$

The strongly connected component without outcoming edges is: $B_{\{II\}} \underbrace{1}_{C} C_{\{I\}}$

A cycle through an accepting state has been found.

Figure 3: Example

following. The whole reachable graph is partitioned into as many regions as the number of network nodes. Each node does the computation on the states belonging to its own region. When a successor belonging to other region is generated the message containing the new state is sent to its owner. Received messages are stored in the (remote) queue and processed in sequence. Only those states are explored which have not been visited yet. This is true for both the DFS and the nested DFS procedures. In contrast with the original algorithm, not all visited states are permanently stored in the set of visited states but only the boarder states and the seeds are. Each node holds the set of permanently visited states in the array PV[i]. To prevent cycling through not permanently stored states the algorithm holds the set of all visited states within the processing of one of the received request. This temporally set is hold in the array V[i] end is initialised to \emptyset before processing another request (state) from the queue of pending requests U[i].

To ensure the right order of nested DFS procedure calls an additional data structure DepS is maintained (see subsection 4.1). This structure is

being built, using one temporary pointer Last_visited, by the procedures CREATE_IN_DepS(s) and ADD_TO_DepS(s1,s2). A new root vertex in the dependency structure which corresponds to the state s is created by the procedure CREATE_IN_DepS(s). Procedure ADD_TO_DepS(s1,s2) creates a vertex corresponding to the state s2, if it does not exist yet, and adds an edge between the vertices corresponding to the states s1 and s2. Vertex corresponding to the state s, in the pseudo-code written as $\langle s \text{ in } DepS \rangle$, is composed from several components (fields): *parent*, *successors*, *state*, *DFS_gone* and *index*. The field *parent* points to the vertex for which this vertex has been created as a successor. The field *index* is a set of names of nodes. The *DFS_gone* field is a flag indicating whether the DFS procedure has already walked through the state up. The meanings of the fields *successors* and *state* are obvious.

Some additional local variables are used in the algorithm. The meanings of Seed, state, came_from and tmp is obvious. The variable toplevel is used to differ whether the procedure DFV was called recursively from DFV or if it was called from the VISIT procedure. The variable Seed_queue is a global variable which is maintained by the MANAGER_PROCESS. It represents the queue of waiting seeds for their nested DFS procedure to be started.

All nodes execute the same code. For simplicity reasons we assume that the master node runs the manager process only. The DFS procedure is started by calling procedure START(i,starting_state). The value of i is the name of the node (integer). The procedure puts the starting_state into the queue of pending request U[i] at the proper node i. The procedure VISIT(i) is called for all nodes except the master one at the end. The MANAGER_PROCESS procedure is called at the master node. The task of the MANAGER_PROCESS procedure has been explained in the subsection 4.2.

The PROCESS_INCOMING_PACKETS procedure is actually a boolean function which returns false if the computation should be stopped for some reason and returns true otherwise. This function plays the role of the client side of the manager process. It updates the numbers of locally received and sent packets and sends this numbers and the information about the node status to the manager process. It also processes all incoming packets. The requests are stored to the U[i] queue, the acknowledgements are collected and the REMOVE procedure is called for them. Also all control packets are handled by it.

Procedure VISIT waits for the queue U[i] to be nonempty. It collects the request from the queue, resets the variables toplevel and V[i]. In the

case that the request is a new one (it is not in the PV[i] set) the procedure DFV is called appropriately. It is necessary to make difference between the first DFS procedure and the nested DFS procedure. In the case of nested DFS procedure the variable Seed must be set, on the other hand in the case of DFS procedure appropriate actions on the DepS structure are performed. The states already processed, which are requested again, are checked for presence in DepS structure. If the corresponding vertex exists its index is updated only, the acknowledgement is generated otherwise.

