Sail Shreds

Input files: /mo/public/problem/sail/01.in, ..., 10.in
Output files: 01.out, ..., 10.out
Time limit: 5 hours :) 
Source code: none!

During the recent two-day storm, a group of sailors shipwrecked on a desert island in the Mediterranean sea. Since their radio is broken, they cannot call for help and their only chance of survival is escaping on a raft. However, they need a sail to power the raft. Luckily, they recovered the main sail from the wrecked ship, but it is torn to several shreds. Hence, they have to sew the shreds together to obtain the original sail.

The sailors quickly realized that each of the shreds is a triangle. Because there were stripes on the sail, it was easy to identify the correct orientation of its triangular parts. In fact, they have to respect the orientations of the shreds, since otherwise the sail would be less resistant to wind and might be torn again. They were trying to find the original arrangement for several hours but with no result. They think that a computer can help them and asked you for help.

Task

You are given the description of the triangular shreds (given by the plane coordinates of the vertices of each triangle) and the dimensions of the original sail which was a rectangle (given by two integers $X$ and $Y$). Your task is to move the shreds (without rotation) to reconstruct the original sail (see the figure). In particular, the triangles should be moved in such a way that

- the whole rectangular area is covered,
- no two triangles intersect, i.e., there is no point which is contained in the interiors of two different triangles, and
- there is no triangle whose part lies outside of the rectangle.

You may assume that there exists a solution for each of the input data. In particular, it holds that the sum of the areas of the shreds is equal to the area of the original sail. There can be several shreds of the same shape.
Description of input

You are not supposed to submit the program to solve the described task. Instead, in the directory /mo/public/problems/sail, you find files 01.in...10.in. The files are the input data of each of the test cases.

Each of the input files (01.in...10.in) describe a single test case and has the following structure. The first line contains three integers $N$, $X$, and $Y$, separated by single spaces. $X$ and $Y$ ($1 \leq X, Y \leq 1000000$) determine the dimensions of the original sail, $X$ being the width and $Y$ being the height, and $N$, $2 \leq N \leq 1000$, is the number of triangular shreds of the sail.

The next $N$ lines describe the individual triangles: $(i+1)$-th line contains six integers $A_{i,x}, A_{i,y}, B_{i,x}, B_{i,y}, C_{i,x}, C_{i,y}$ separated by single spaces. These six numbers describe the three vertices $A_i, B_i, and C_i$ of the $i$-th triangle: the vertex $A_i$ has coordinates $(A_{i,x}, A_{i,y})$, $B_i$ has coordinates $(B_{i,x}, B_{i,y})$, and $C_i$ has coordinates $(C_{i,x}, C_{i,y})$. You may assume that $0 \leq A_{i,x}, A_{i,y}, B_{i,x}, B_{i,y}, C_{i,x}, C_{i,y} \leq 1000000$.

Note that the position of a triangle (specified in the input file) is irrelevant. E.g., if the third line of the example input were replaced with $661\ 451\ 66$, the given set of the triangular shreds would be the same.

Description of output

For each input file, you should create a corresponding output file 01.out ...10.out. You should not submit any program files for this problem.

The output file $XX.out$ should consist of exactly $N$ lines describing the arrangement of the shreds of the sail such that all the three conditions in the task description are met. More specifically, the $i$-th line should contain two integers, $A_{i,x}^*$ and $A_{i,y}^*$ separated by a single space—the coordinates of the point $A_i$ after moving the $i$-th shred to the appropriate place. Note that the left bottom corner of the sail has always coordinates $(0, 0)$ and the right top has coordinates $(X, Y)$ as depicted in the figure.

Example

The following input and output correspond to the picture (note that the shreds in the left part of the picture reflect only the given shapes of the shreds and not their positions).

Input:
6 10 5
4 0 12 4 4 5
4 5 12 4 14 5
0 3 10 3 4 5
4 5 10 3 8 7
7 7 10 5 11
0 1 2 0 2 2
Testing your solutions before submission

In order to help you with finding the solution, there is a simple program you can use to check if your output is correct and visualize the solution. The program is called with two parameters using the following command: `draw_sail XX.in XX.out` where XX.in is one of the input files and XX.out is the corresponding output file. The program will generate and display a postscript file depicting the assembly of the sail and check it for errors. In particular, the areas of the sail covered by no triangles will be red, areas covered by more than one triangle will be blue, and the parts of triangles lying outside of the sail will be green. Don’t forget that you can use the zoom in/zoom out functionality of the program gv to display details of the sail. You can also directly print the picture corresponding to the output file from the program gv.