The DFV procedure checks whether the state belongs to the same node. If no, the message containing the state is sent to the node owning the state and the DepS structure is updated. (Note: In the case of nested DFS procedure the seed, which is the nested search running for, is included in the message as well.) When the DFV procedure is called from the VISIT procedure a new root vertex to the DepS structure must be added and the state must be stored in the set of permanently visited states PV[i]. Also in the case that the state is a seed it is necessary to update the DepS structure. Note that the DepS structure is maintained only for the first DFS procedure and not for the nested DFS procedure. Conversely the check whether the reached state is the Seed is done only in the nested DFS procedure. The CYCLE_FOUND procedure informs the manager process about the fact that a cycle has been found. Before all the successors of the state are generated the state is added to the set of actually visited states (V[i]). Not visited successors are handled by recursive calling of procedure DFV. If the successor is a seed or a border state which is in the DepS structure already (so it must be in PV[i]), the appropriate edge is added to the DepS structure. After all successors of the state have been processed and the state is a seed, the check whether there are any more successors of the corresponding vertex in the DepS structure is performed. In the case there are no successors the vertex is removed from DepS by the procedure REMOVE.

Procedure REMOVE (vertex) is crucial with respect to maintaining the DepS structure. It is responsible not only for freeing the vertices from the memory but also for sending the seeds to the global queue (Seed_queue) and for sending all appropriate acknowledgements (this is done by procedure ACK(vertex)). Also, it is responsible for the recursive removing of vertices. See the pseudo-code for details.

Note that the same state can be visited twice. In the DFS procedure and in the nested DFS procedure. To store the information about the fact that the state has or has not been visited in one or both DFS procedures only one additional bit is required (see [Hol91]). We suppose that this one additional bit is included in the bit vector representing the state. That's why the bit vectors representing the same state differ in the case of DFS procedure and nested DFS procedure.

The Partition function is used for partitioning of state space. The choice of "good" partition function is crucial in the distributed algorithm because a "bad" partition of states among the nodes may cause communication overhead. This was explained in [LS99] where also a few partition function has been proposed and tested.

The pseudo-code of the new algorithm follows:

```
procedure START(i,start_state)
begin
  DepS := {};
  U[i] := {};
  PV[i] := {};
  Last_visited := nil;
  Seed := nil;
  if (i = Partition(start_state)) then
  begin
    U[i] := U[i] + {start_state};
  end;
  if (i = 0) then
  begin
    MANAGER_PROCESS();
  end
  else
  begin
    VISIT(i);
  end;
end.
procedure VISIT(i)
begin
  while (PROCESS_INCOMING_PACKETS()) do
  begin
    if (U[i] <> {}) then
    begin
      get (state, came_from) from U[i];
      toplevel := true;
      V[i] := {};
      if (state not in PV[i])) then
      begin
        if (Nested(state)) then
        begin
```

```
Seed := state.seed;
          DFV(i,state);
        end
        else
        begin
          DFV(i,state);
          if (<state in DepS>.successors = {}) then
          begin
            REMOVE(<state in DepS>);
          end;
        end;
      end
      else
      begin
        if (state in DepS) then
        begin
          <state in DepS>.index := <state in DepS>.index
                                    + {came_from};
        end
        else
        begin
          ACK(<state in DepS>);
        end;
      end;
    end;
  end;
end.
procedure REMOVE(vertex)
begin
  if Accepting(vertex.state) then
  begin
    Seed_queue := Seed_queue + {vertex.state};
  end;
  ACK(vertex);
  tmp:=vertex.parent;
  tmp.successors := tmp.successors - {vertex};
  free(vertex);
  if ((tmp.successors = {}) and (tmp <> nil)
                             and (tmp.DFS_gone)) then
  begin
    REMOVE(tmp);
  end;
end.
```

```
procedure DFV(i,state)
begin
  if (PARTITION(state) <> i) then
  begin
    U[PARTITION(state)] := U[PARTITION(state)] + {state};
    if (not Nested(state)) then
    begin
      ADD_TO_DepS (Last_visited, state);
    end;
    return;
  end;
  if (toplevel) then
  begin
    toplevel := false;
    PV[i] := PV[i] + state;
    if (not Nested(state)) then
    begin
      CREATE_IN_DepS(state);
      Last_visited := state;
    end;
  end;
  if (Accepting(state)) then
  begin
    if (not(toplevel) and (not Nested(state))) then
    begin
      ADD_TO_DepS(Last_visited,state);
      Last_visited := state;
      PV[i] := PV[i] + state;
    end;
  end;
  V[i] := V[i] + {state};
  for (newstate in successors of state) do
  begin
    if (Nested(state) and (Seed=newstate)) then
    begin
      CYCLE_FOUND();
    end;
    if (newstate not in (V + DepS + PV[i])) then
    begin
      DFV(i,newstate);
    end
    else
    begin
      if (newstate in DepS) then
      begin
```

```
ADD_TO_DepS (Last_visited,newstate);
end;
end;
if (Accepting(state) and (not Nested(state))) then
begin
Last_visited := <Last_visited in DepS>.parent;
<state in DepS>.DFS_gone := true;
if (<state in DepS>.successors = {}) then
begin
REMOVE(<state in DepS>);
end;
end;
end;
end;
```

5 Complexity and effectiveness

We shall try to estimate the overall size of the dependency structures constructed during the distributed computations. For any node, there are two kinds of states stored in the structure – all *seeds* that are visited by this node, and all states that arise in the computation but are transferred to another node in accordance with the partition function (*border states*). The number of the latter is crucial because this can be in the worst case square wrt the overall number of states.

The partition function we employ was originally proposed in [LS99] where it was also shown that with this function, the fraction of border states in the global state space is at most $\frac{2}{P}$, where *P* is the number of processes. The number of border states *T* is bounded by the expression $S \times R$, where *S* is the number of states and *R* is the maximum of out-going degrees over all states. *R* is at most $P \times ND$, where *ND* is the maximal number of nondeterministic choices of a process. Thus we get that $T \leq (S \times P \times ND)$ and the average number of border states is $\frac{2}{P} \times S \times P \times ND = 2S \times ND$. Hence, the number of states stored in the dynamic structure is on average $S + 2(2S \times ND)$ which works out to be $O(S \times ND)$. In most real systems the amount of non-determinism (represented by *ND*) is limited and small. We may conclude that the memory complexity of the distributed algorithm is on average linear in the size of the state space and the factor given by non-determinism.

We will compare our approach with the simple method of synchronisation proposed in [LS99]. We will look in detail at how the first and nested depth-first-search procedures work. The first DFS searches through the state space and marks accepting states (seeds) with a particular kind of flag. The computation of first DFS is completely asynchronous and is never halted before the whole state space is searched. The nested DFS searches in a similar, i.e. distributed, way the subgraph rooted in the currently processed seed. If there are seeds ready to be processed the nested DFS is running in parallel with the first DFS. Therefore this method allows parallel computations which are almost disabled in the simple synchronisation technique.

6 Conclusions and Future Research

We have proposed an extension to the existing distributed algorithm used in the verification checker SPIN which allows to model-check LTL formulas. This problem was suggested in [LS99] and left unsolved. The method used is very simple and requires some synchronisation between nodes. The resulting algorithm has been implemented and we have performed several experiments on a cluster on workstations. We have used artificial verification problems to test the performance of the algorithm. Our results show, that it is possible to increase the capability of SPIN to check LTL formulas.

There are several problems we intent to consider in the future. First, we have used MPI library to get a fast prototype implementation. However, the overhead caused by this communication infrastructure is quite high and using another communication infrastructure (like TCP/IP) will certainly lead to better performance. Second, we have used the partition function from SPIN. Partition function plays crucial role and techniques particularly suited for model-checking LTL formulas should be investigated. The main open problem is to find a general strategy for distributed nested depth first search algorithm.

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